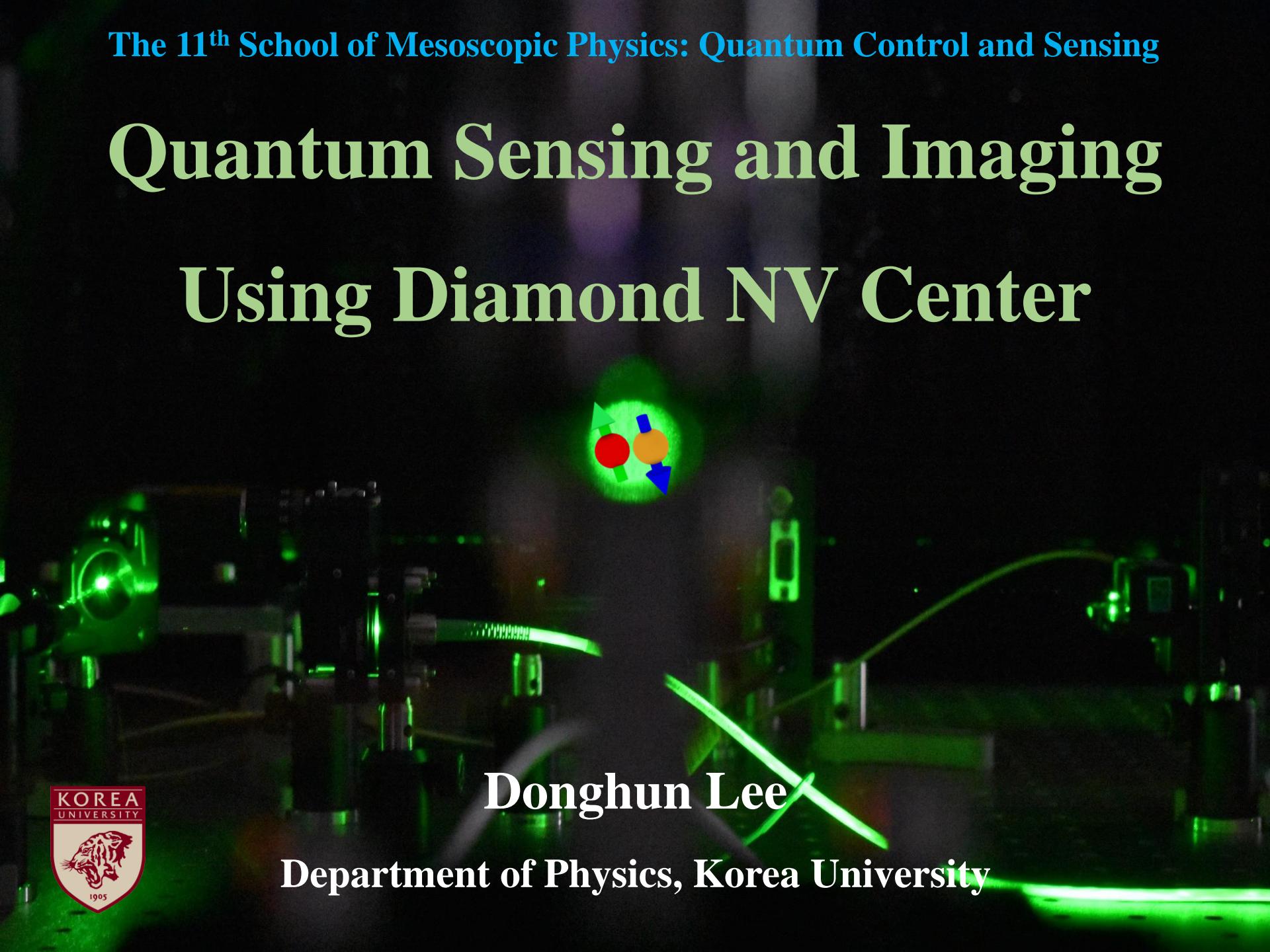


# Quantum Sensing and Imaging

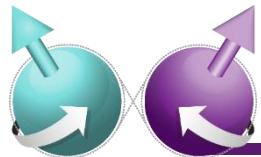
## Using Diamond NV Center



Donghun Lee

Department of Physics, Korea University

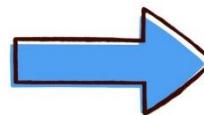




# Beginning the era of quantum technology

## Quantum Mechanics

- Duality
- Uncertainty
- Superposition
- Entanglement



## Quantum Technology

- Quantum computation
- Quantum communication
- Quantum simulation
- Quantum sensing

반도체 이론, 기초 실험



Se photocell (1931, Weston)



진공튜브 컴퓨터 (1946, ENIAC)

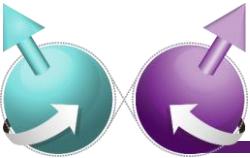
양자정보 이론, 기초 실험



양자센서 (?)



양자컴퓨터 (?)



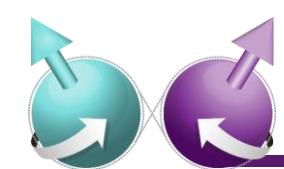
# Quantum sensing ?

개념 및 정의	참고문헌
양자시스템(예, 큐비트) 또는 양자결맞음(예, 중첩)을 이용하여 물리량(예, 온도, 자기장)을 측정하는 기술	[1]
양자얽힘(entanglement), 압착(squeezing) 등 양자특성을 이용하여 물리량을 양자한계(standard quantum limit) 이하로 측정하는 기술	[1]
고전시스템만을 사용했을 때 얻을 수 있는 것보다 더 나은 민감도와 분해능을 얻기 위해 양자얽힘과 같은 양자특성을 활용하는 기술	[2]
기존 센서/이미징의 정밀도를 획기적으로 개선하고 새로운 초정밀 양자센서/이미징 산업을 창출할 수 있는 기술을 포함	[2]

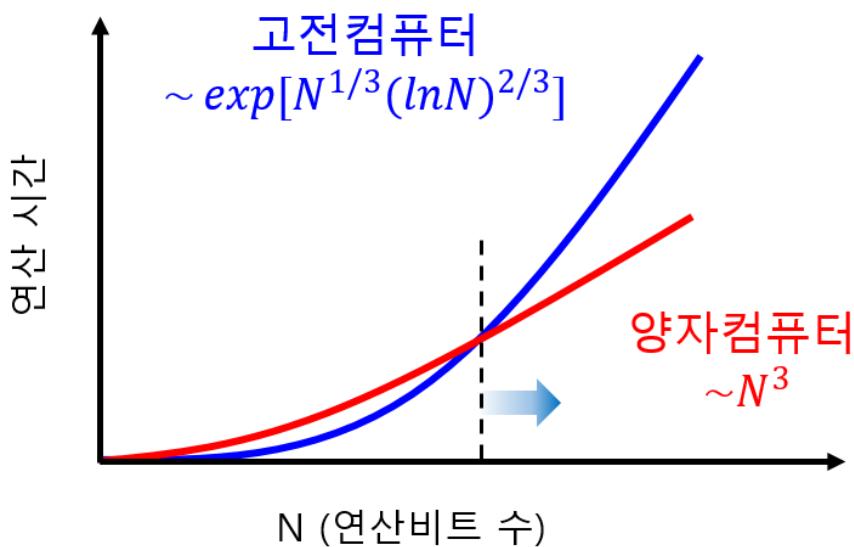
[1] C. L. Degen, F. Reinhard, P. Cappellaro, “Quantum Sensing”, *Reviews of Modern Physics* 89, 0034–6861, 2017.

[2] 정보통신기술진흥센터 ICT R&D 기술로드맵 2023.

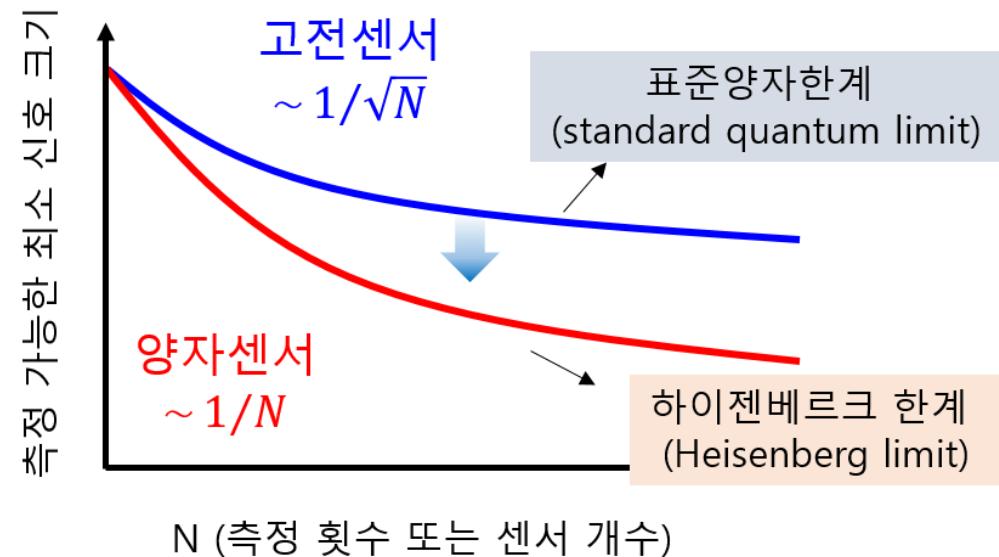
# Quantum sensing and quantum limit

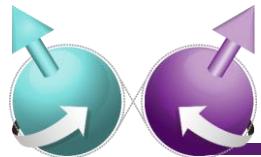


## 양자컴퓨팅 / 양자우월성



## 양자센싱 / 양자한계





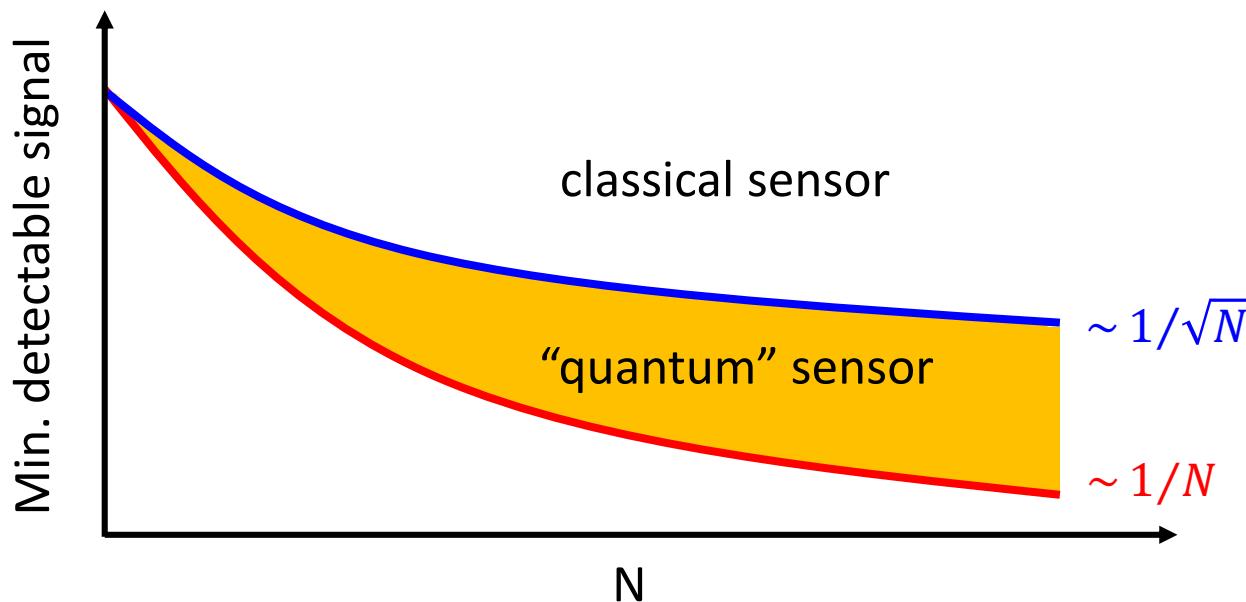
## Sensitivity of quantum sensor

$$\text{민감도 (sensitivity)} \approx \frac{1}{\sqrt{N}} \frac{1}{\sqrt{T}}$$

물리량  
[  $\frac{\text{물리량}}{\sqrt{\text{Hz}}}$  ]

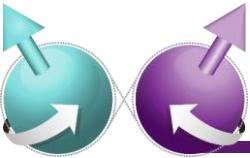
$N$  : # of measurements or # of sensors

$T$  : Coherence time ,  $T_1, T_2, T_2^*$



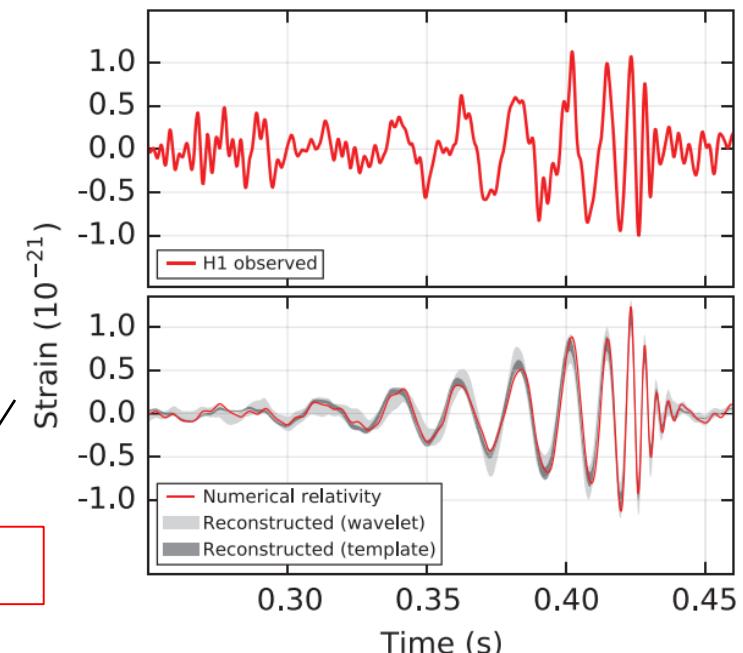
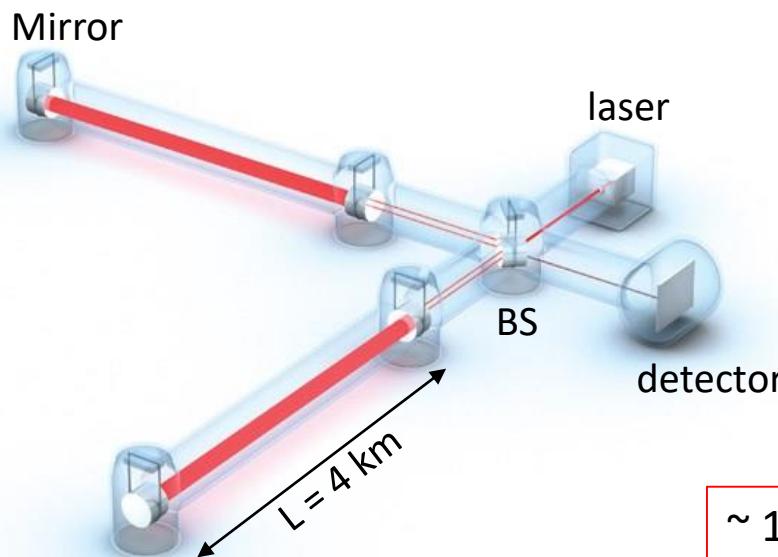
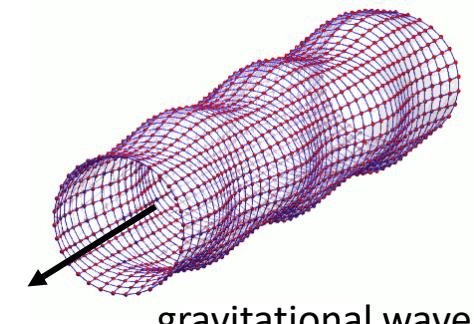
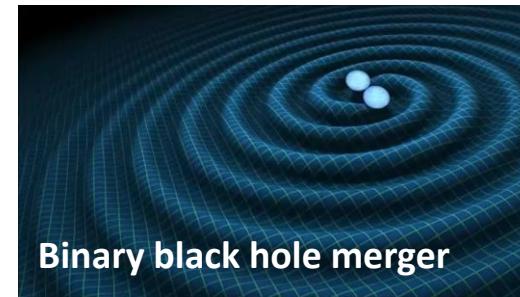
표준양자한계  
(standard quantum limit)

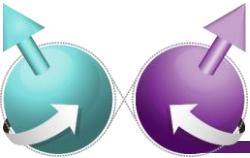
하이젠베르크 한계  
(Heisenberg limit)



# Example : Gravitational Wave Detection

LIGO (Laser Interferometer Gravitational-Wave Observatory), Nobel prize at 2017

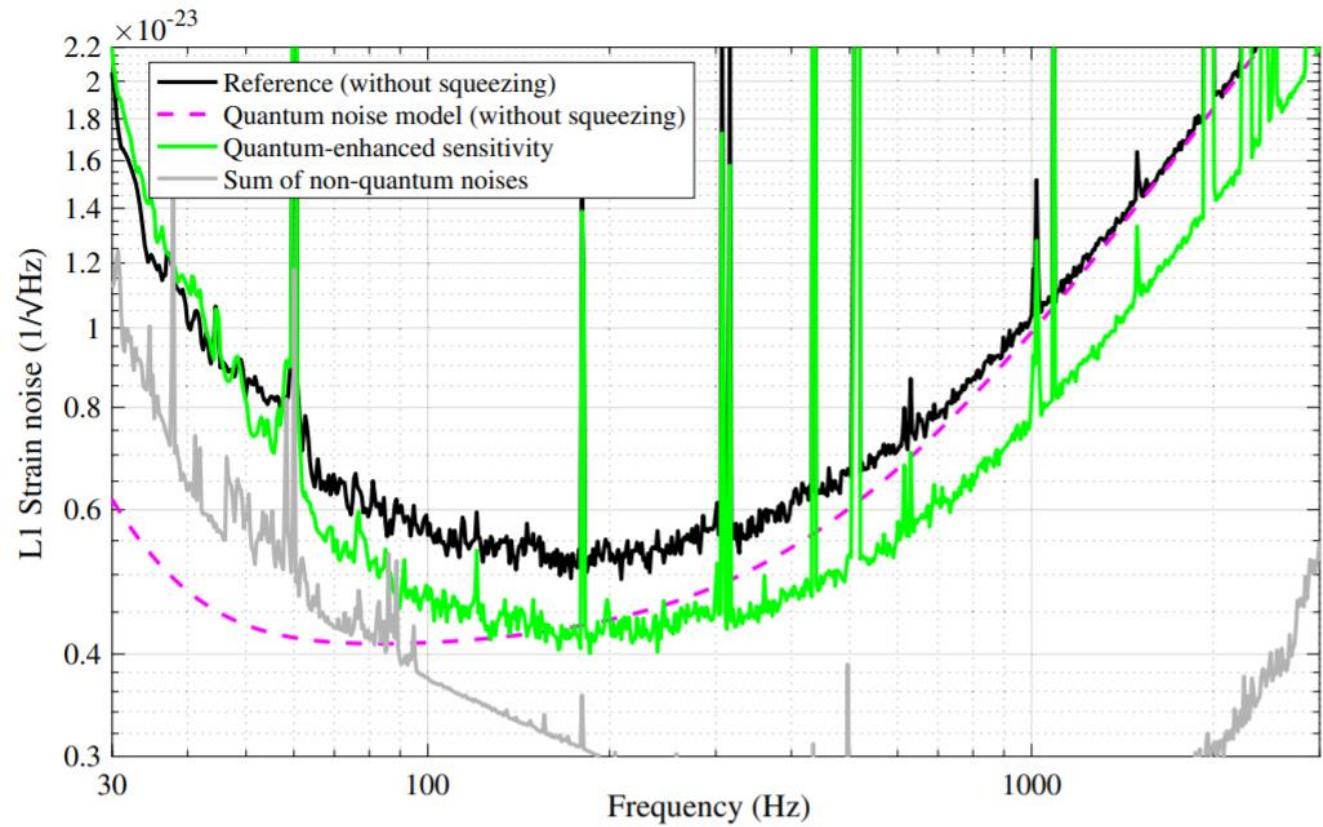
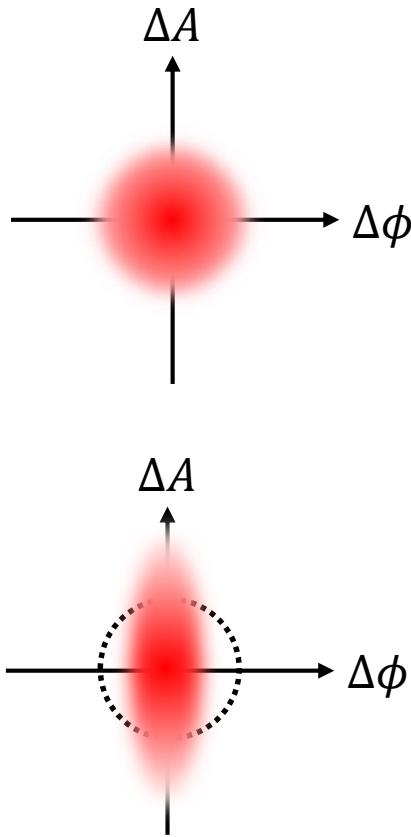




## Example : Gravitational Wave Detection

LIGO (Laser Interferometer Gravitational-Wave Observatory), Nobel prize at 2017

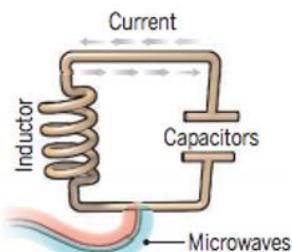
50 % improvement with quantum squeezed light



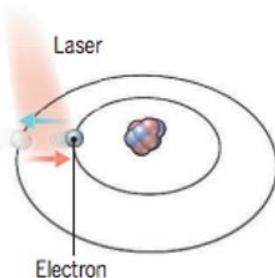
# Classification of quantum sensing

## ➤ 양자센서에 따른 분류

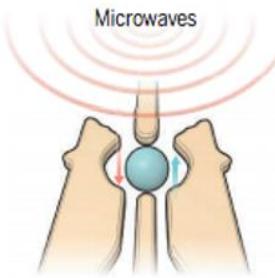
초전도 소자



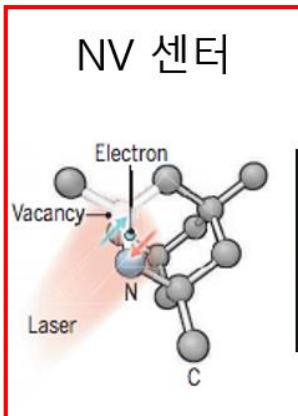
이온, 원자



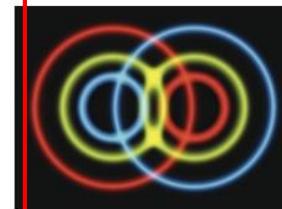
반도체 양자점



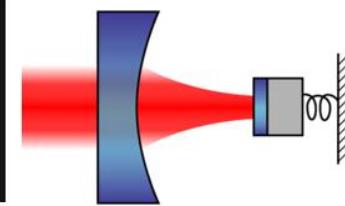
NV 센터



광자

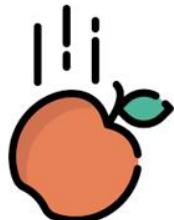


역학계



## ➤ 센싱 물리량에 따른 분류

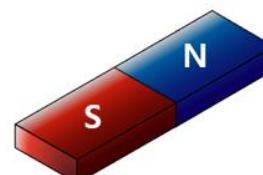
중력/힘



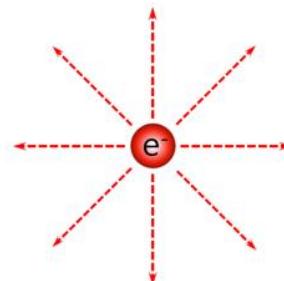
회전/각속도



자기장/스핀



전기장/전하

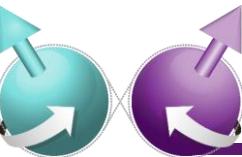


온도



시간





# Classification of quantum sensing

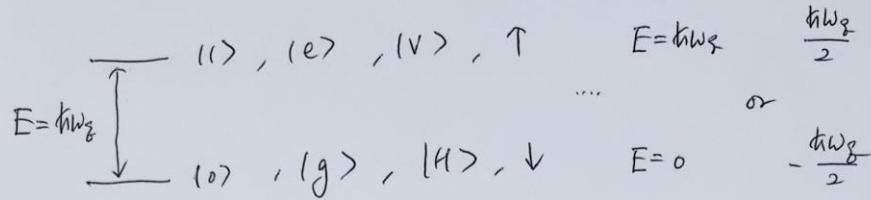
대분류	소분류	큐빗	측정하는 양	진동수	초기화	상태읽기
중성 원자	원자 증기	원자스핀	자기장, 회전, 시간/진동수	dc-GHz	광학	광학
	차가운 구름	원자스핀	자기장, 가속도, 시간/진동수	dc-GHz	광학	광학
간접 이온	-	수명이 긴 전자 상태	시간/진동수	THz	광학	광학
			회전	-	광학	광학
		진동 모드	전기장, 힘	MHz	광학	광학
리드버그 원자	-	리드버그 상태	전기장	dc, GHz	광학	광학
고체 스픬 (양상블)	NMR 센서	핵 스픬	자기장	dc	열	픽업 코일
	NV 센터 양상블	전자스핀	자기장, 전기장, 온도, 압력, 회전	dc-GHz	광학	광학
고체 스픬 (단일 스픬)	Si 반도체의 P 도너	전자스핀	자기장	dc-GHz	열	전기
	반도체 양자 점	전자스핀	자기장, 전기장	dc-GHz	전기, 광학	전기, 광학
	단일 NV 센터	전자스핀	자기장, 전기장, 온도, 압력, 회전	dc-GHz	광학	광학
초전도 회로	SQUID	초전류	자기장	dc-GHz	열	전기
	Flux 큐빗	순환 전류	자기장	dc-GHz	열	전기
	전하 큐빗	전하고유상태	전기장	dc-GHz	열	전기
기본 입자	뮤온	뮤온 스픬	자기장	dc	방사성 붕괴	방사성 붕괴
	중성자	핵스핀	자기장, 포논 밀도, 중력	dc	브래그 산란	브래그 산란
기타센서	SET	전하고유상태	전기장	dc-MHz	열	전기
	광역학계	포논	힘, 가속도, 질량, 자기장, 전압	-	-	-
	간섭계	광자, (원자, 분자)	변위, 굴절률	-	-	-

# 강의 계획

- Part 1 : 스피in 큐비트 기반 양자센싱 기초 원리
- Part 2 : 다이아몬드 NV 센터 소개
- Part 3 : NV 센터 기반 양자센싱 및 이미징 연구 소개

# **Part 1 : 스피너 큐비트 기반 양자센싱 기초 원리**

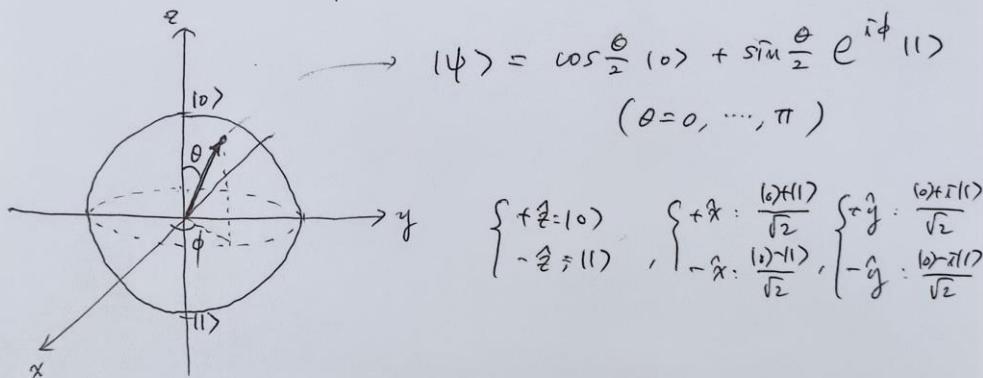
## 1.1 Qubit (Two level system)



Qubit state :  $|\psi\rangle = \alpha|0\rangle + \beta|1\rangle$   
 $(|\alpha|^2 + |\beta|^2 = 1)$

$$\rightarrow |\psi\rangle = \alpha|0\rangle + \beta e^{i\phi}|1\rangle \quad \phi: \text{relative phase}$$

### 1.2. Bloch representation



•  $\pi$  ( $180^\circ$ ) turn around  $\hat{z}$  :  $|\psi\rangle \rightarrow |\psi'\rangle$

$$\begin{aligned} |\psi'\rangle &= \cos\frac{\theta}{2}|0\rangle + \sin\frac{\theta}{2} e^{i(\phi+\pi)}|1\rangle \\ &= \cos\frac{\theta}{2}|0\rangle - \sin\frac{\theta}{2}|1\rangle \end{aligned}$$

$$\not Z \equiv \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} = \sigma_z$$

(2)

- $\Pi$  around  $\hat{x}$  :  $|0\rangle \rightarrow |1\rangle$ ,  $|1\rangle \rightarrow |0\rangle$

$$X \equiv \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} = \sigma_x$$

- $\Pi$  around  $\hat{y}$  :

$$Y \equiv \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix} = \sigma_y$$

### 1, 3. Qubit Hamiltonian

$$\begin{aligned} H &= \hbar\omega_z |1\rangle\langle 1| + 0 \cdot |0\rangle\langle 0| \\ &= \frac{\hbar\omega_z}{2} |1\rangle\langle 1| - \frac{\hbar\omega_z}{2} |0\rangle\langle 0| \\ &= -\frac{\hbar\omega_z}{2} \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} = -\frac{\hbar\omega_z}{2} \sigma_z \end{aligned}$$

#### ① time evolution

$$\frac{d}{dt}|\psi\rangle = -\frac{i}{\hbar} H |\psi\rangle, \quad H = -\frac{\hbar\omega_z}{2} \sigma_z$$

$$\rightarrow \frac{d}{dt} \begin{pmatrix} \alpha \\ \beta \end{pmatrix} = -\frac{i}{\hbar} \left( -\frac{\hbar\omega_z}{2} \right) \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \begin{pmatrix} \alpha \\ \beta \end{pmatrix}$$

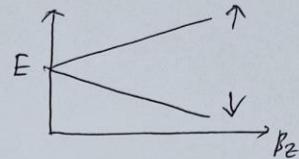
$$\rightarrow \begin{pmatrix} \dot{\alpha} \\ \dot{\beta} \end{pmatrix} = \begin{pmatrix} i \frac{\hbar\omega_z}{2} \alpha \\ -i \frac{\hbar\omega_z}{2} \beta \end{pmatrix}$$

$$\therefore \alpha(t) = e^{+i \frac{\hbar\omega_z t}{2}} \alpha(0), \quad \beta(t) = e^{-i \frac{\hbar\omega_z t}{2}} \beta(0)$$

$\therefore$  process at  $\omega_z$

② Zeeman splitting

$$\begin{array}{c} \longrightarrow \uparrow m_s = +\frac{1}{2} \\ \longrightarrow \downarrow m_s = -\frac{1}{2} \end{array} \quad \uparrow B_z$$



$$H = -\frac{\hbar\omega_p}{2}\sigma_z - \frac{\hbar\gamma}{2}B_z\sigma_z$$

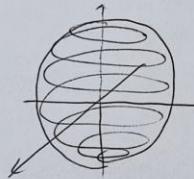
$\therefore$  precess at  $\omega_p + \gamma B_z$

"1/22" at  $B_z = 100$  Gaus

③ Driving with  $H_{\perp}(x, y)$

$$E = \hbar\omega_p \begin{bmatrix} \uparrow \\ \downarrow \end{bmatrix} \text{ in } \omega, \Omega, \quad H = -\frac{\hbar\omega_p}{2}\sigma_z + \hbar\Omega \cos \omega t \sigma_x$$

$$\text{time evolution: } i\hbar \frac{d}{dt} \begin{pmatrix} \alpha \\ \beta \end{pmatrix} = \begin{pmatrix} -\frac{\hbar\omega_p}{2} \alpha \\ +\frac{\hbar\omega_p}{2} \beta \end{pmatrix} + \hbar\Omega \cos \omega t \begin{pmatrix} \rho \\ \omega \end{pmatrix}$$



at lab frame,  
 $\left\{ \begin{array}{l} \text{precess freq} \sim \omega_p(n) \text{ (fast)} \\ \text{rot freq} \sim \omega \text{ (ul. \omega)} \end{array} \right.$

Go into "rotating frame"

$$\begin{pmatrix} \alpha \\ \beta \end{pmatrix} = \begin{pmatrix} \tilde{\alpha} e^{+i\frac{\omega}{2}t} \\ \tilde{\beta} e^{-i\frac{\omega}{2}t} \end{pmatrix}$$

$$\rightarrow \underbrace{i\hbar \left( +i\frac{\omega}{2} \right)}_{= -\frac{\hbar\omega}{2}} \begin{pmatrix} \tilde{\alpha} e^{i\frac{\omega}{2}t} \\ -\tilde{\beta} e^{-i\frac{\omega}{2}t} \end{pmatrix} + i\hbar \begin{pmatrix} \dot{\tilde{\alpha}} e^{i\frac{\omega}{2}t} \\ \dot{\tilde{\beta}} e^{-i\frac{\omega}{2}t} \end{pmatrix}$$

$$\begin{aligned}
 (\cos\omega t)\rho &= \frac{1}{2} (e^{i\omega t} + e^{-i\omega t}) \tilde{\rho} e^{-i\frac{\omega}{2}t} \\
 &= \frac{1}{2} \left( e^{i\frac{\omega}{2}t} + \underbrace{e^{-i\frac{3\omega}{2}t}}_{\approx 0 \text{ RWA (Rotating Wave Approx.)}} \right) \tilde{\rho} \approx \frac{1}{2} e^{i\frac{\omega}{2}t} \tilde{\rho} \\
 \rightarrow \quad \tilde{\rho} &\approx -\frac{i\omega g}{2} \begin{pmatrix} \dot{x} \\ -\dot{p} \end{pmatrix} + \frac{i\Omega}{2} \begin{pmatrix} \dot{p} \\ x \end{pmatrix}
 \end{aligned}$$

$$\begin{aligned}
 \cancel{e^{i\frac{\omega}{2}t}} \rightarrow ik \begin{pmatrix} \dot{x} \\ \dot{p} \end{pmatrix} &= -\left(\frac{i\omega g}{2} - \frac{i\omega}{2}\right) \begin{pmatrix} x \\ p \end{pmatrix} + \frac{i\Omega}{2} \begin{pmatrix} p \\ x \end{pmatrix} \\
 &= -\frac{i\delta}{2} \sigma_x \begin{pmatrix} x \\ p \end{pmatrix} + \frac{i\Omega}{2} \sigma_x \begin{pmatrix} x \\ p \end{pmatrix} \\
 \left( \delta \equiv \omega_p - \omega, \text{ detuning } \boxed{\frac{\omega_p}{\omega} \delta} \right) \\
 &= \hat{H} \begin{pmatrix} x \\ p \end{pmatrix}, \quad \hat{H} = -\frac{i\delta}{2} \sigma_x + \frac{i\Omega}{2} \sigma_x
 \end{aligned}$$

On resonance,  $\delta = 0$

$$ik \begin{pmatrix} \dot{x} \\ \dot{p} \end{pmatrix} = \frac{i\Omega}{2} \sigma_x \begin{pmatrix} \dot{x} \\ \dot{p} \end{pmatrix}$$

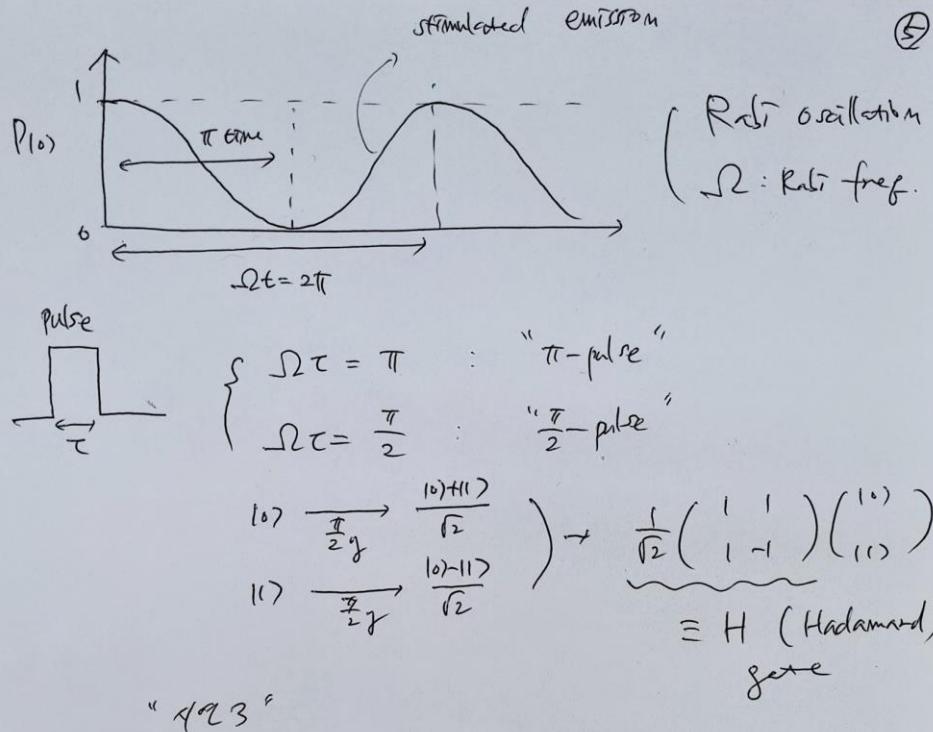
rotates around  $\hat{x}$  at freq of  $i\Omega$

$|1\rangle, P_{11\rangle}$

$|10\rangle, P_{10\rangle}$

$$\langle \sigma_z \rangle = P_{10\rangle} - P_{11\rangle} = P_{10\rangle} - (1 - P_{11\rangle}) = 2P_{10\rangle} - 1$$

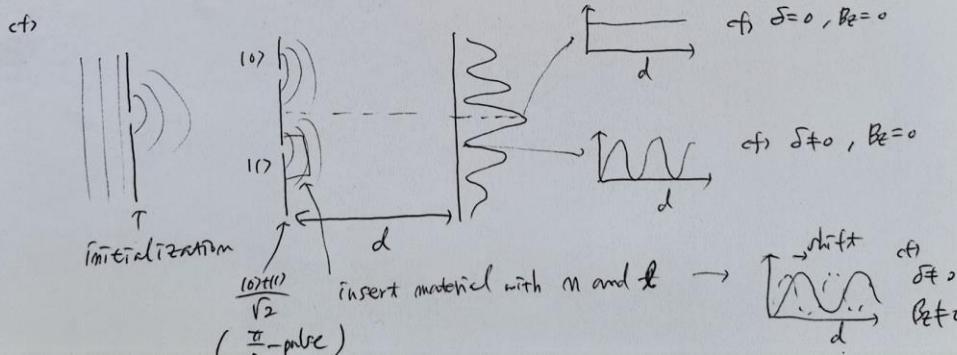
$$\therefore P_{10\rangle}(t) = \frac{1}{2} (1 + \langle \sigma_z \rangle) = \frac{1}{2} (1 + \cos\omega t)$$



④ Ramsey interferometry (DC field sensing)

$$H = - \frac{\hbar \omega_z}{z} \sigma_z - \frac{\hbar \gamma}{z} B_z \delta_z$$

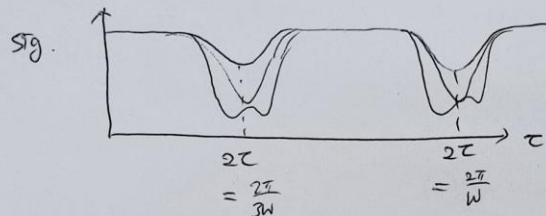
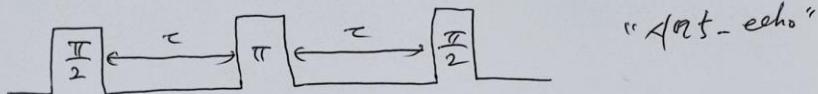
rotating frame  $\tilde{H} = -\left(\frac{\hbar\delta}{2} + \frac{\hbar\gamma}{2}B_z\right)\delta_2$  "Aoz + Raney"



⑤ (spin) Hahn echo (AC field sensing)

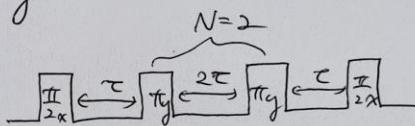
6

$$\tilde{H} = -\frac{\hbar\delta}{2}\sigma_z - \frac{\hbar\delta}{2}B_2 \sin(\omega t + \phi)\sigma_z$$

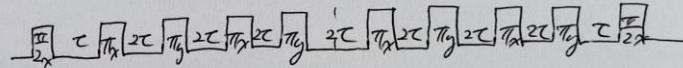


## ⑥ Dynamical decoupling

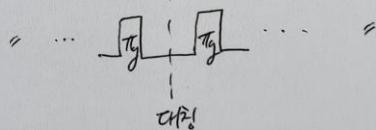
- CPMG ( $-N$ )  
(Car-Purcell-Meiboom-Gill)



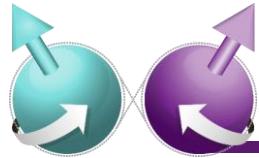
- XI-4



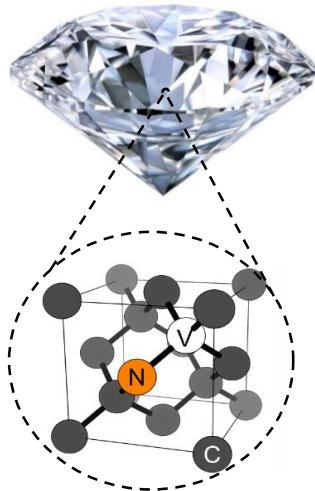
- XI-8



## **Part 2 : 다이아몬드 NV 센터 소개**



# Nitrogen-vacancy (NV) defect centers in diamond



## Quantum Point Defects (QPDs)

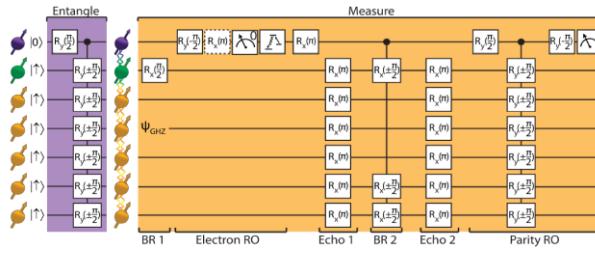
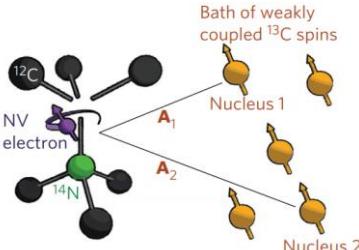
## “trapped ions” in solids

- long coherence time
  - atomic size
  - optically addressable
  - room temperature operation

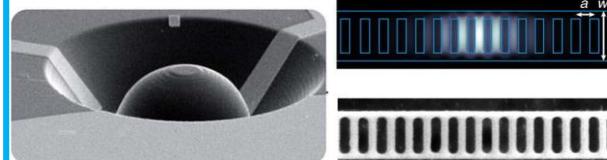
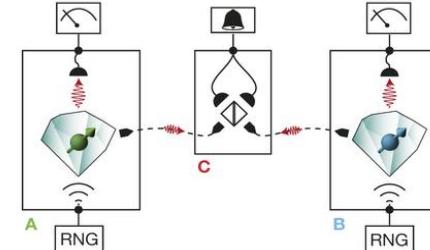
# defects in semiconductors

- fast manipulation
  - nano fabrication
  - scalable
  - integrated, devices on-chip

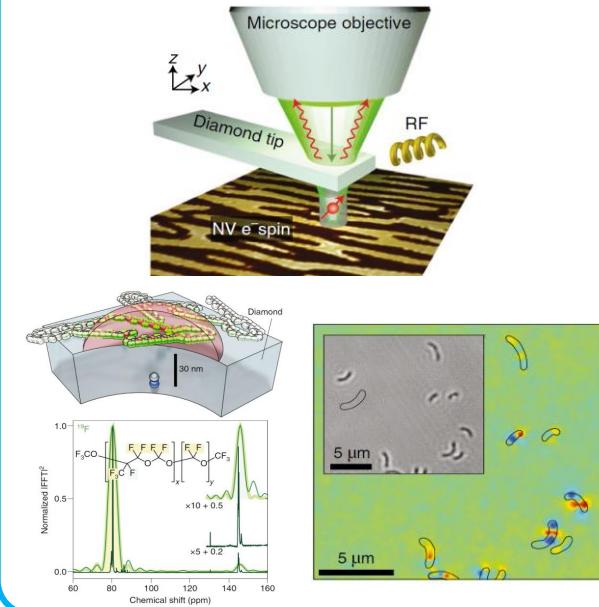
## Quantum computation

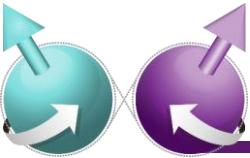


## Quantum communication

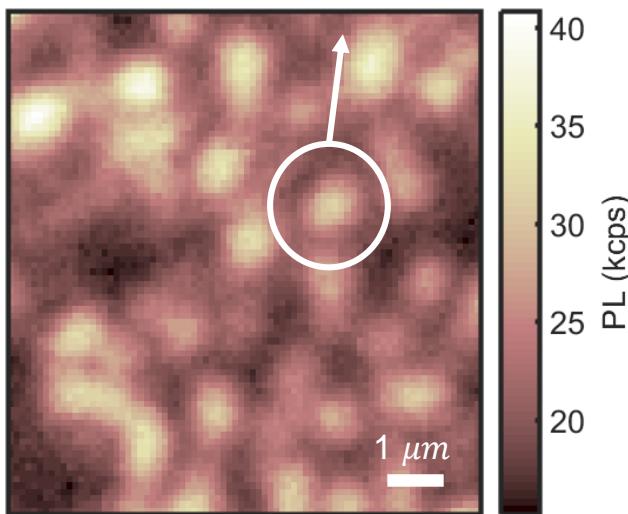
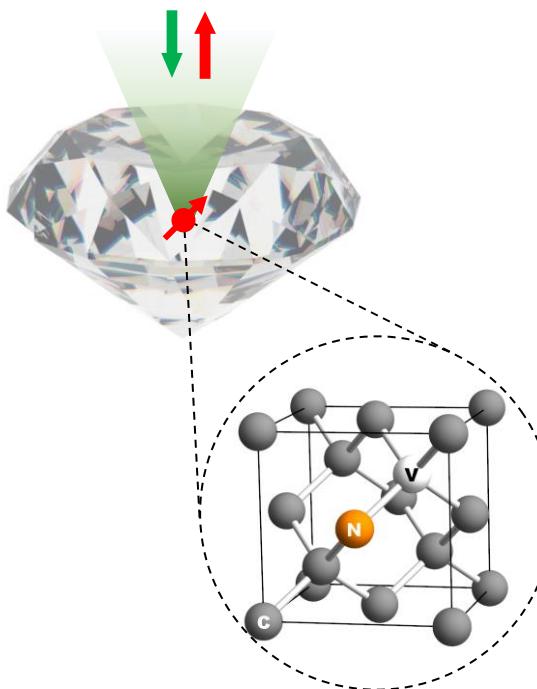


## Quantum sensing



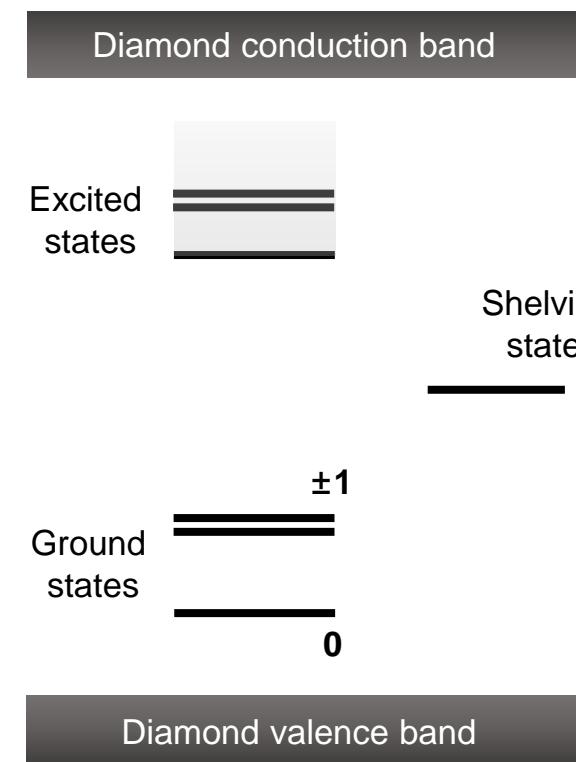


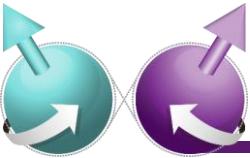
# Nitrogen-vacancy (NV) defect centers in diamond



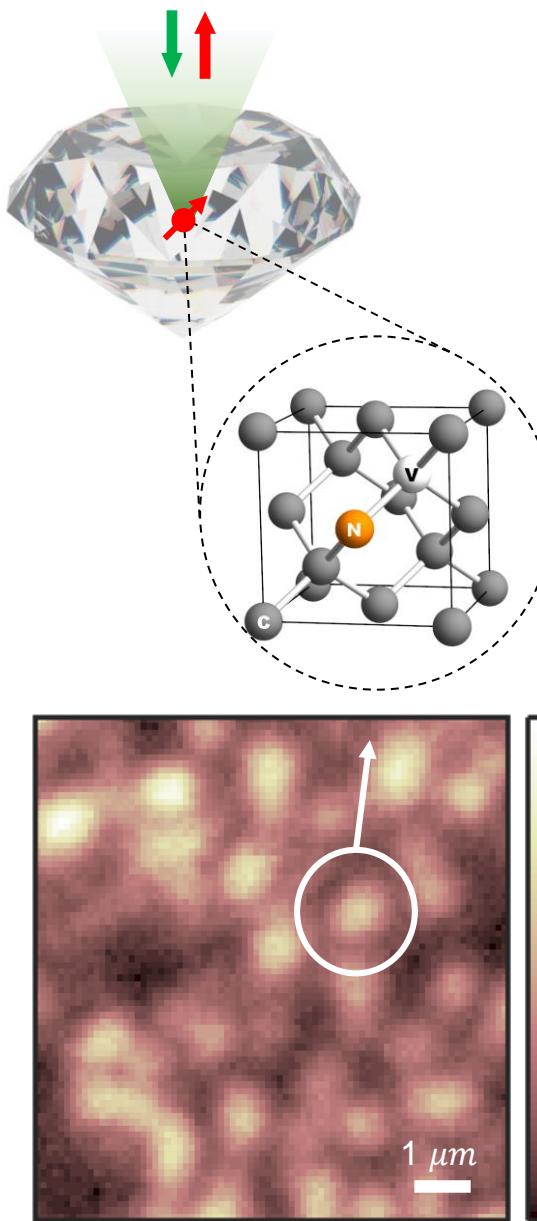
## NV defect centers in diamond

- $S = 1$  ground states i.e.  $m_s = 0, m_s = \pm 1$
- Spin levels are very sensitive to external magnetic field
- Magnetic signal is optically detected (ODMR)



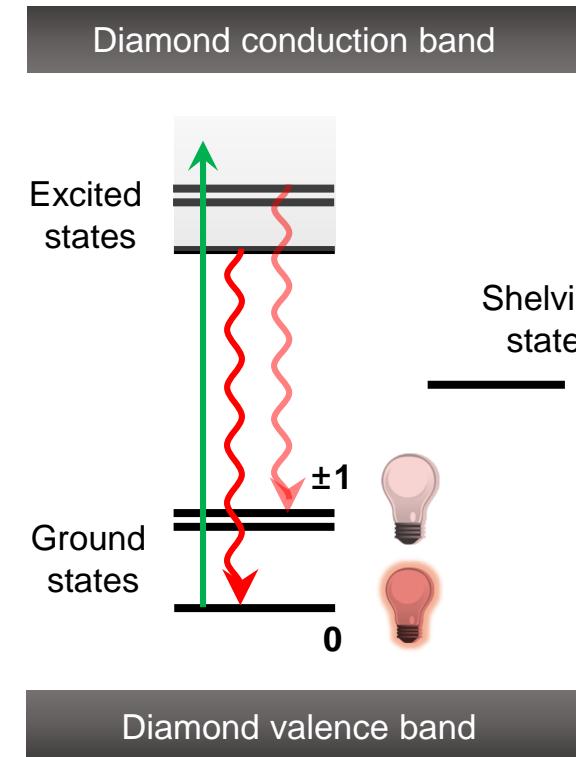


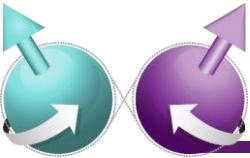
# Nitrogen-vacancy (NV) defect centers in diamond



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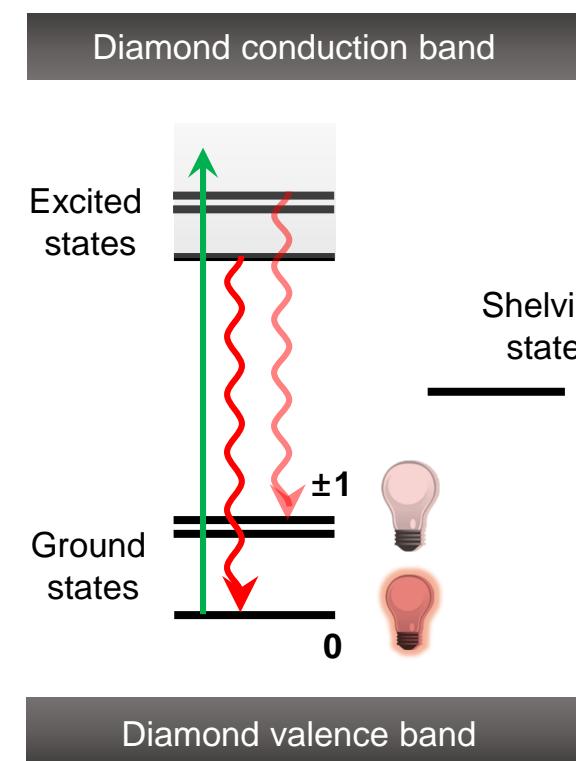
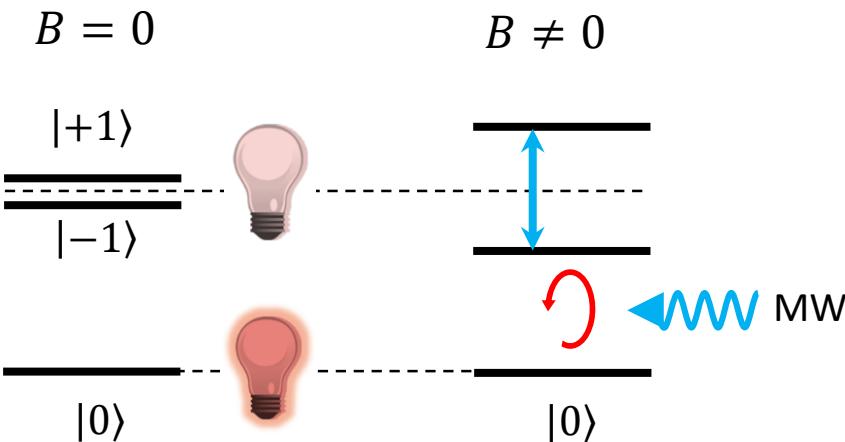


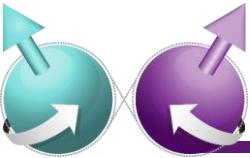


# Nitrogen-vacancy (NV) defect centers in diamond

## NV defect centers in diamond

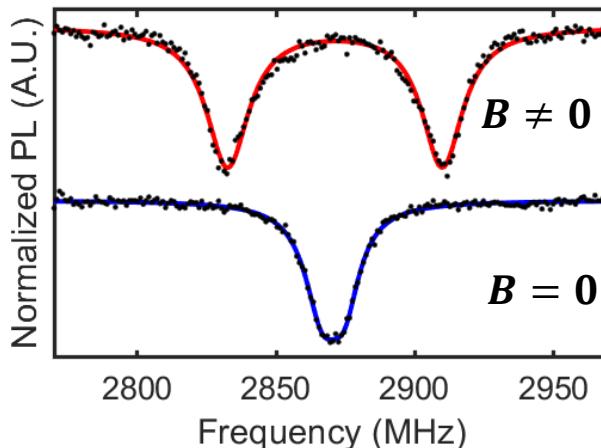
- $S = 1$  ground states i.e.  $m_s = 0, m_s = \pm 1$
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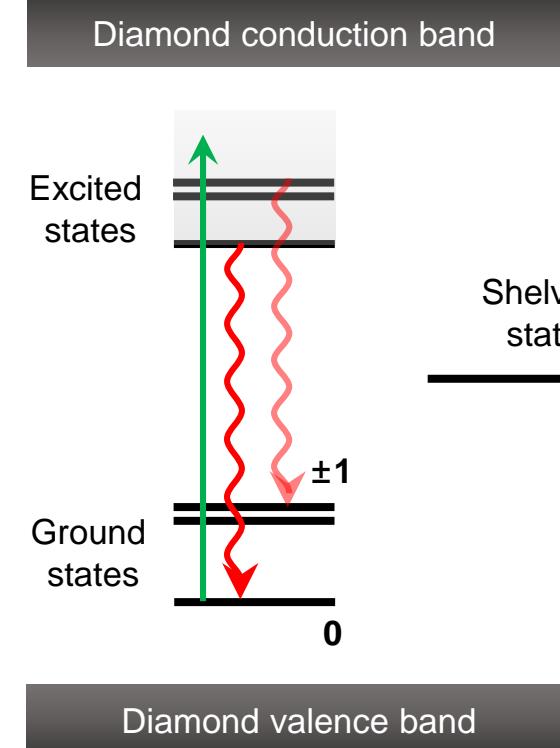
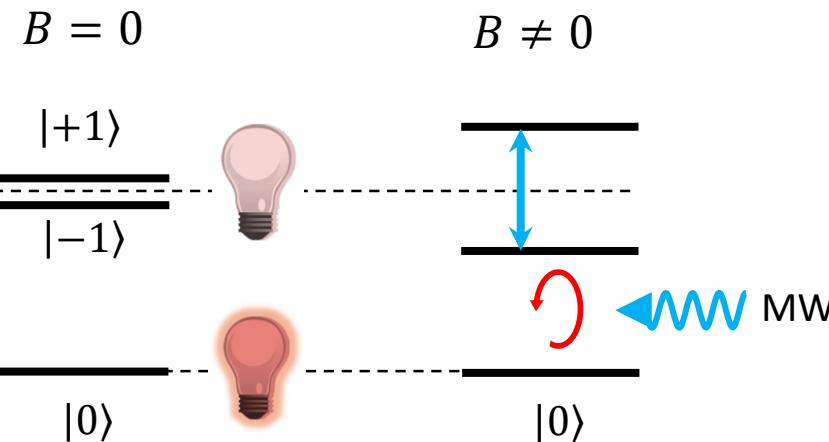
# Nitrogen-vacancy (NV) defect centers in diamond

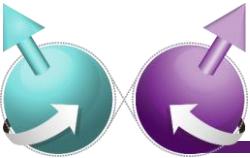
## Optically-detected ESR



## NV defect centers in diamond

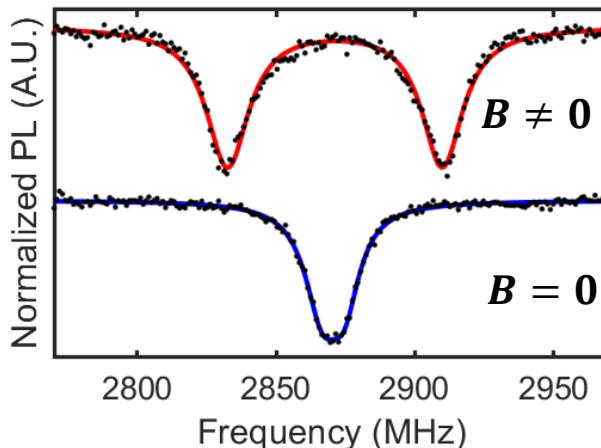
- $S = 1$  ground states i.e.  $m_s = 0, m_s = \pm 1$
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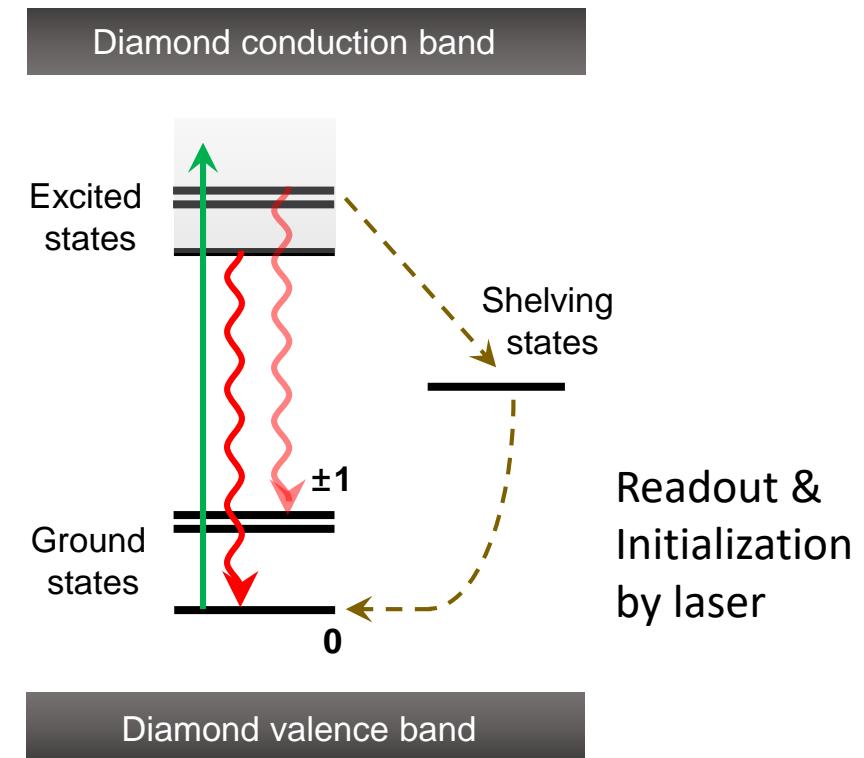
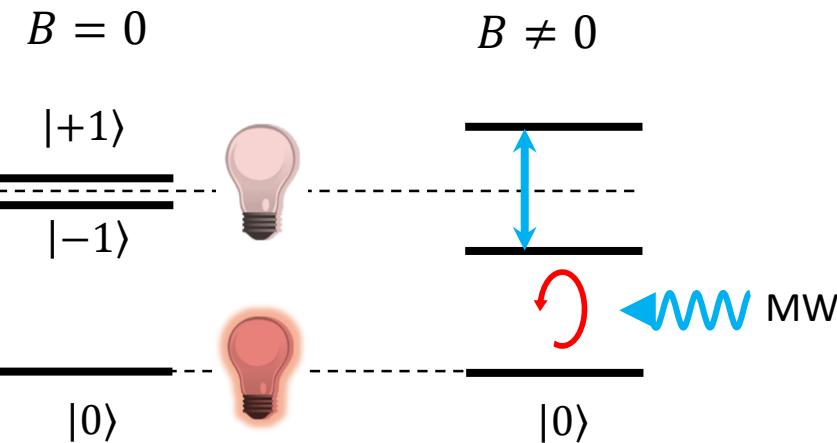
# Nitrogen-vacancy (NV) defect centers in diamond

## Optically-detected ESR

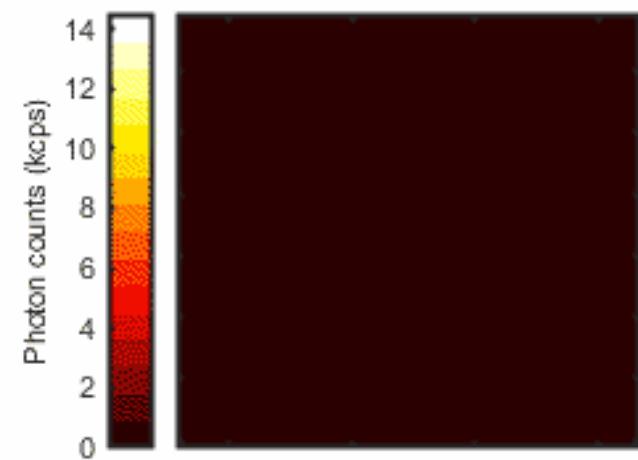
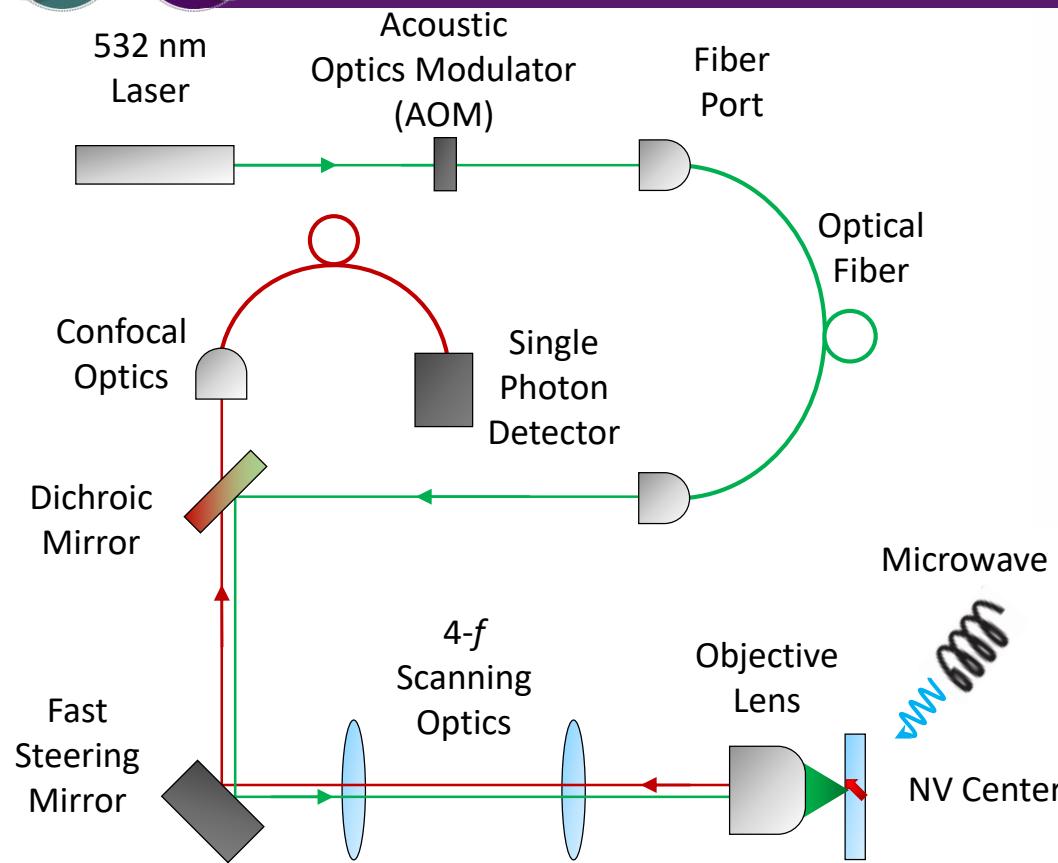


## NV defect centers in diamond

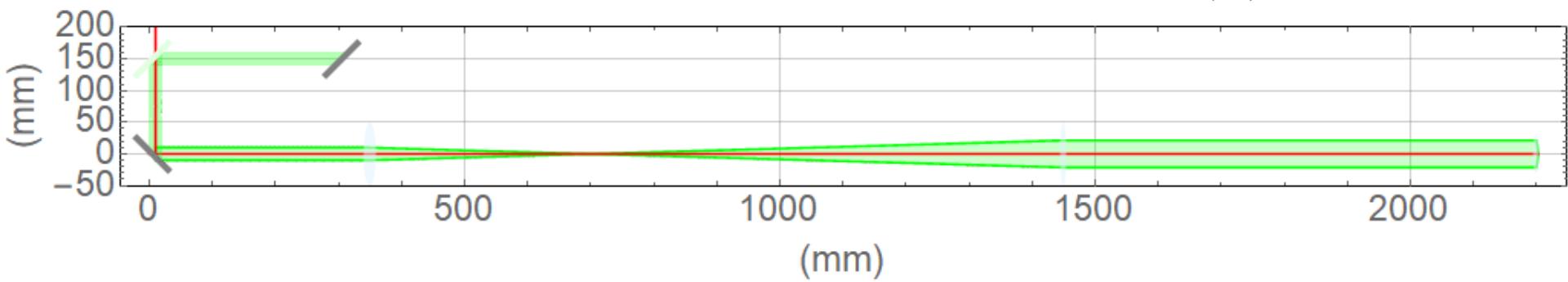
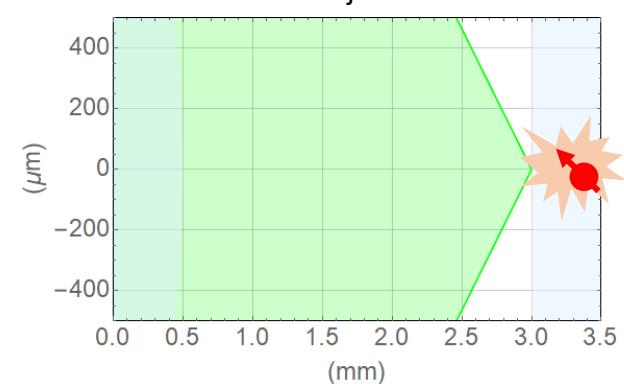
- $S = 1$  ground states i.e.  $m_s = 0, m_s = \pm 1$
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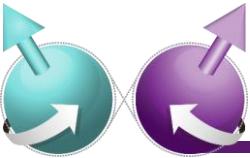


# Experimental confocal optics setup



At the end of objective lens NA=0.7





# Sensitivity of diamond NV center

Physical property	Sensitivity	Physical property	Sensitivity	References
Magnetic field	< 1 nT/Hz <sup>1/2</sup> (single NV) < 1 pT/Hz <sup>1/2</sup> (ensemble)	Temperature	< 1 mK/Hz <sup>1/2</sup>	J. Taylor et al., Nat. Phys. 2008 T. Wolf et al., PRX 2015 F. Dolde et al., PRL 2014 K. Lee et al., PR Applied 2016
Electric field	< 100 Vcm <sup>-1</sup> /Hz <sup>1/2</sup>	Rotation	< 1 mdeg /Hz <sup>1/2</sup>	G. Kuscko et al., Nature 2013 A. Ajoy et al., PRA 2012
Strain field	< 10 <sup>-7</sup> /Hz <sup>1/2</sup>	Pressure	< 0.1 MPa/Hz <sup>1/2</sup>	M. Doherty et al., PRL 2014 R. Schirhagl et al., Ann. Rev. Phys. Chem. 2014
Spatial resolution	~ 10 nm	Detection bandwidth	DC – GHz	Operating temperature
Other advantages	<ul style="list-style-type: none"> <li>chemically stable, non-toxic and bio-friendly</li> <li>optically stable (free from photobleaching)</li> <li>suitable for devices (nano fabrication)</li> </ul>			

## **Part 3 : NV 센터 기반 양자센싱 및 이미징 연구 소개**



# Quantum sensing examples

## Static magnetism

Domain wall

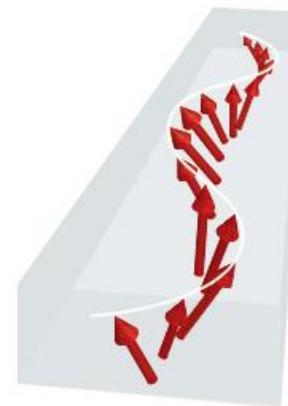


Skyrmion

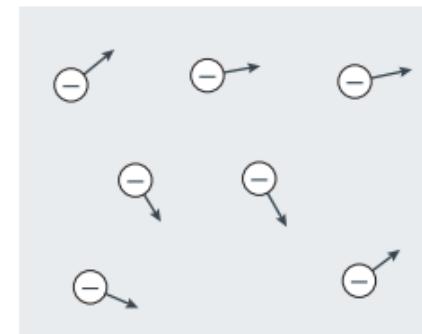


## Magnetic excitations

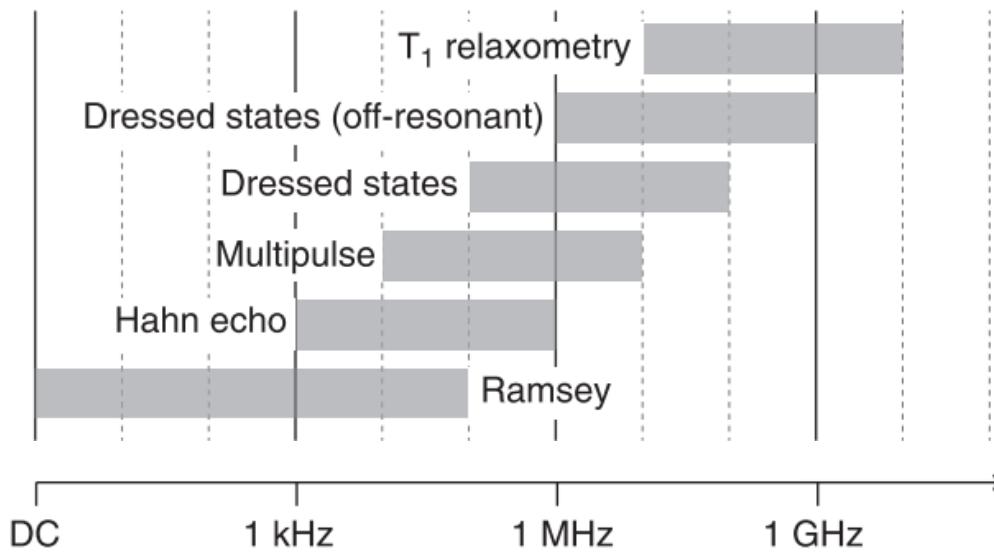
Spin wave



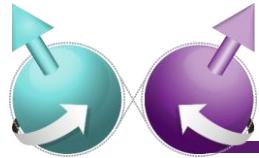
## Noise currents



F. Casola *et al.*, Nat. Rev. Mater. (2018)



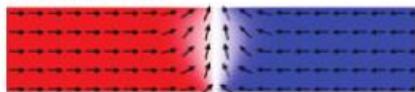
C. Degen *et al.*, Rev. of Mod. Phys. (2017)



# Quantum sensing examples

## Static magnetism

Domain wall

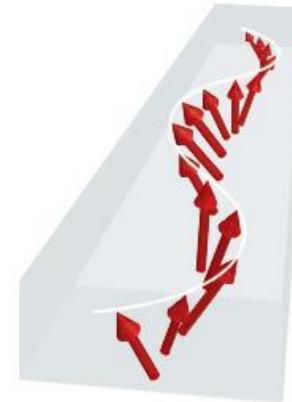


Skyrmion

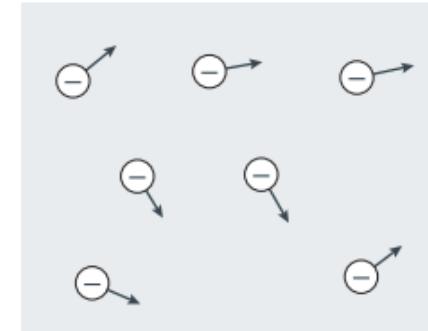


## Magnetic excitations

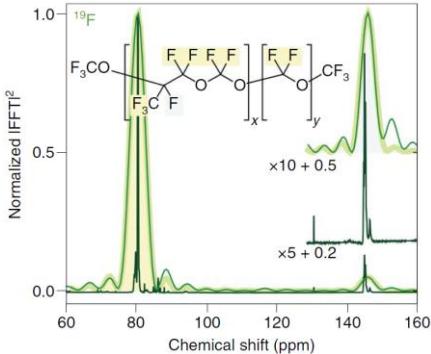
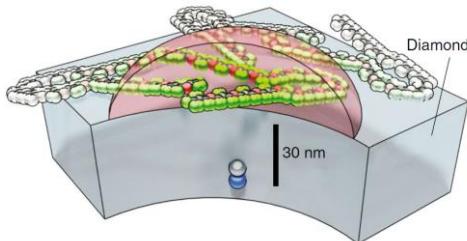
Spin wave



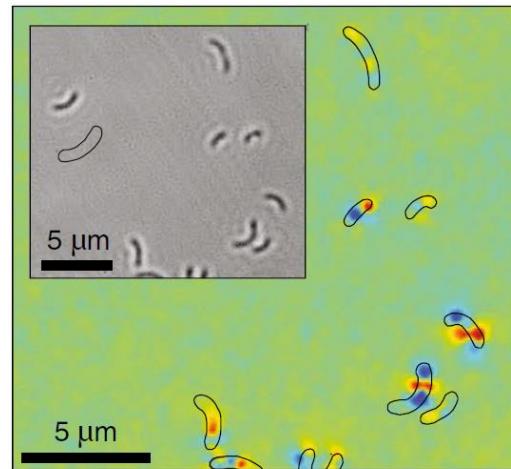
## Noise currents



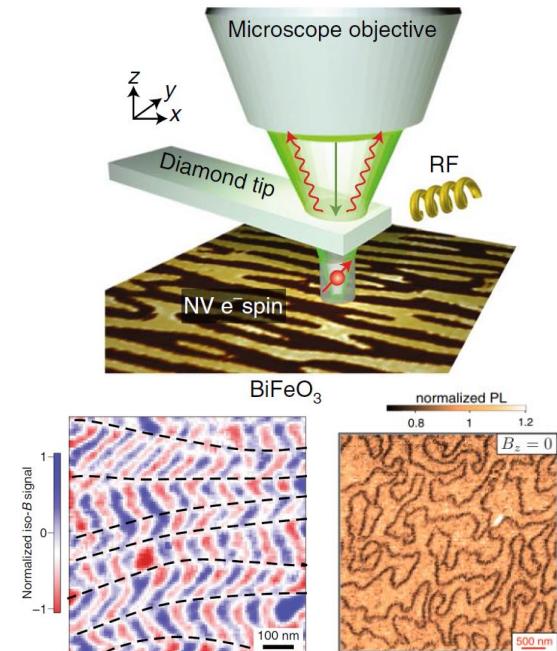
F. Casola *et al.*, Nat. Rev. Mater. (2018)



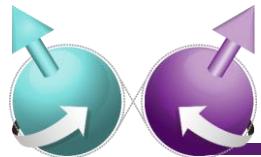
N. Aslam *et al.* Science 2017



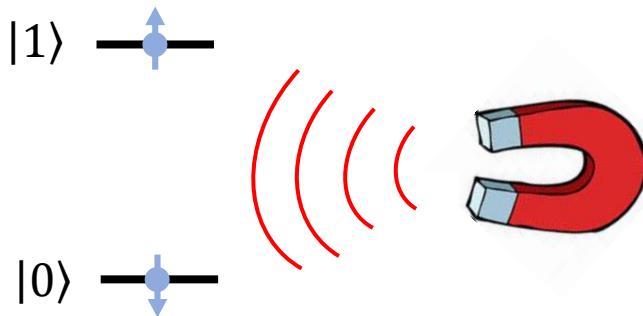
Le Sage *et al.* Nature 2013



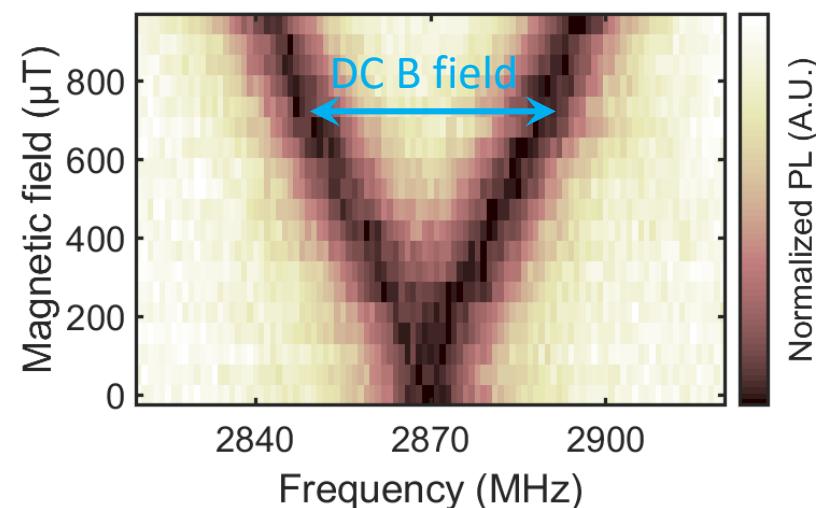
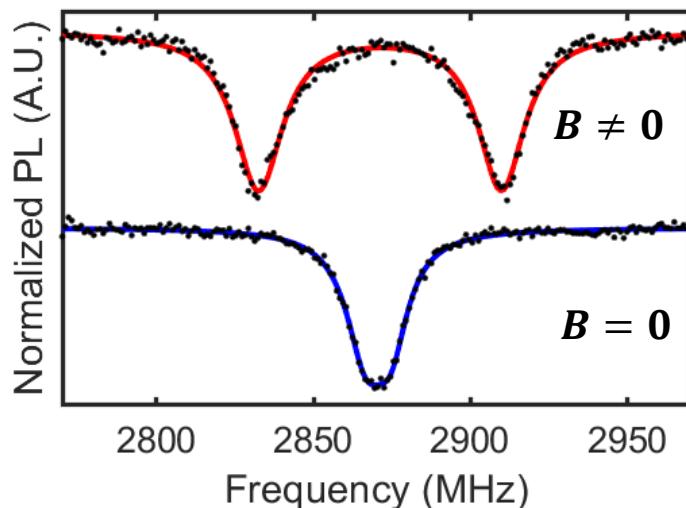
I. Gross *et al.* Nature 2017



# Sensing static (DC) B field

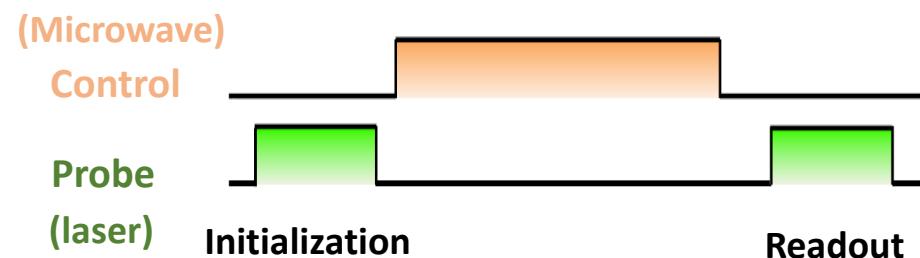
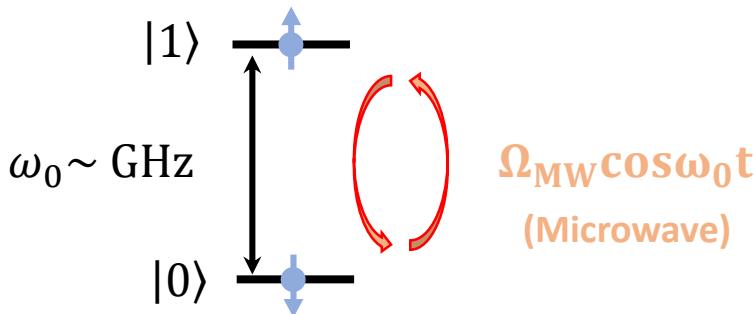


Optically-detected ESR

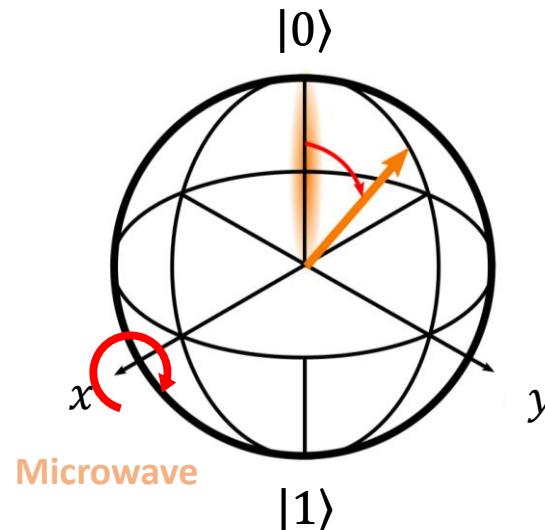
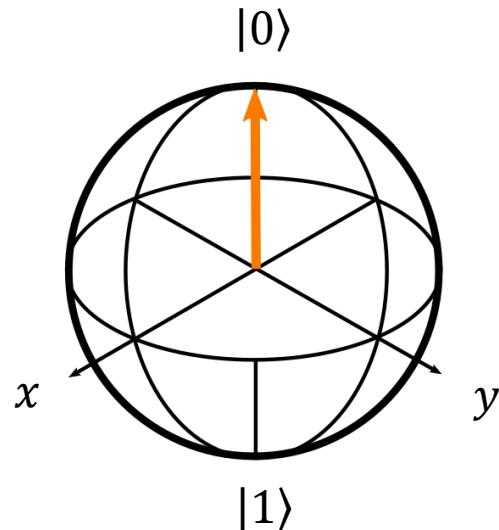




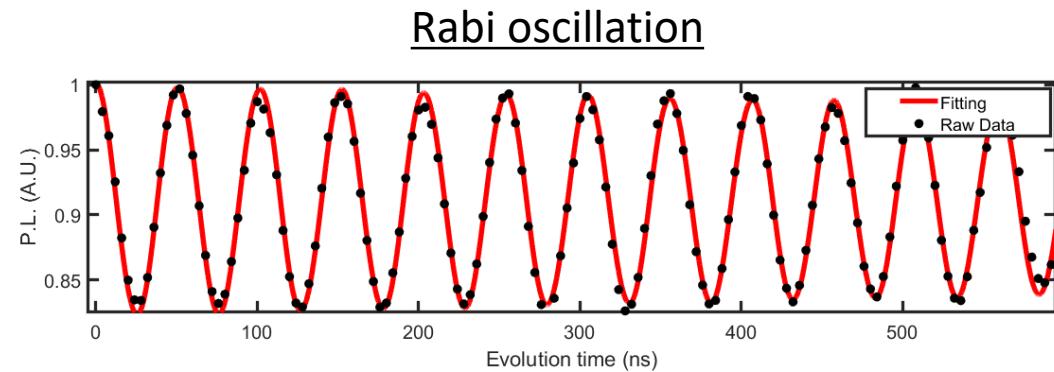
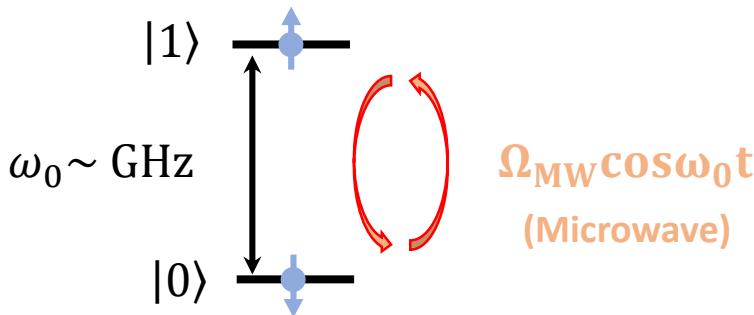
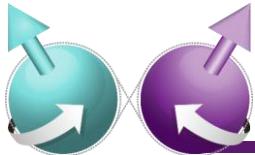
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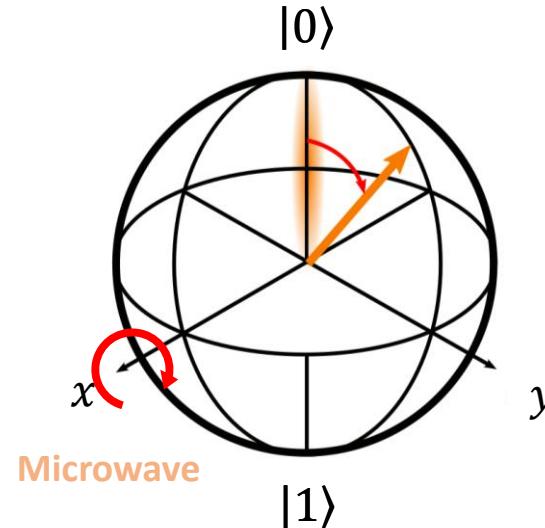
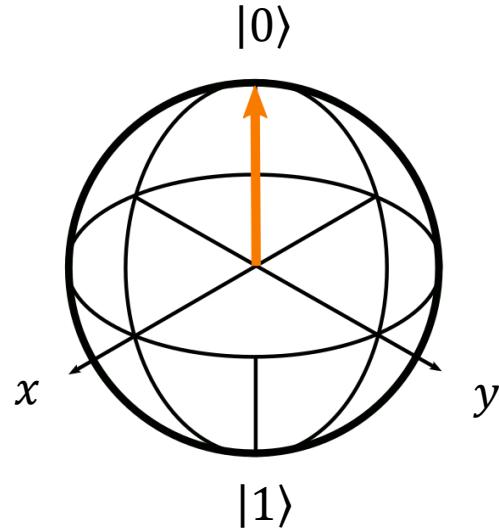
Initialization



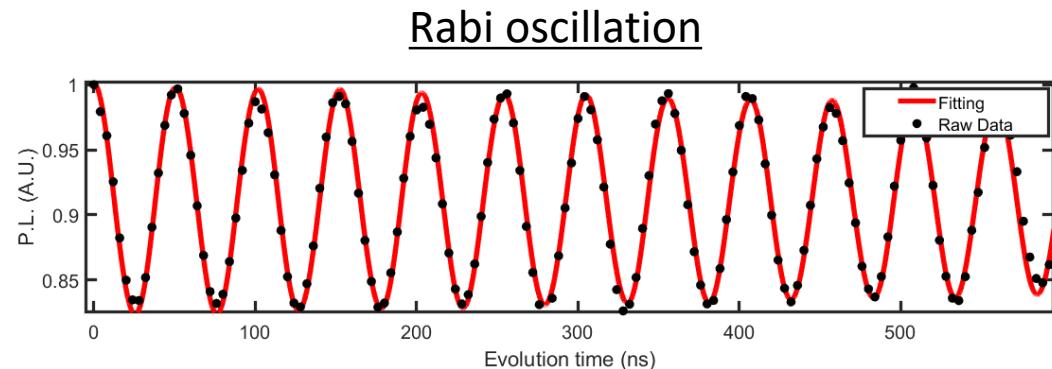
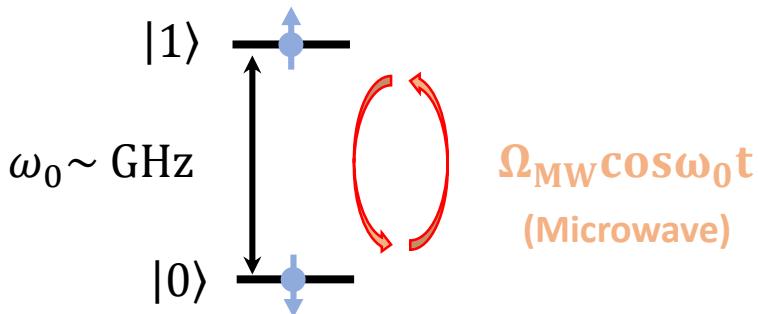
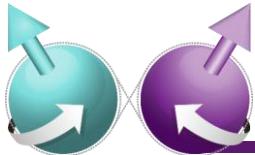
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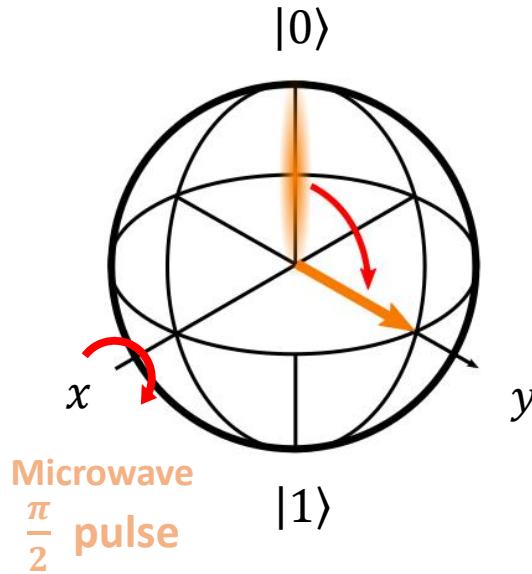
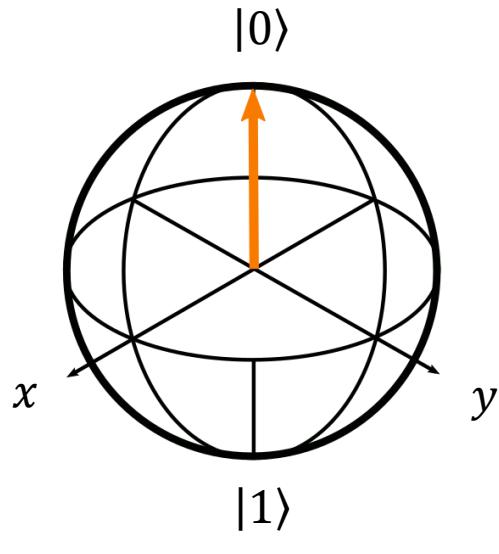
Initialization



# Sensing static (DC) B field

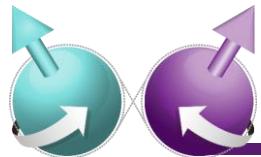


Initialization



$$|\psi\rangle = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle)$$





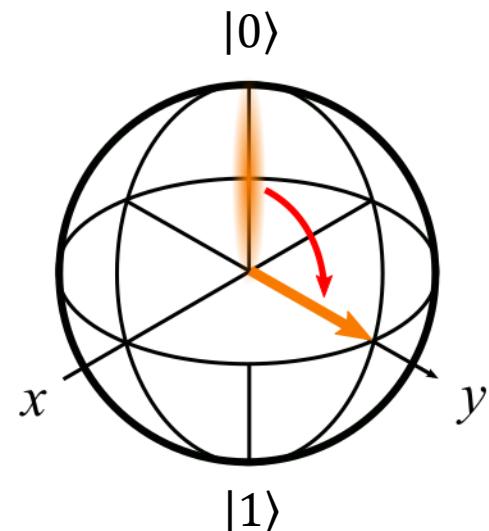
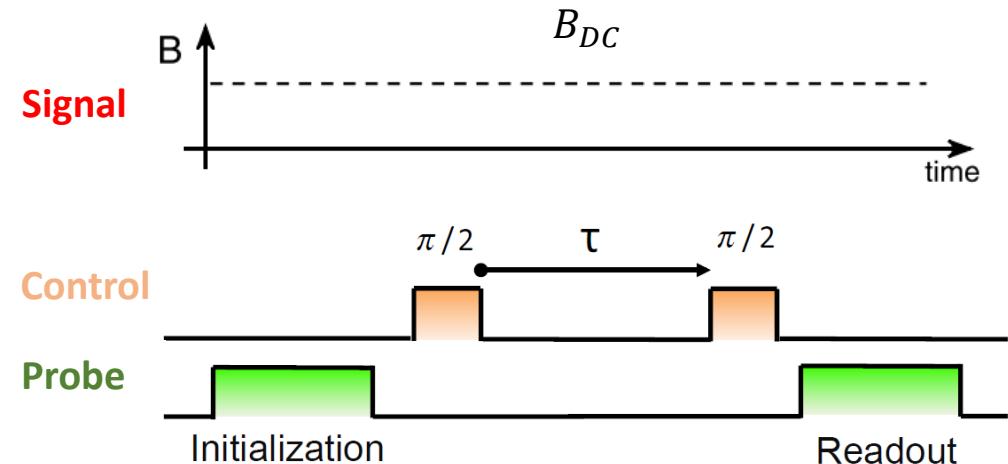
# Sensing static (DC) B field

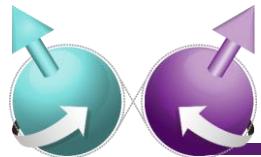
$|1\rangle$  —

$|0\rangle$  —

$$|\psi\rangle = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle)$$

## Ramsey Interferometry





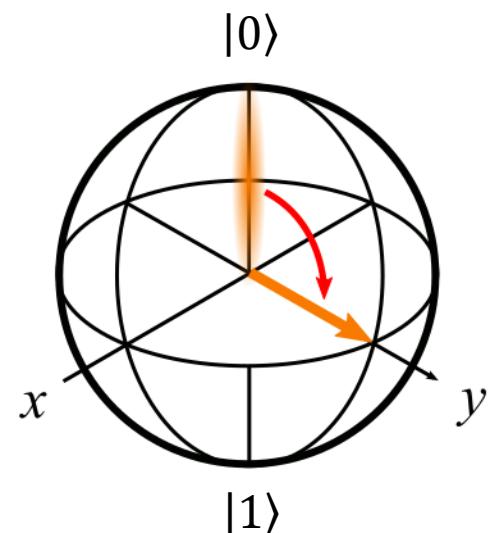
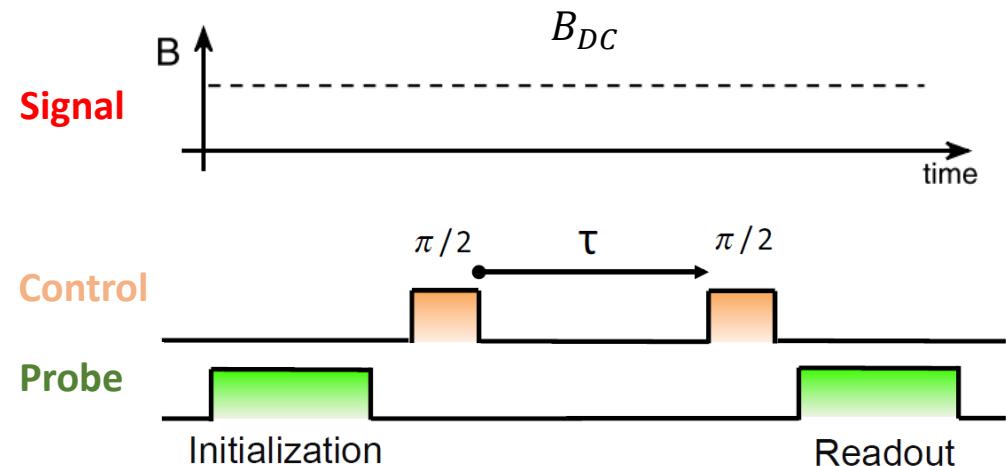
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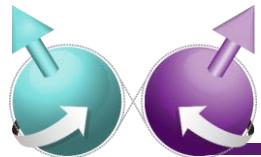
$|1\rangle$  —

$|0\rangle$  —

$$|\psi\rangle = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle)$$

## Ramsey Interferometry



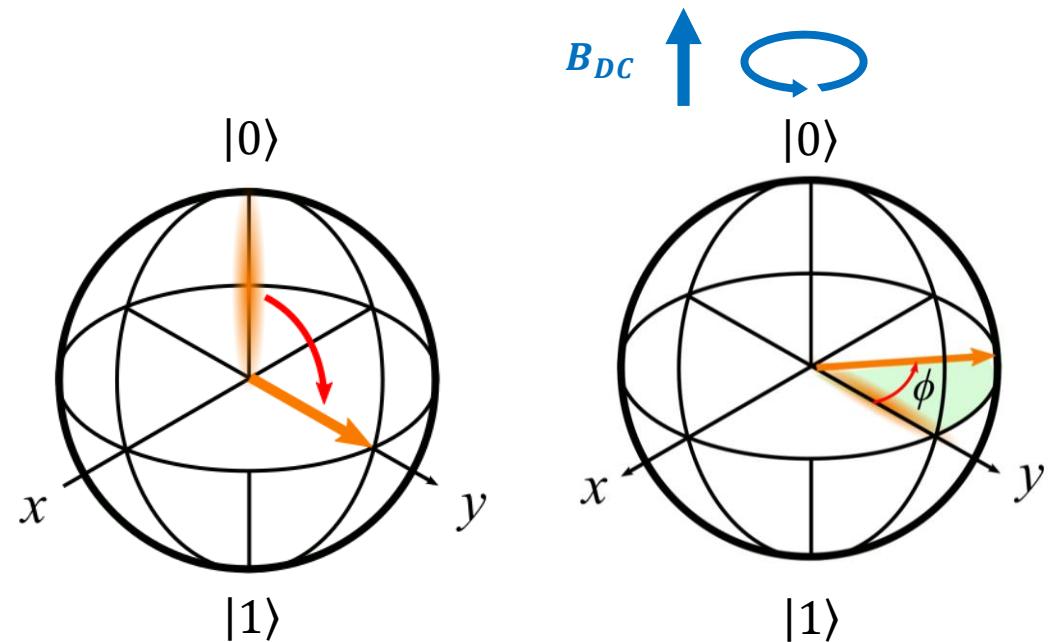
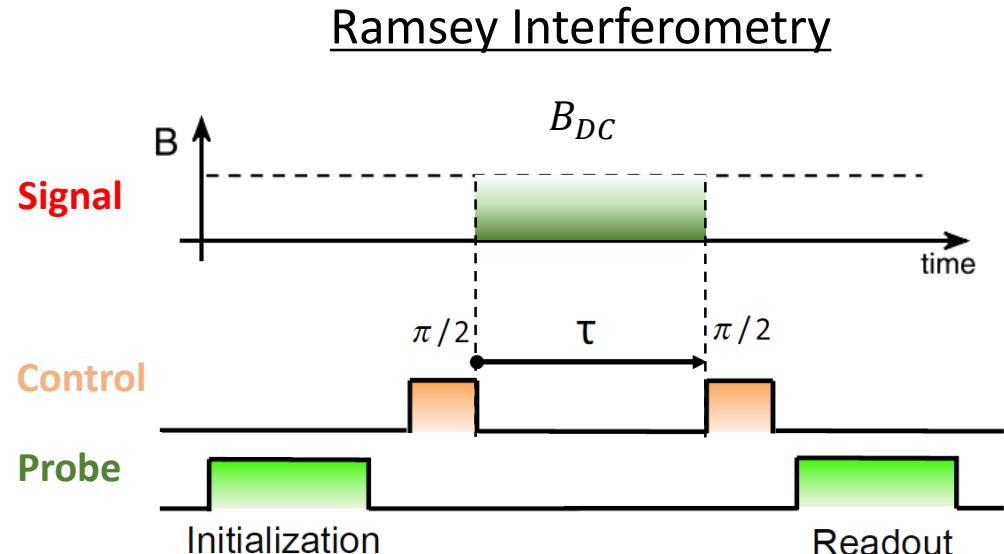


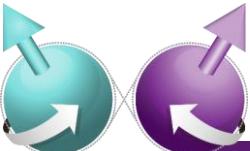
# Sensing static (DC) B field

$$|1\rangle \xrightarrow{\Delta E}$$

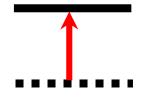
$$|0\rangle$$

$$|\psi\rangle = \frac{1}{\sqrt{2}}(|0\rangle + e^{i\phi}|1\rangle)$$

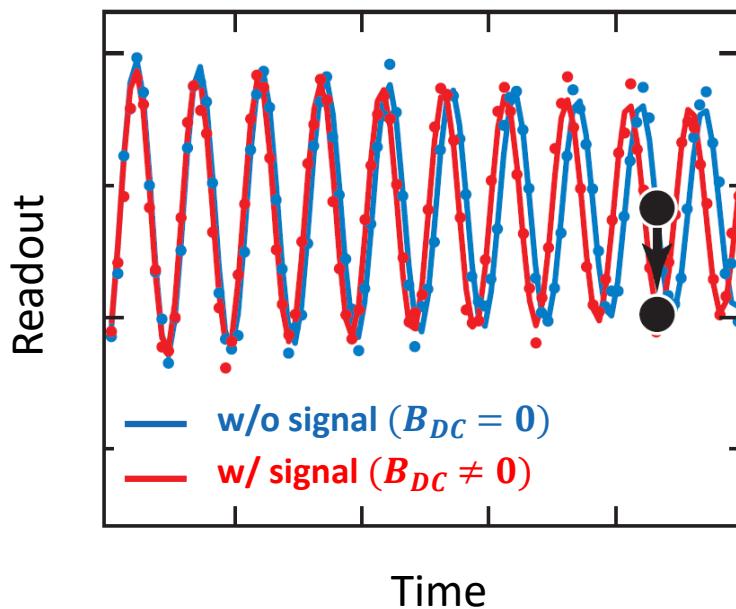
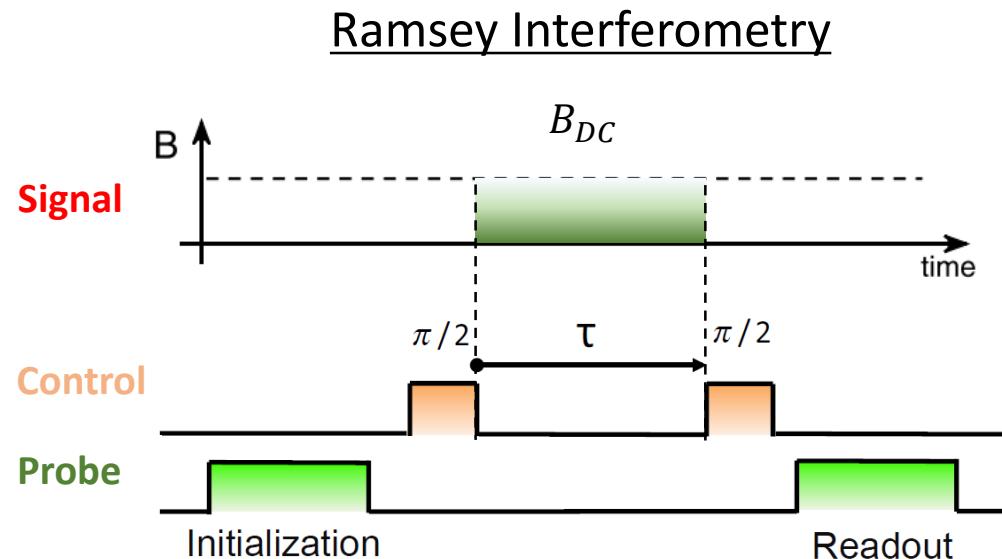




# Sensing static (DC) B field

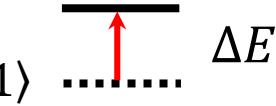
$|1\rangle$    $\Delta E$

$|0\rangle$  



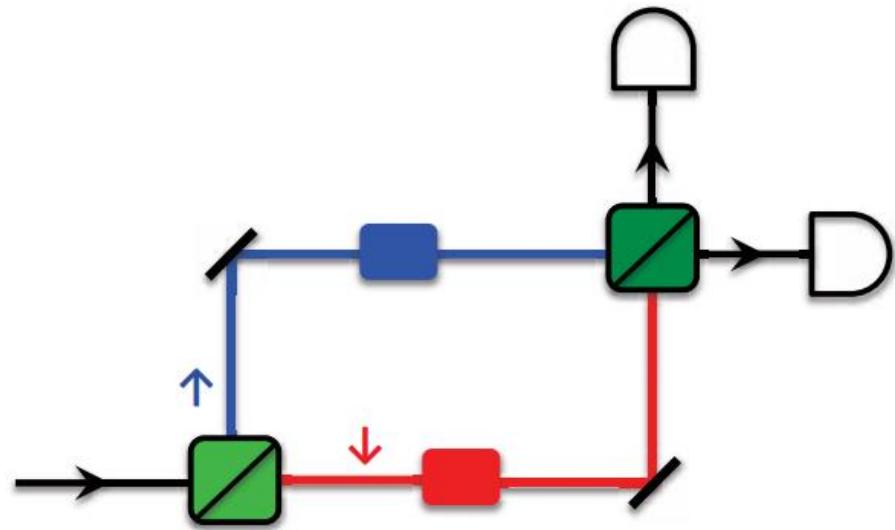
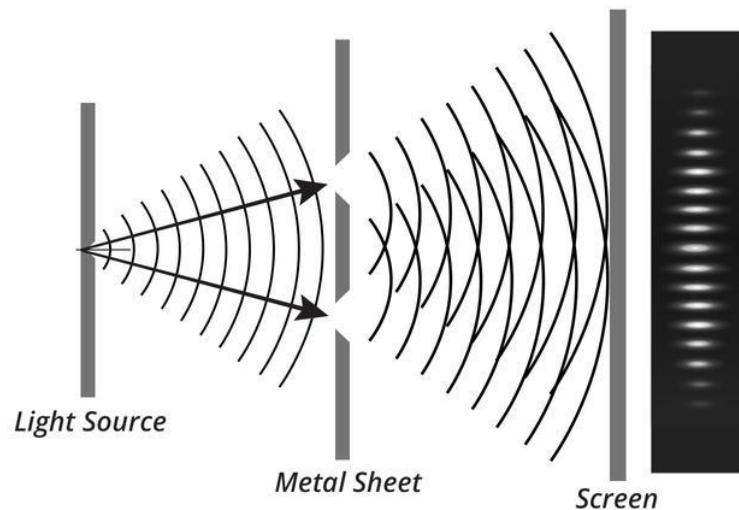
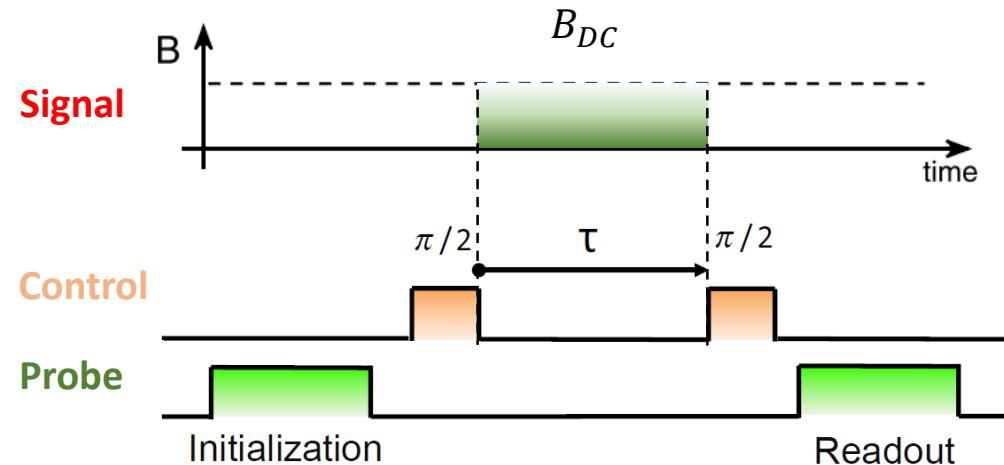


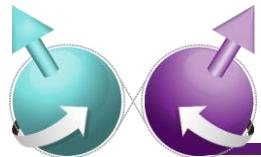
# Sensing static (DC) B field

$|1\rangle$  

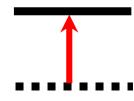
$|0\rangle$

## Ramsey Interferometry

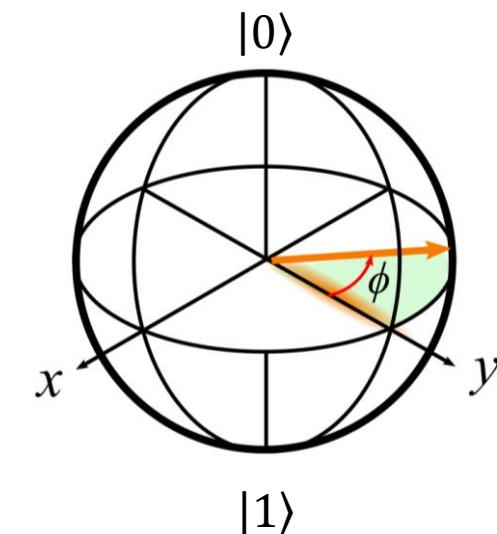
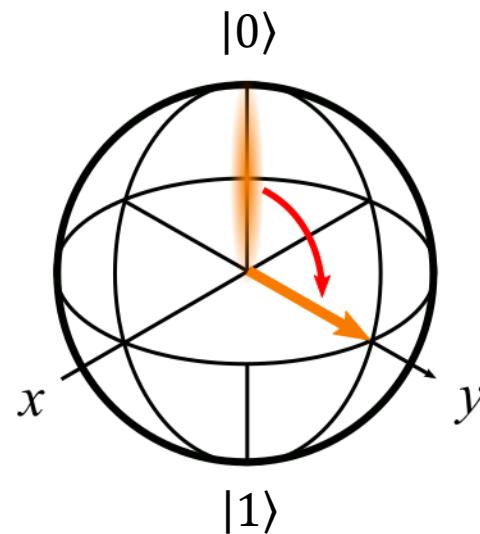
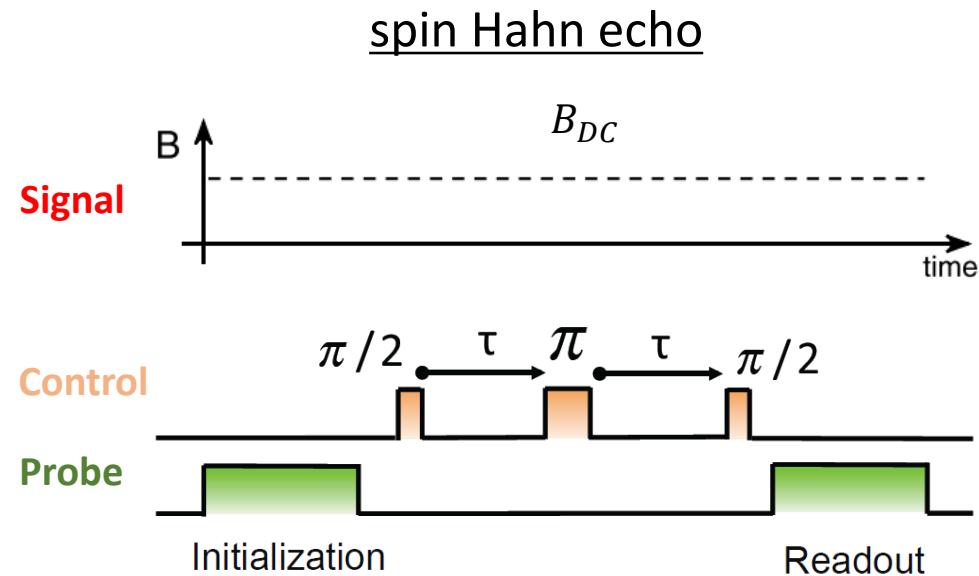


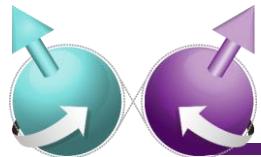


# Sensing dynamics (AC) B field

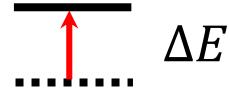
$|1\rangle$    $\Delta E$

$|0\rangle$  

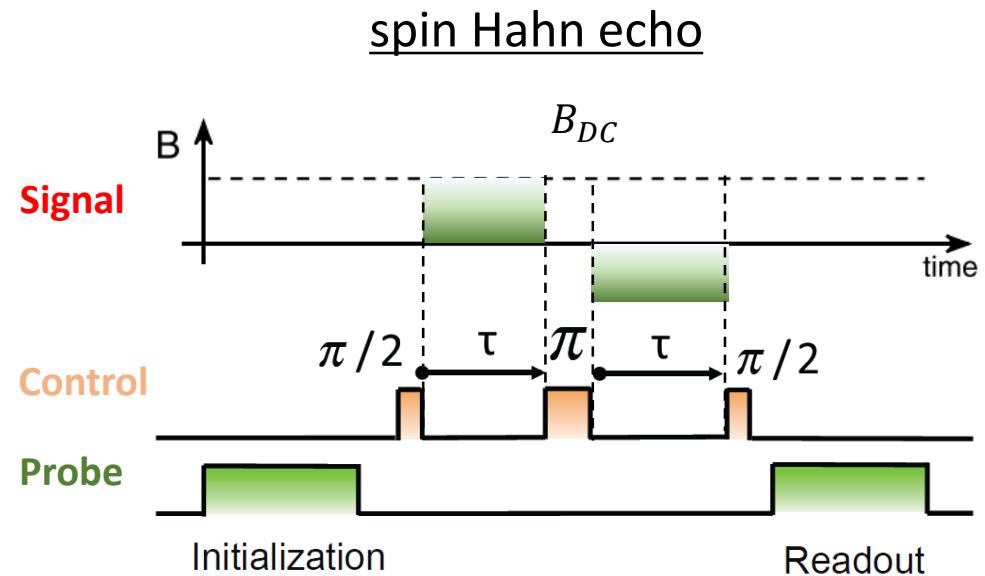




# Sensing dynamics (AC) B field

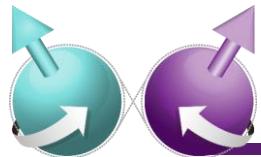
$|1\rangle$  

$|0\rangle$

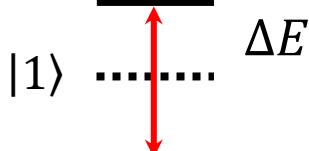


$$\phi = \phi_1 - \phi_2 = 0$$

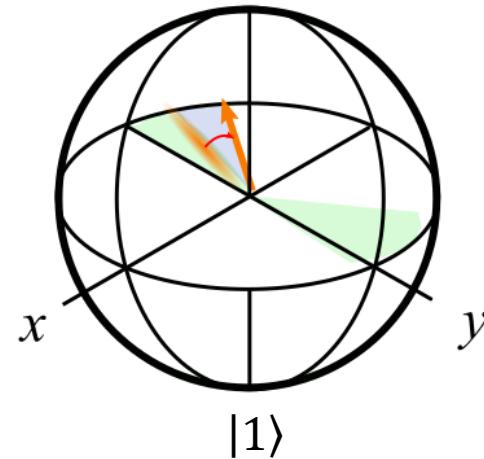
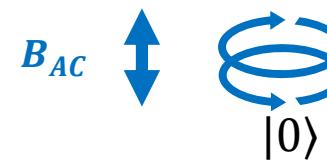
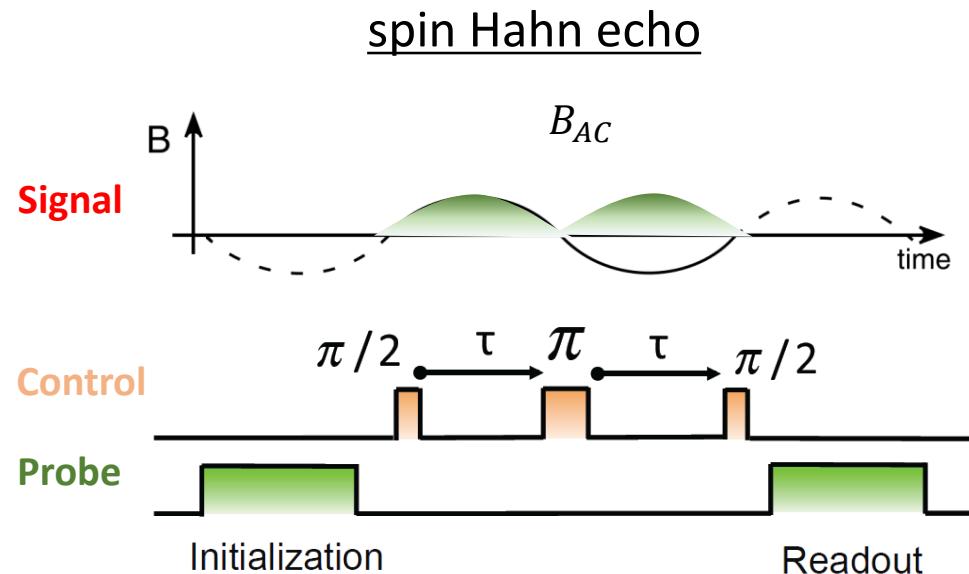
for DC signal

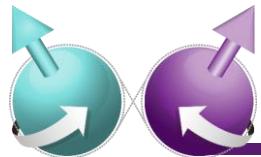


# Sensing dynamics (AC) B field

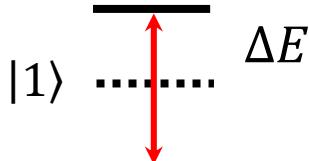


$|0\rangle$



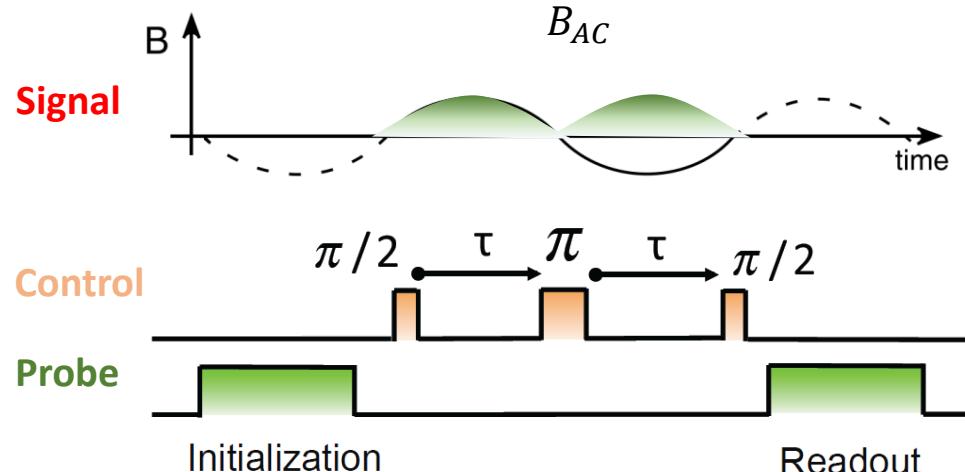


# Sensing dynamics (AC) B field

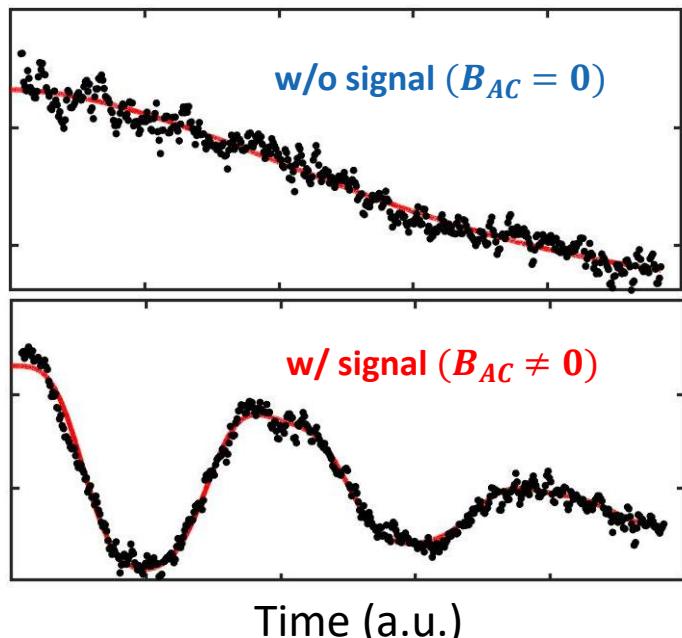


$|0\rangle$

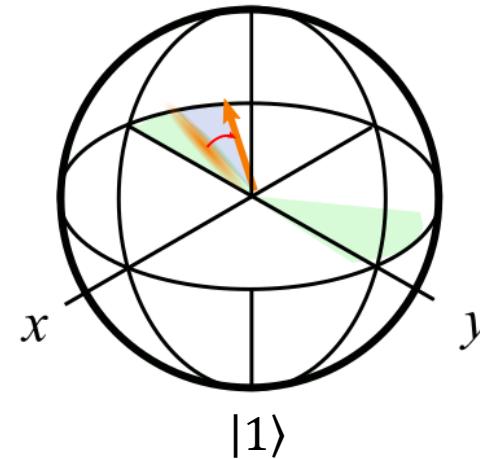
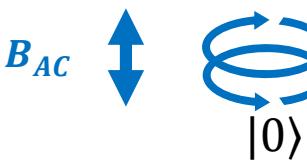
spin Hahn echo

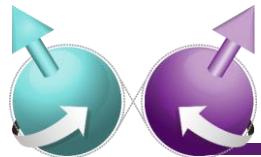


Readout (a.u.)



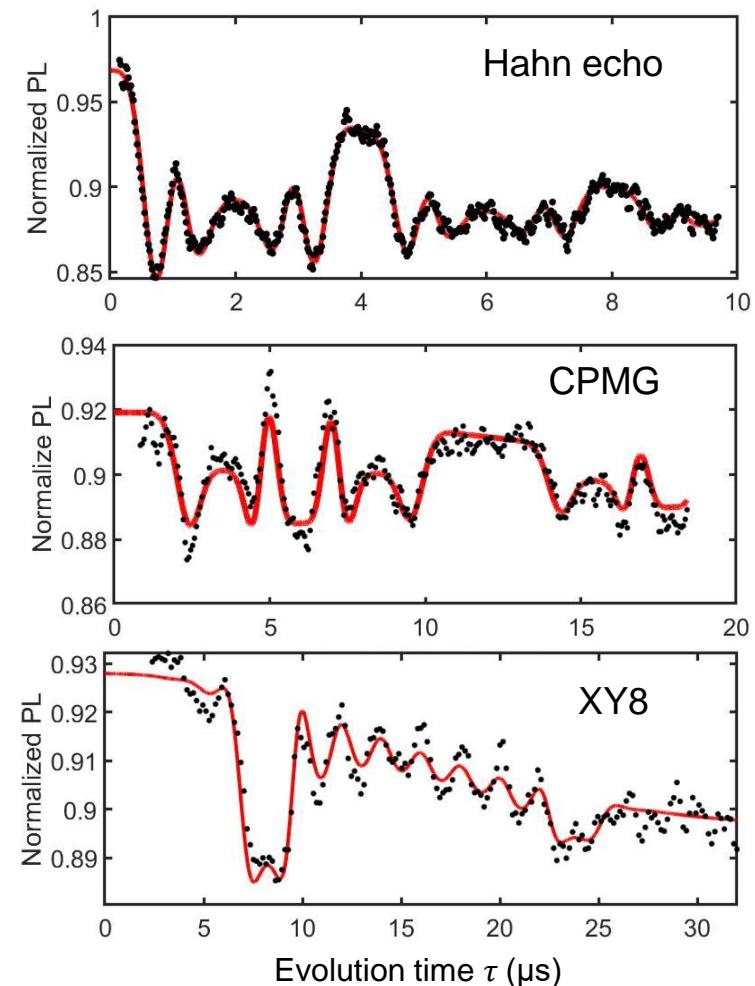
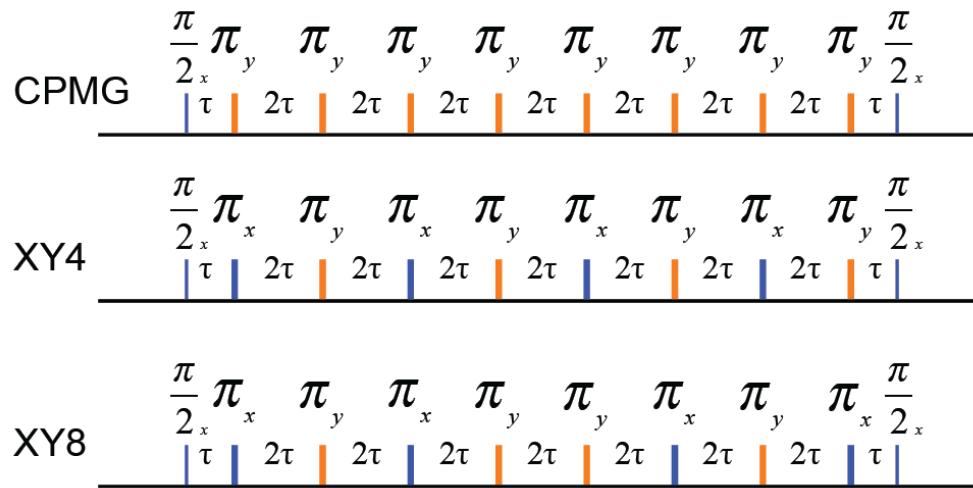
Time (a.u.)

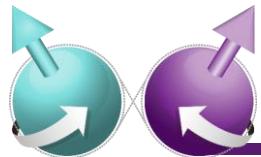




# Sensing dynamics (AC) B field

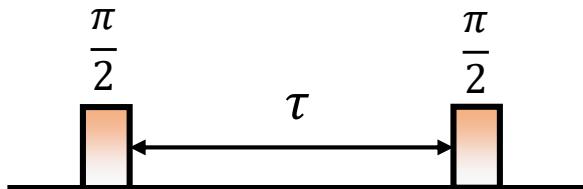
## Dynamical decoupling



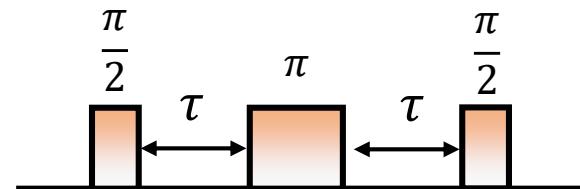


# Sensing dynamics (AC) B field

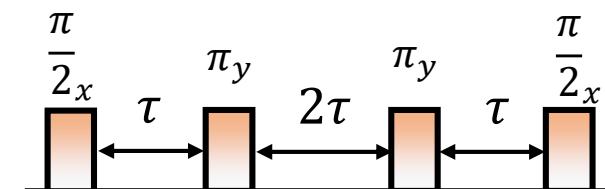
Ramsey



Hahn echo

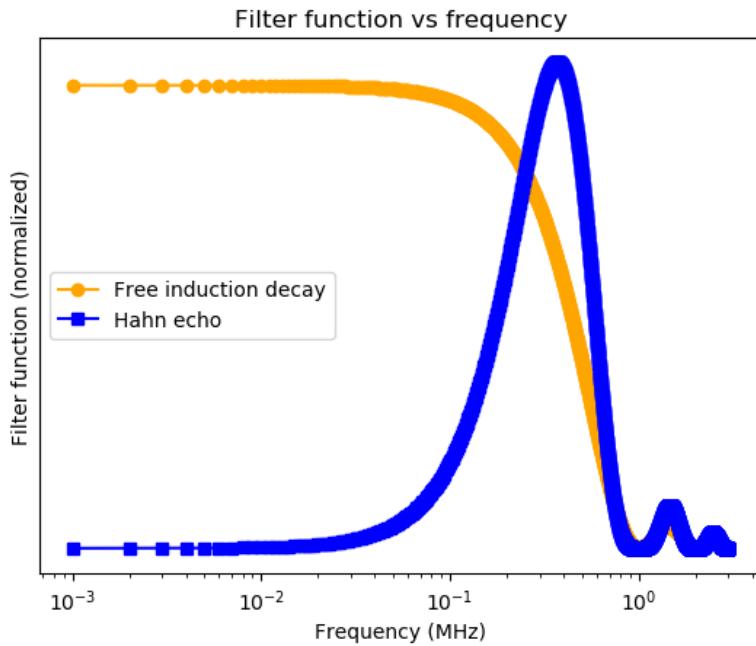


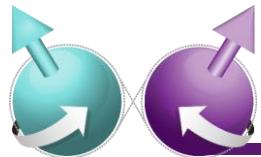
CPMG-N



$$\langle 0 | \rho | 1 \rangle \sim \exp\left\{-\frac{1}{\hbar^2} \int_{-\infty}^{\infty} d\omega \tilde{S}(\omega) F(\tau, \omega)\right\}$$

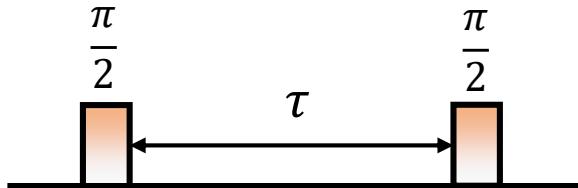
signal      filter function



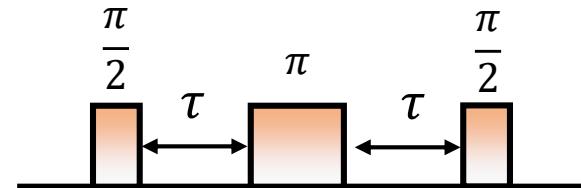


# Sensing dynamics (AC) B field

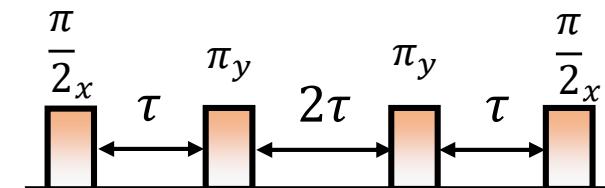
Ramsey



Hahn echo



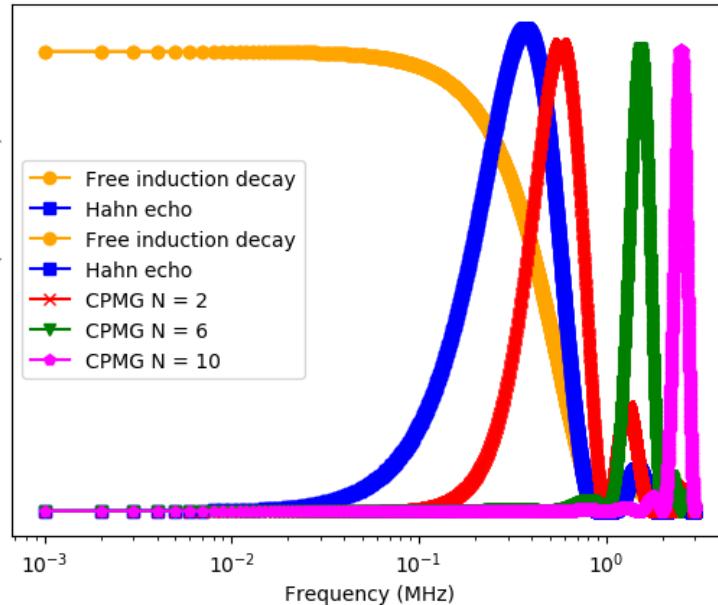
CPMG-N



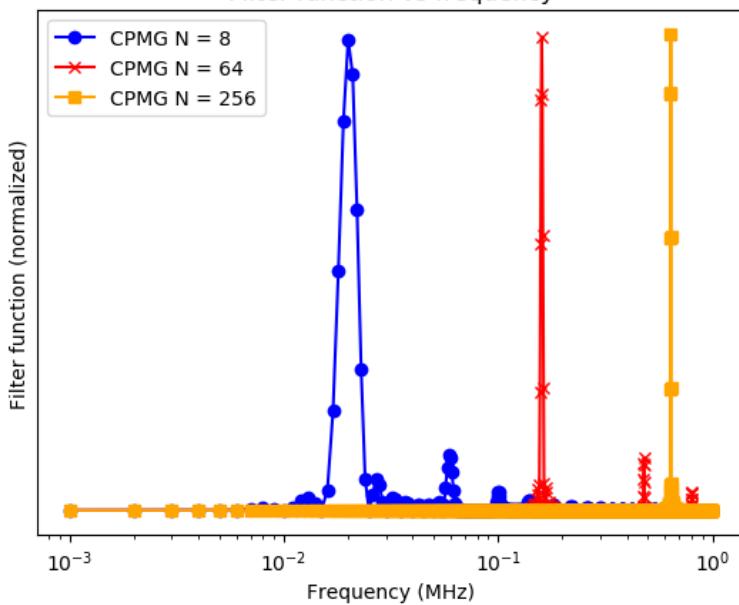
$$\langle 0 | \rho | 1 \rangle \sim \exp\left\{-\frac{1}{\hbar^2} \int_{-\infty}^{\infty} d\omega \tilde{S}(\omega) F(\tau, \omega)\right\}$$

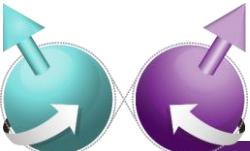
signal                          filter function

Filter function vs frequency



Filter function vs frequency

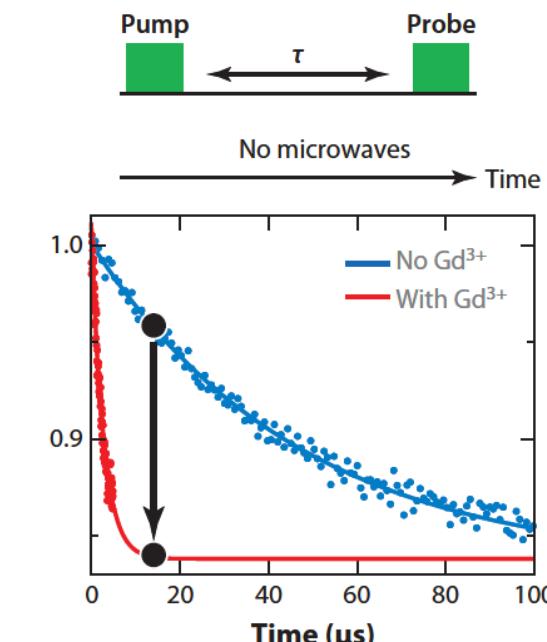
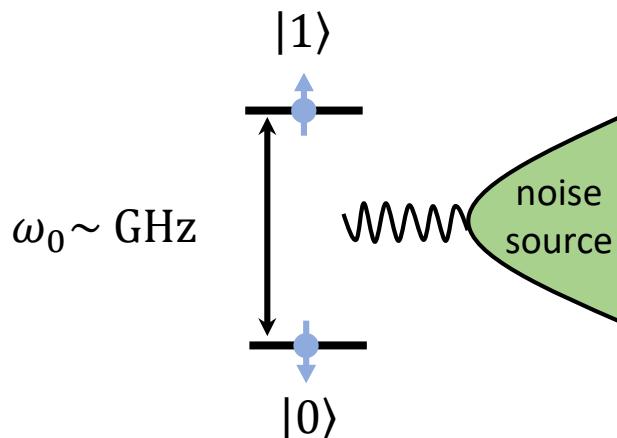


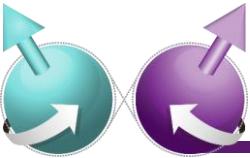


# Sensing dynamics (AC) B field

General quantum sensing methods

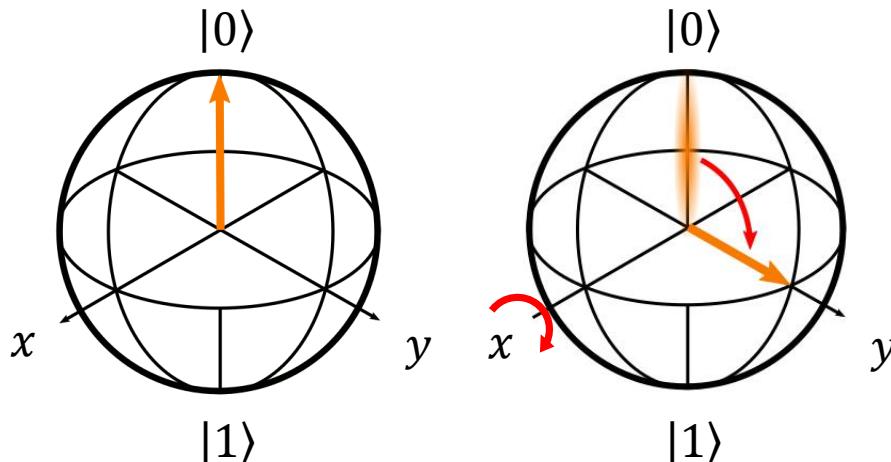
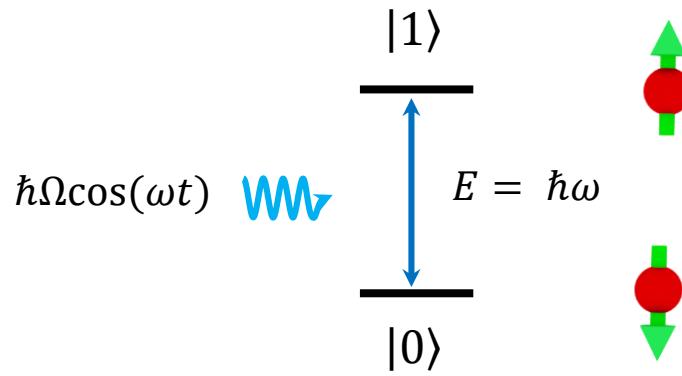
- {
- DC (dc  $\sim$  kHz) : Ramsey
  - AC (kHz  $\sim$  100 kHz) : Echo
  - AC ( $\sim$  MHz) : CPMG, XY4, XY8
  - :
  - AC ( $\sim$  GHz) :  $T_1$  relaxometry



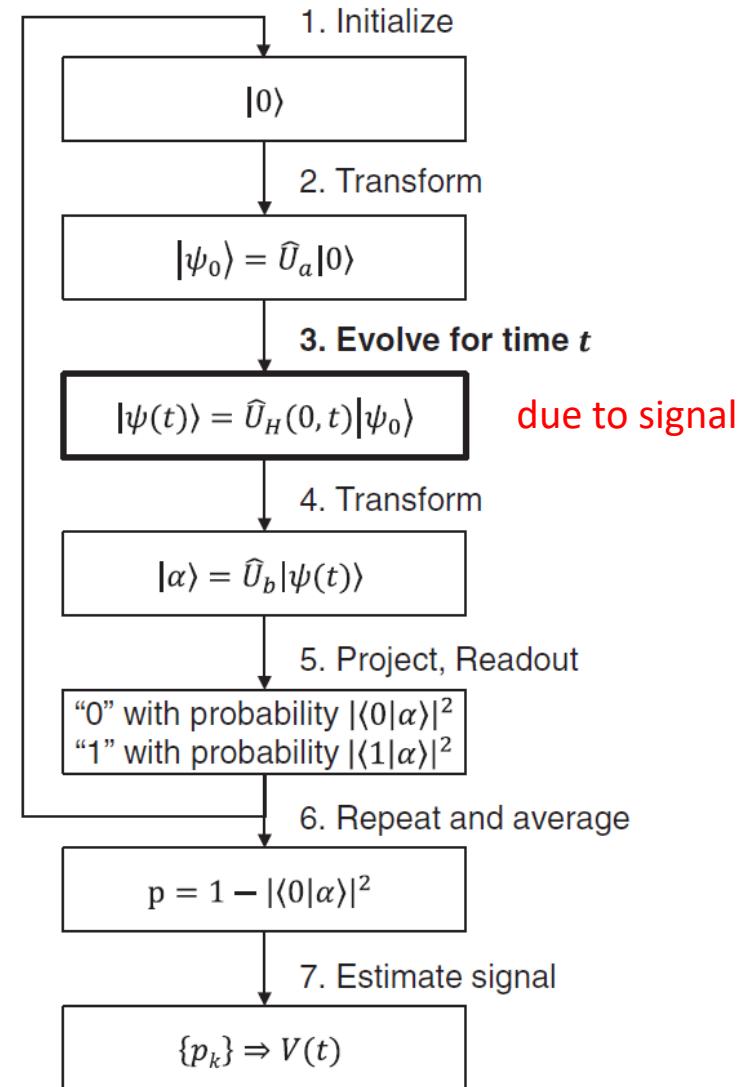


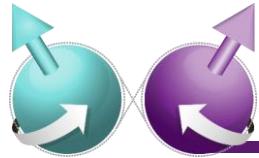
# Quantum sensing protocol

**Qubit**

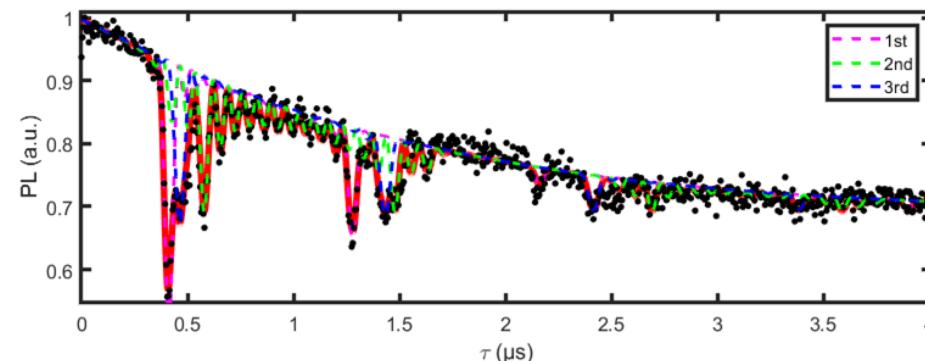
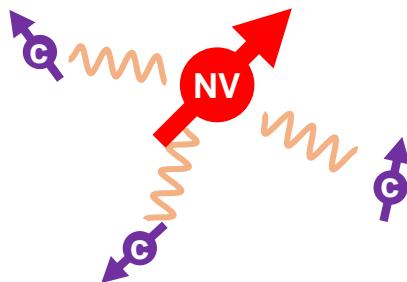


$$|\psi\rangle = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle)$$



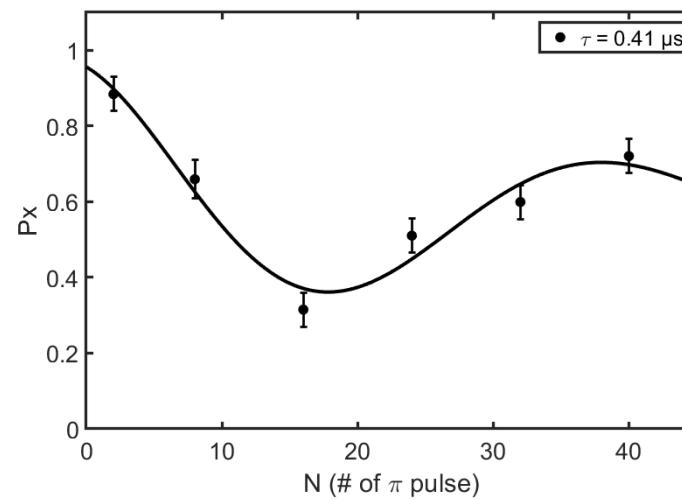
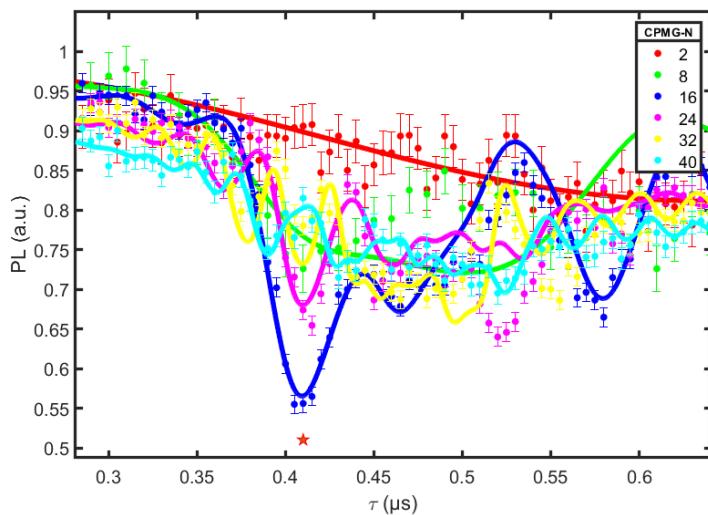


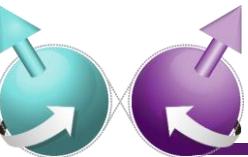
# Advanced quantum sensing with multi-qubits



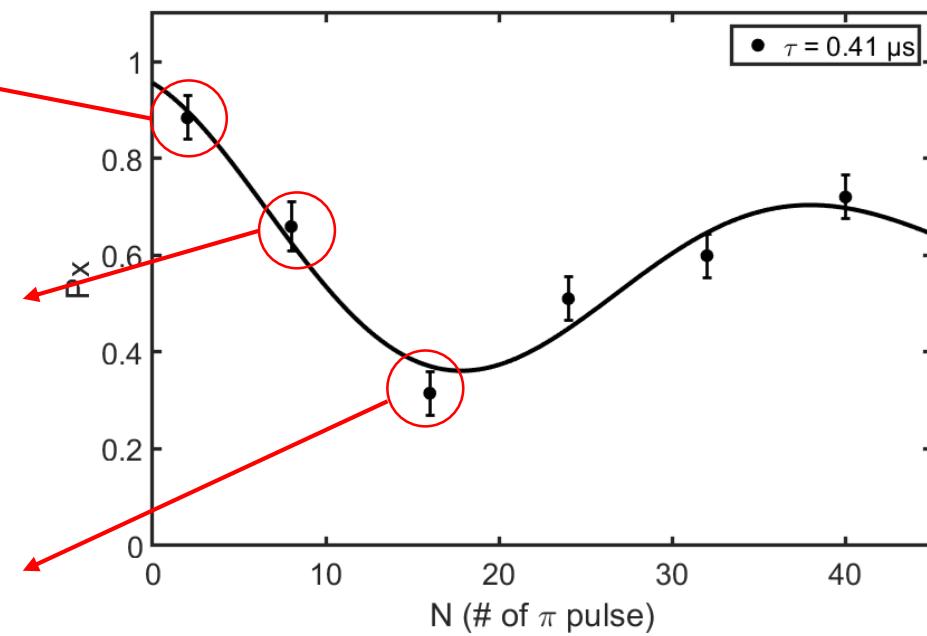
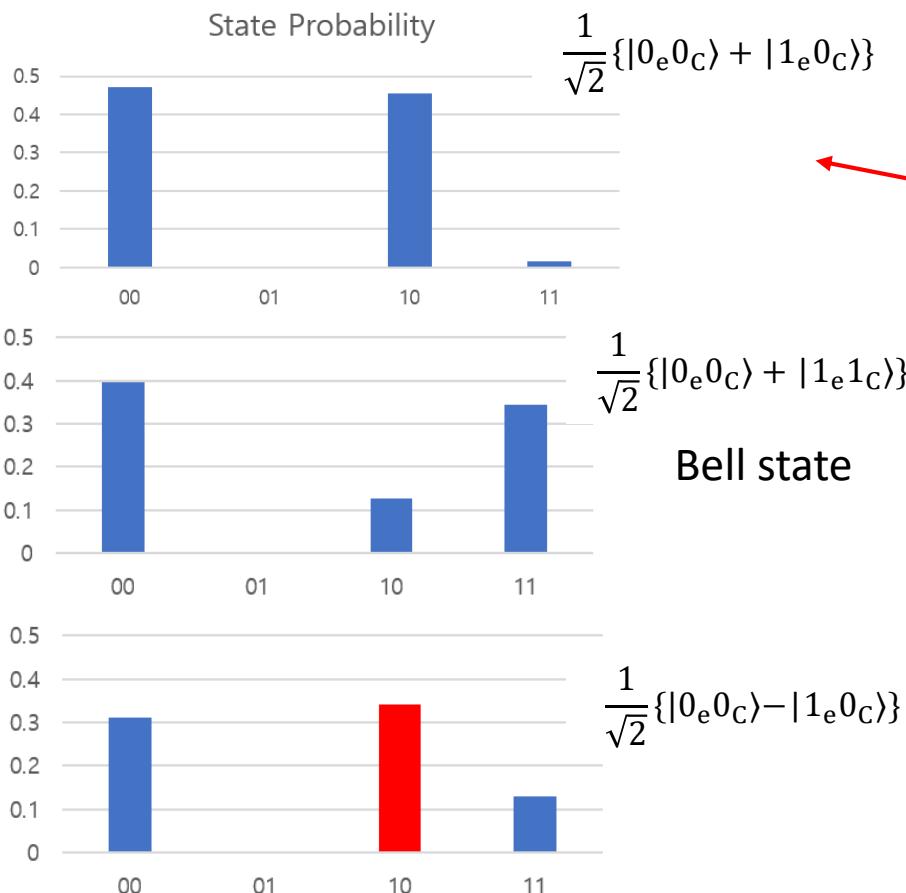
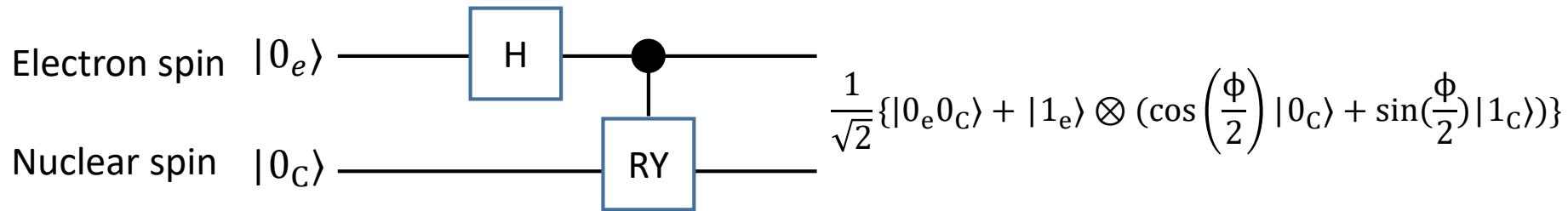
<sup>13</sup> C index	1	2	3
A <sub>  </sub> (kHz)	167.7 ± 11.2	- 46.2 ± 11.8	54.6 ± 12.0
A <sub>⊥</sub> (kHz)	99.65 ± 6.9	148.8 ± 2.4	55.1 ± 2.9

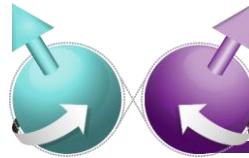
CPMG based C<sub>e</sub>NOT<sub>n</sub> operation





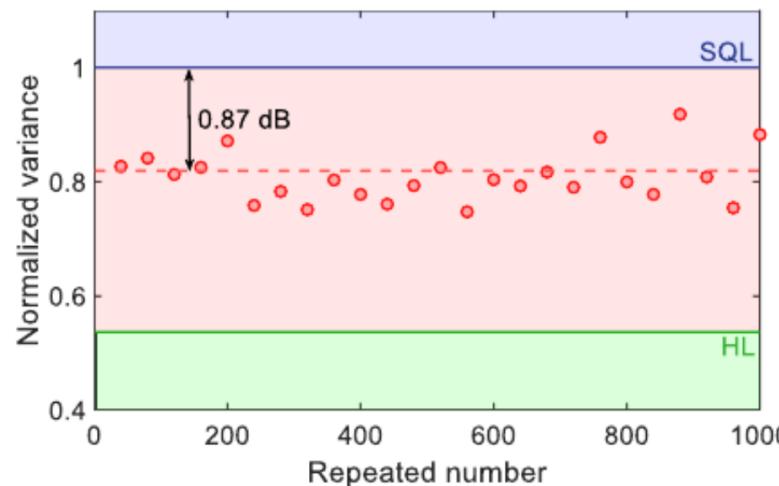
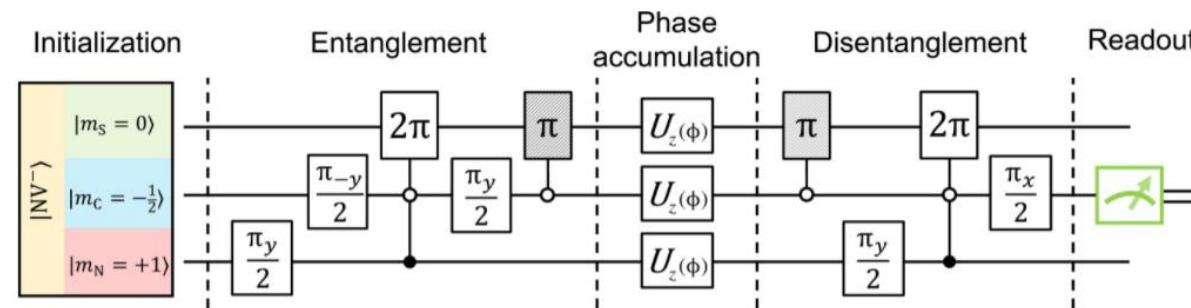
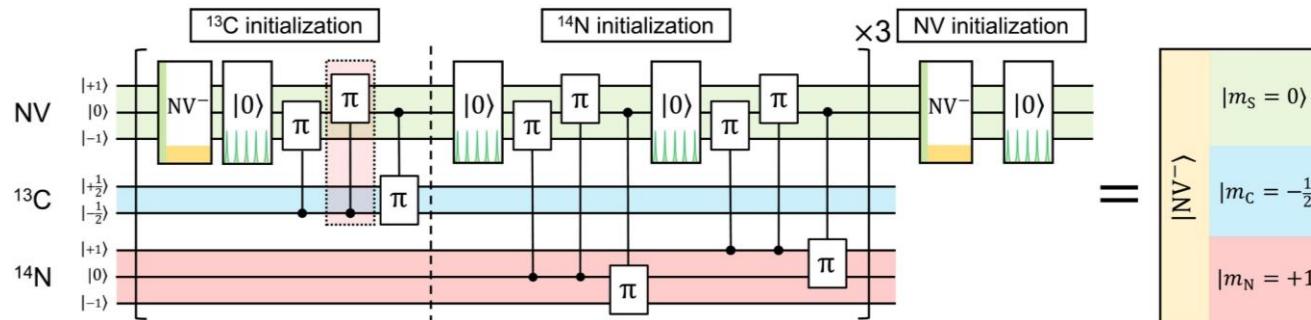
# Advanced quantum sensing with multi-qubits

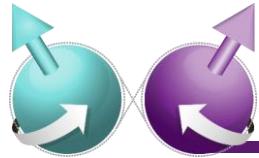




# Advanced quantum sensing with multi-qubits

## Quantum sensing below standard quantum limit

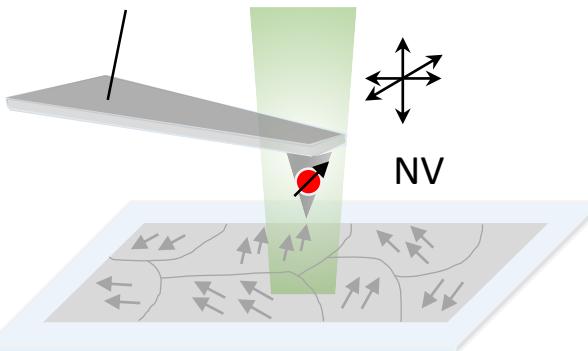




# Quantum imaging based on diamond NV centers

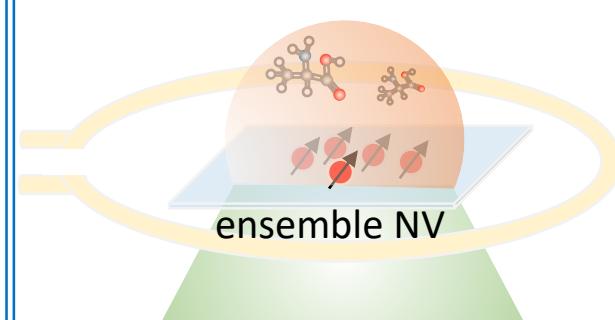
nm scale imaging

Scanning probe



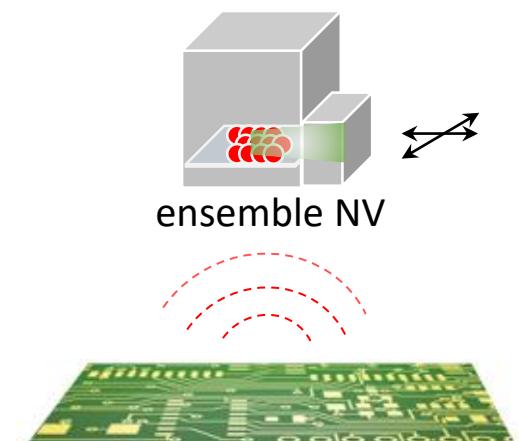
μm scale imaging

magnetic sample



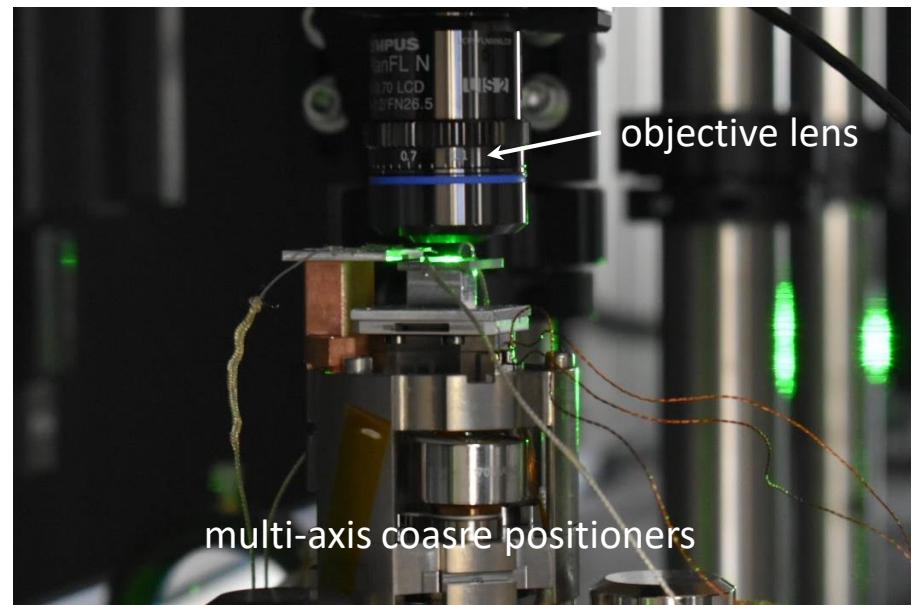
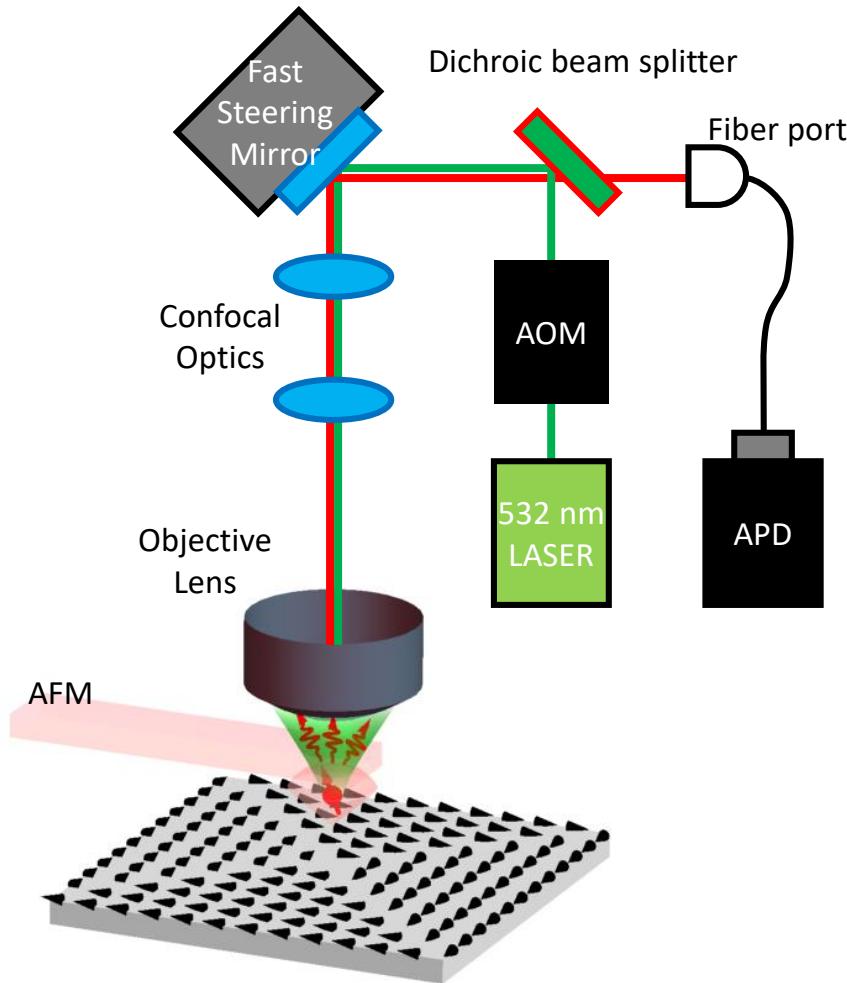
mm scale imaging

ensemble NV



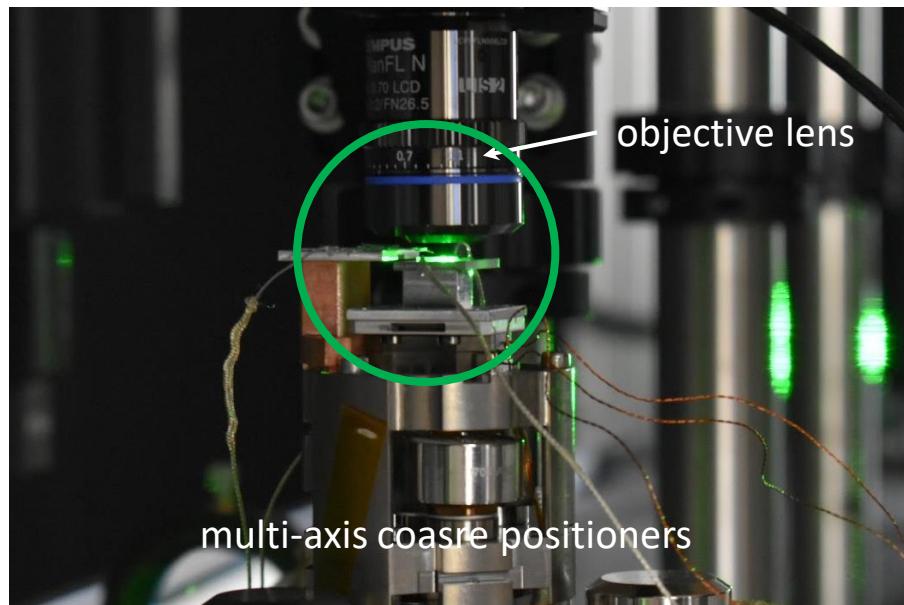
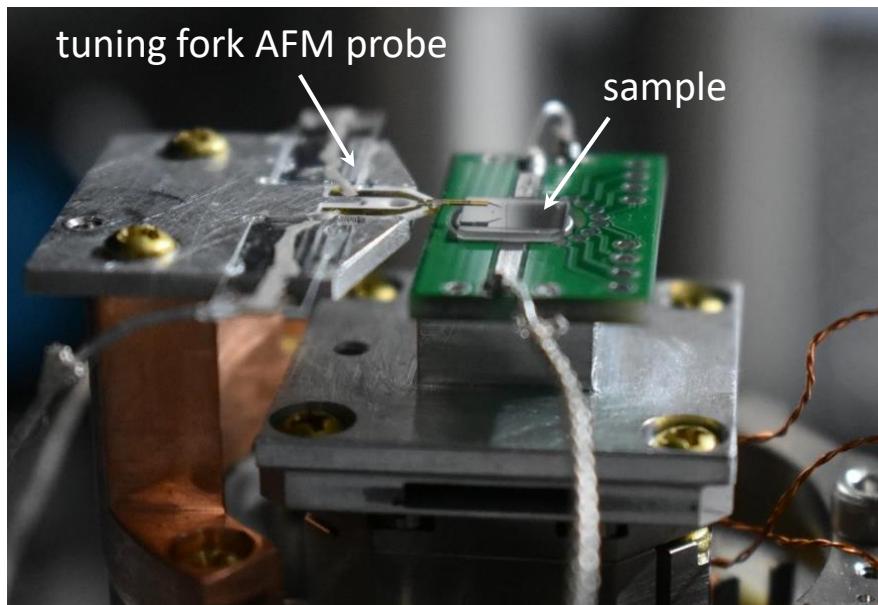


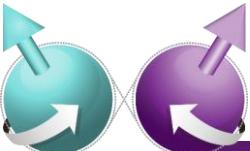
# Imaging with single spin scanning magnetometer



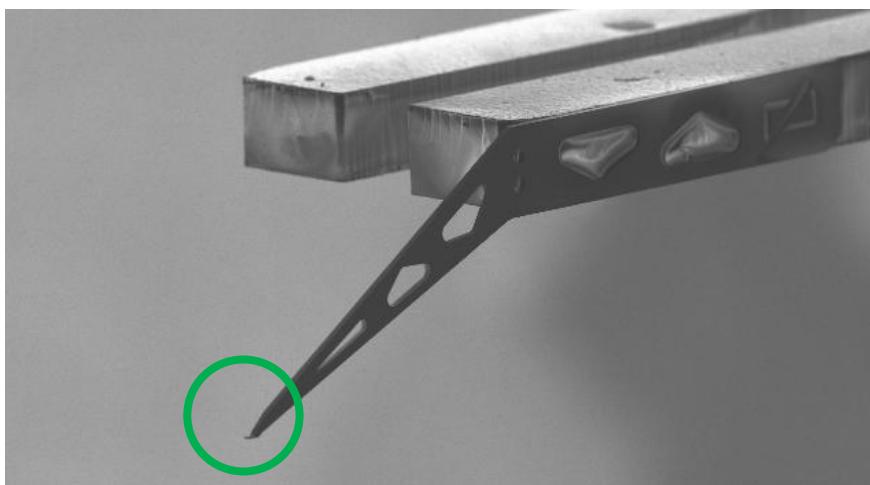
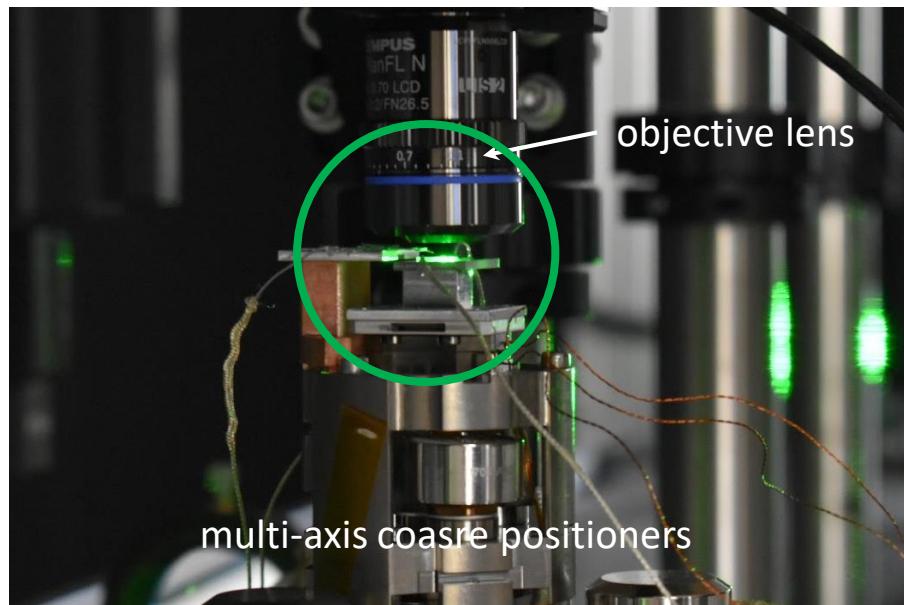
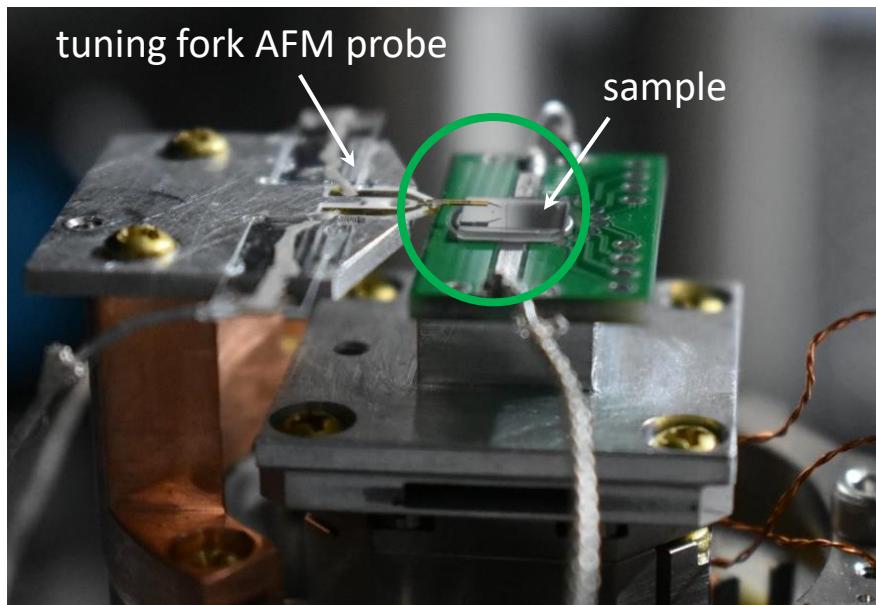


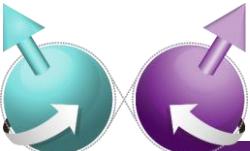
# Imaging with single spin scanning magnetometer



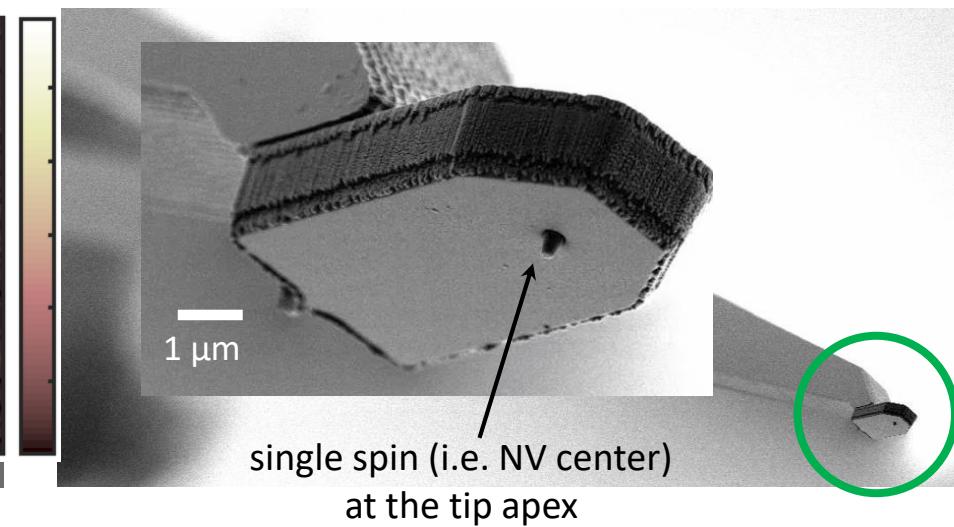
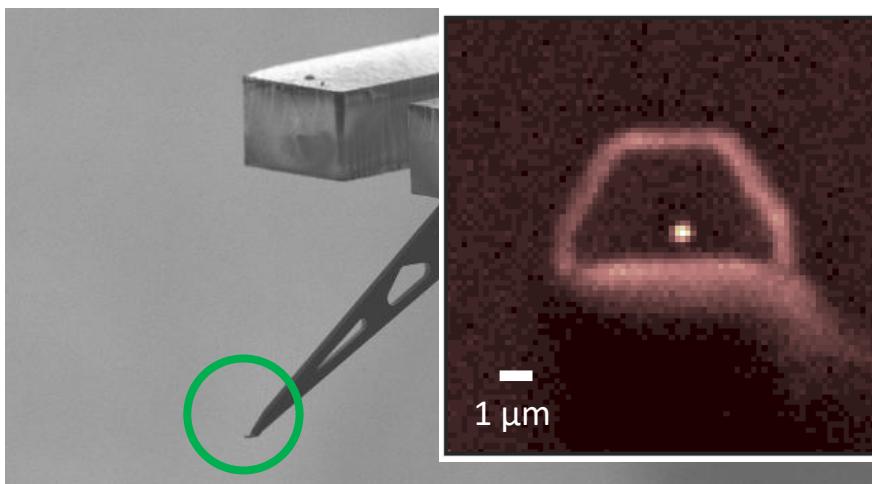
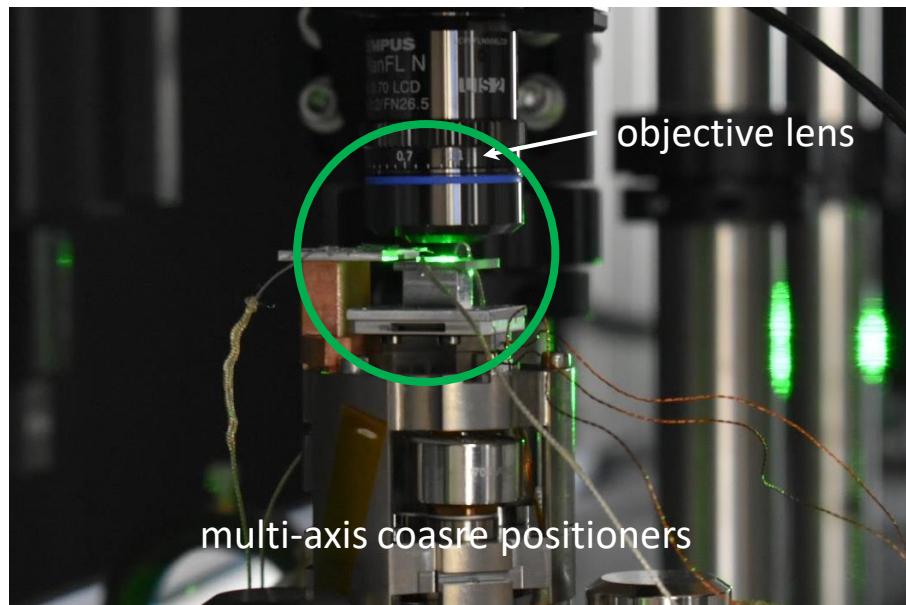
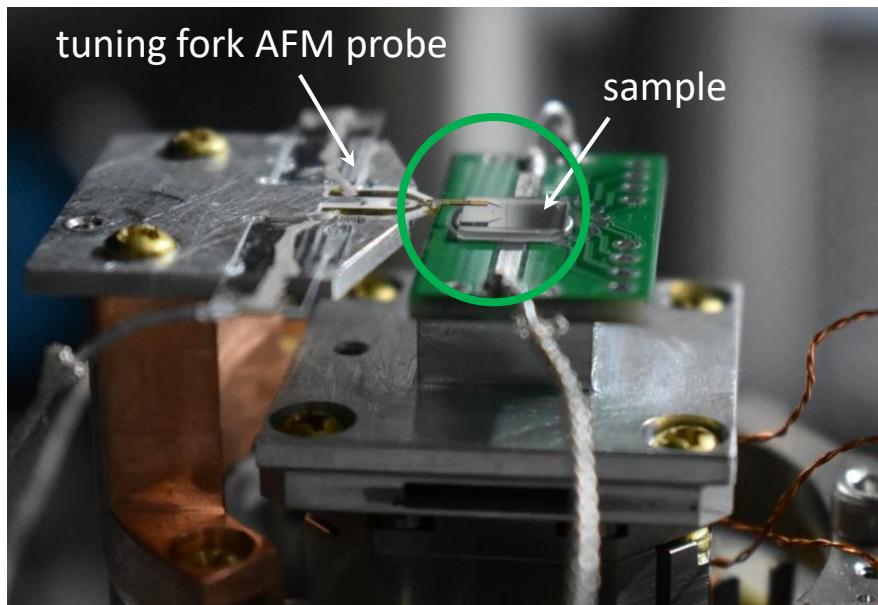


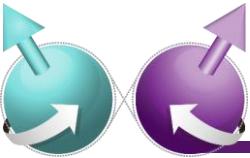
# Imaging with single spin scanning magnetometer





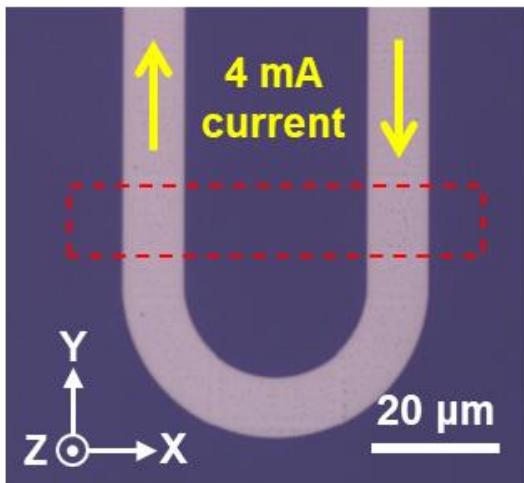
# Imaging with single spin scanning magnetometer



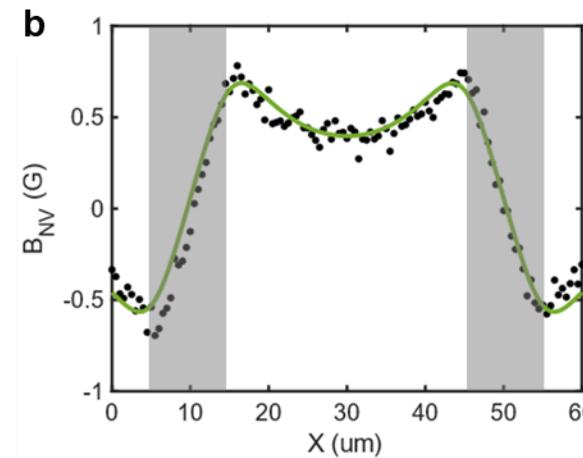
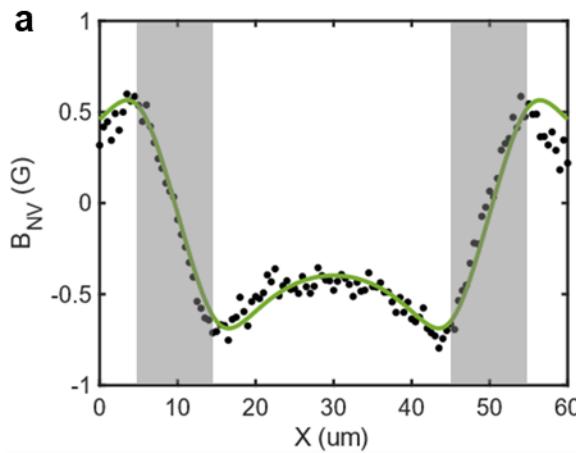
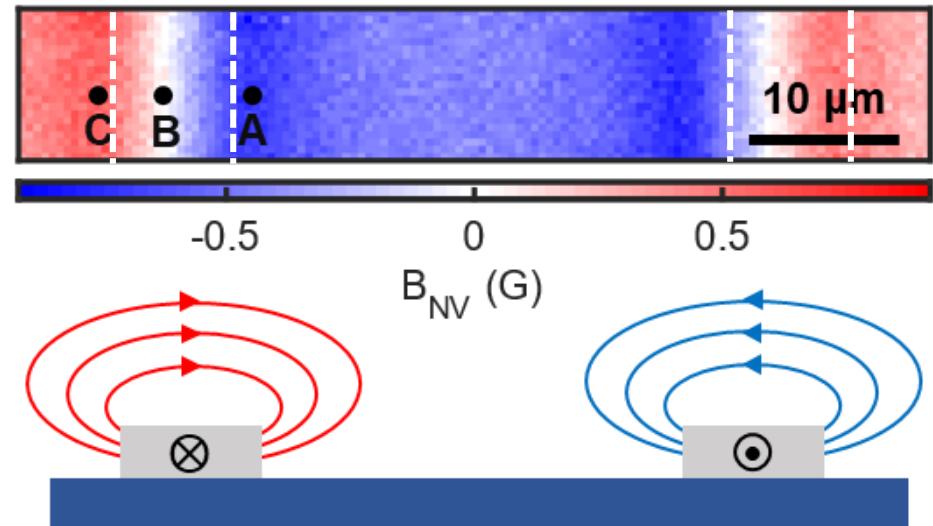


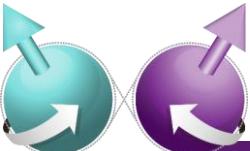
# Imaging example with current device

- Optical image of Pt wire



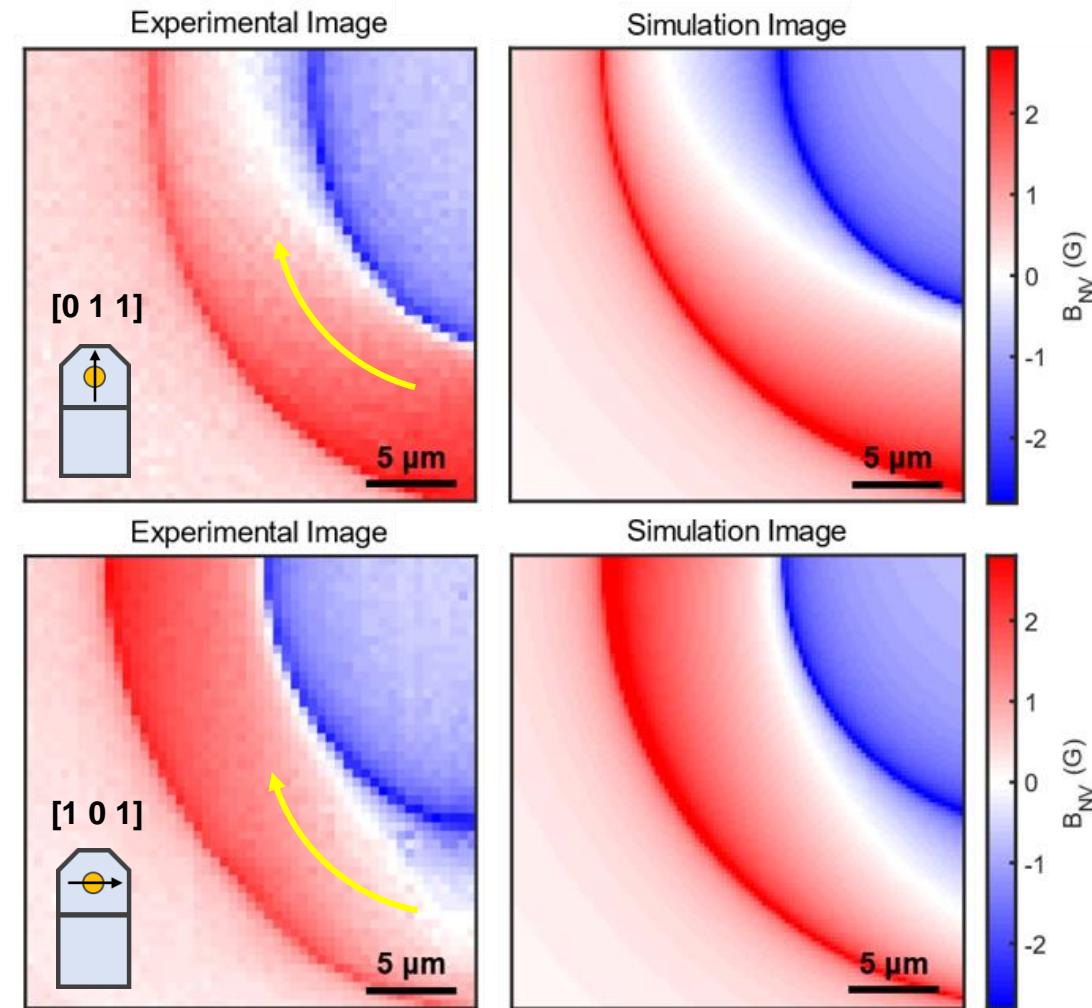
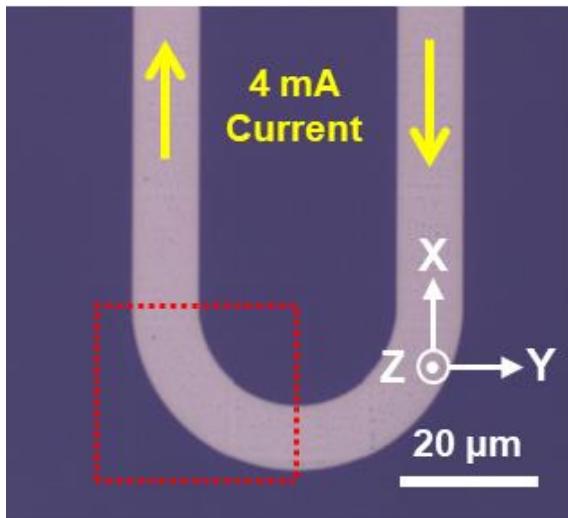
- Magnetic field image of the dashed area

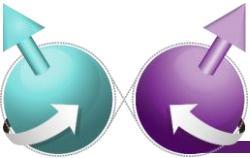




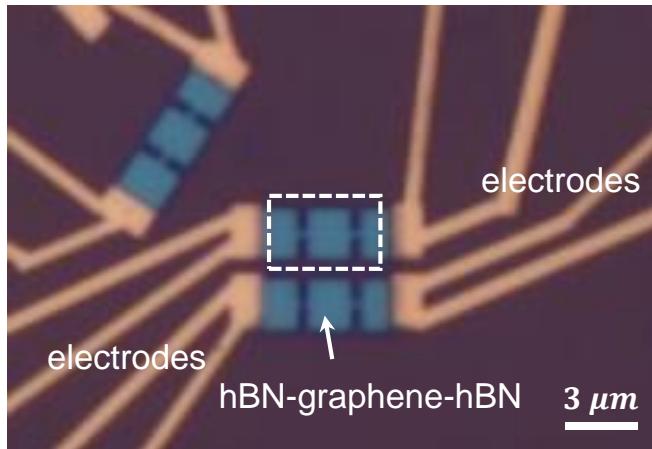
# Imaging example with current device

- Optical image of Pt wire

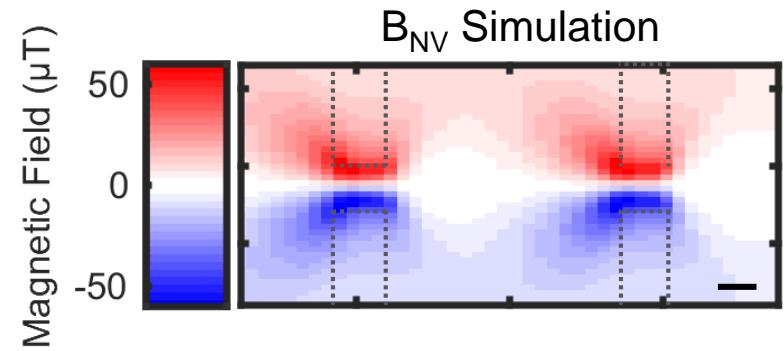
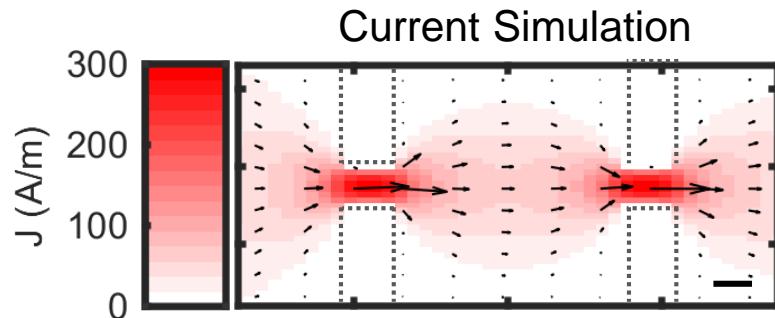
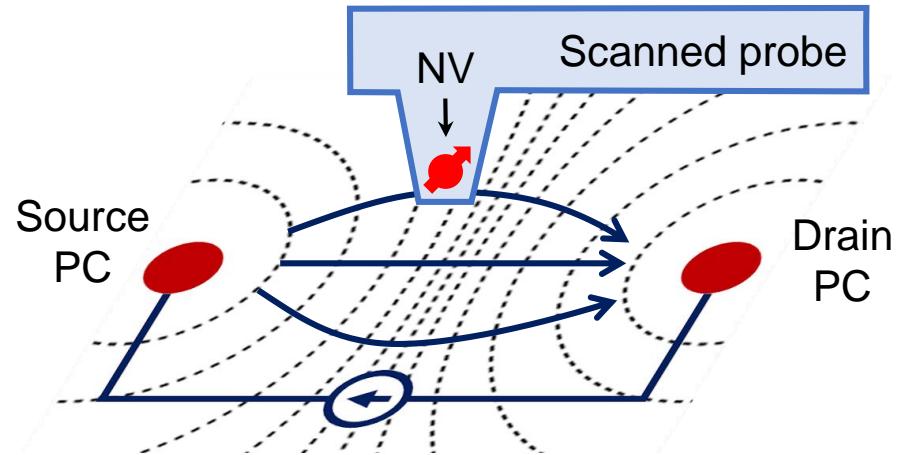




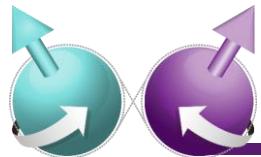
# Imaging example with graphene device



Graphene sample (Prof. Gil-Ho Lee, POSTECH)

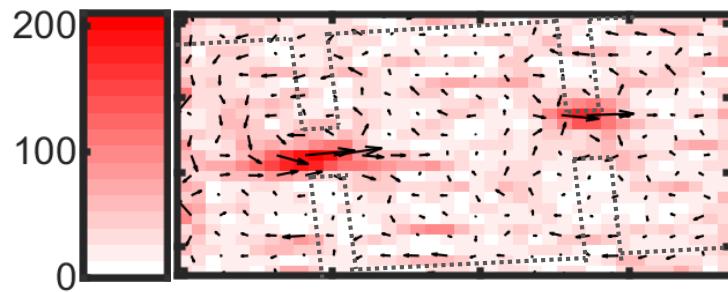


Is a single component of magnetic field enough to reconstruct current profile ? Yes!

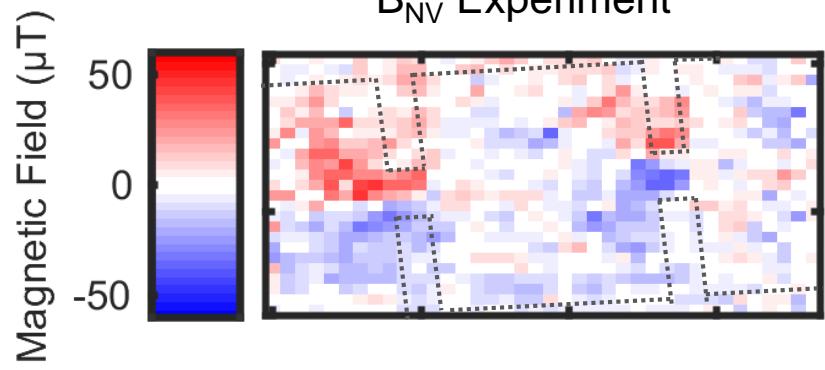


# Imaging example with graphene device

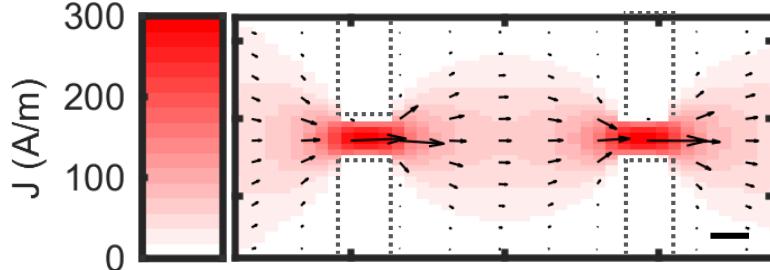
Reconstructed current density



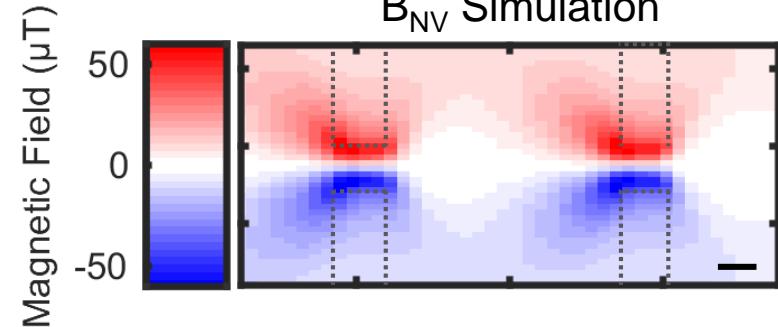
$B_{NV}$  Experiment



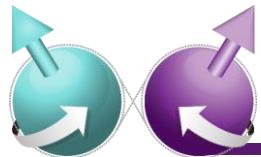
Current Simulation



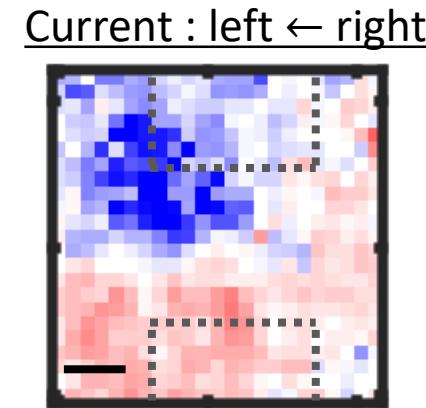
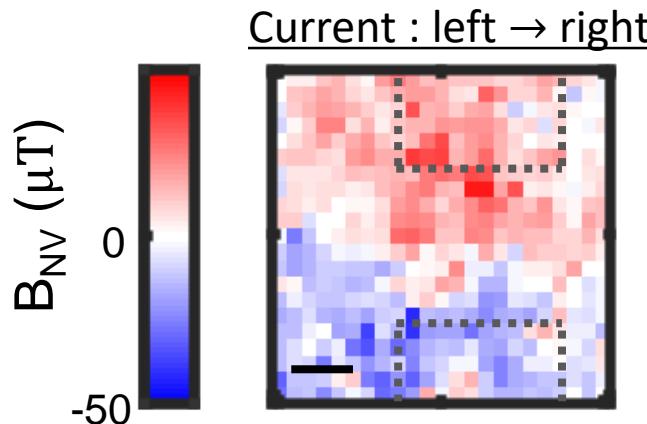
$B_{NV}$  Simulation



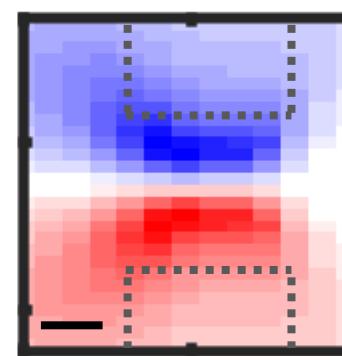
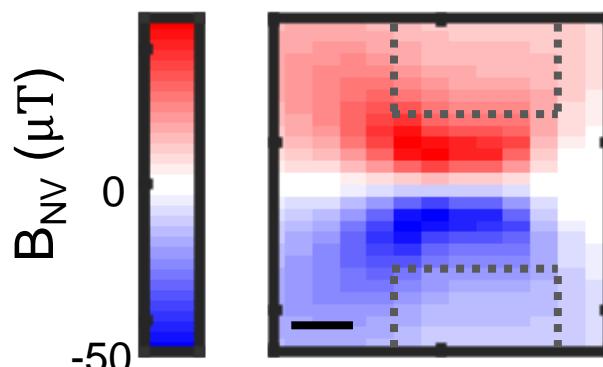
Is a single component of magnetic field enough to reconstruct current profile ? Yes!



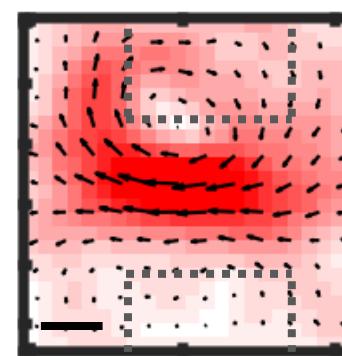
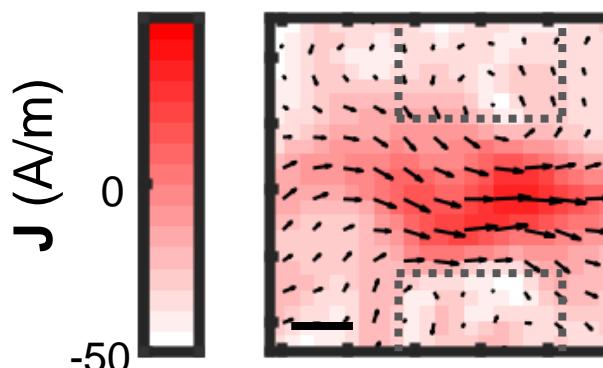
# Imaging example with graphene device



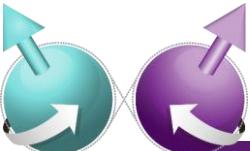
Magnetic field  
(experiment)



Magnetic field  
(simulation)

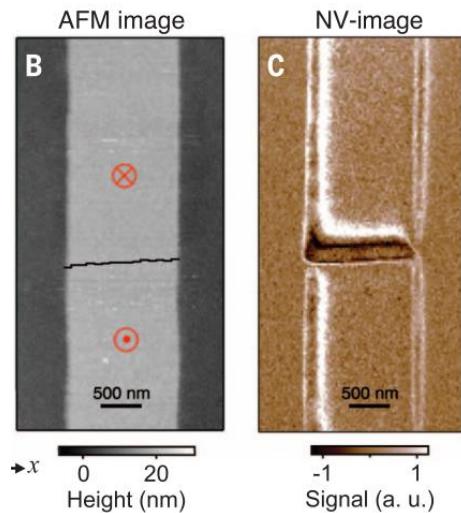


Reconstructed  
current density



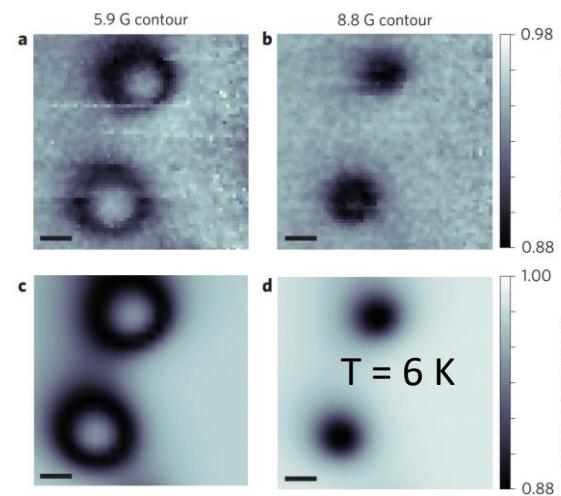
# More imaging examples

## Domain wall



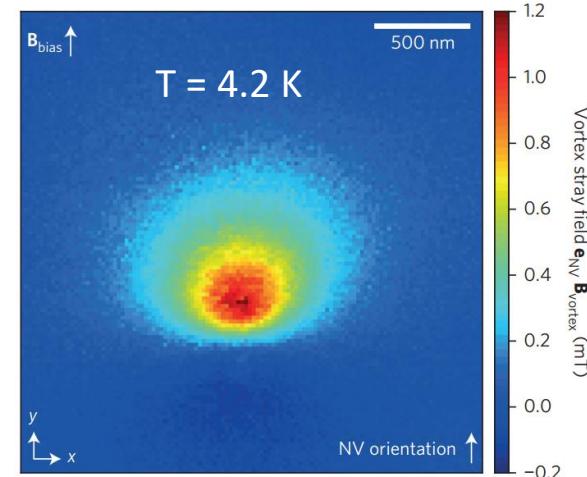
J. P. Tetienne *et al.*, Science (2014)

## Superconducting vortices in BaFe<sub>2</sub>(As<sub>0.7</sub>P<sub>0.3</sub>)<sub>2</sub>



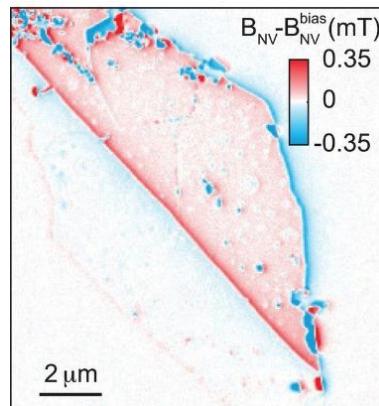
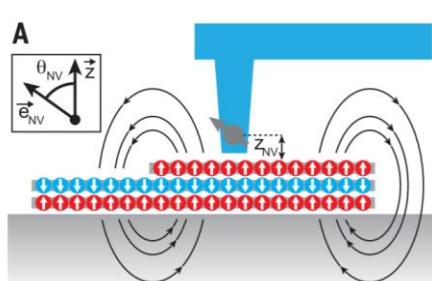
M. Pelliccione *et al.*, Nat. Nano. (2016)

## Superconducting vortex in YBCO



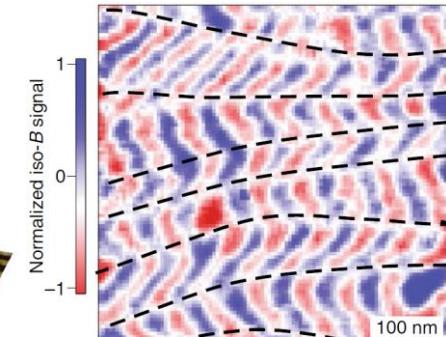
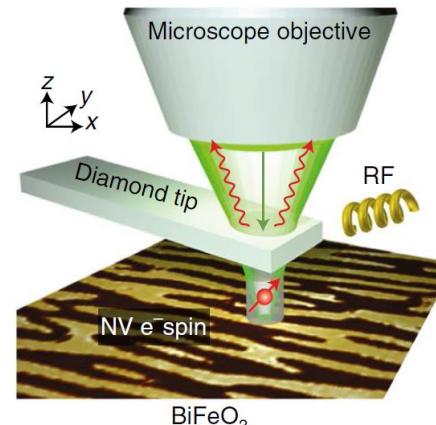
L. Thiel *et al.*, Nat. Nano. (2016)

## 2D ferromagnetism

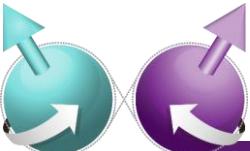


L. Thiel *et al.*, Science (2019)

## Anti-ferromagnetic order

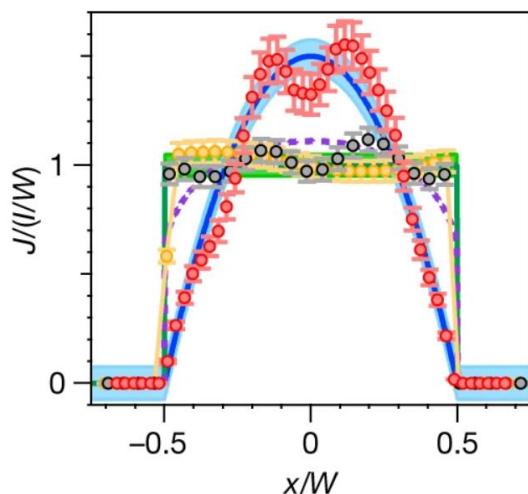
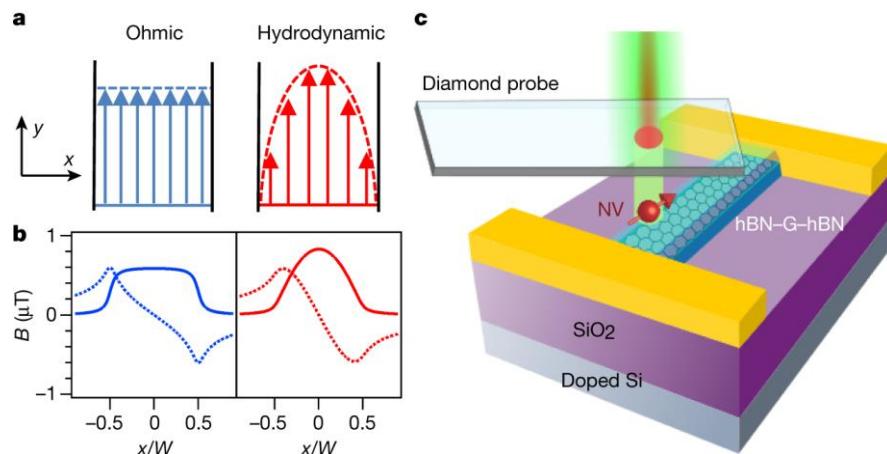


I. Gross *et al.*, Nature (2017)

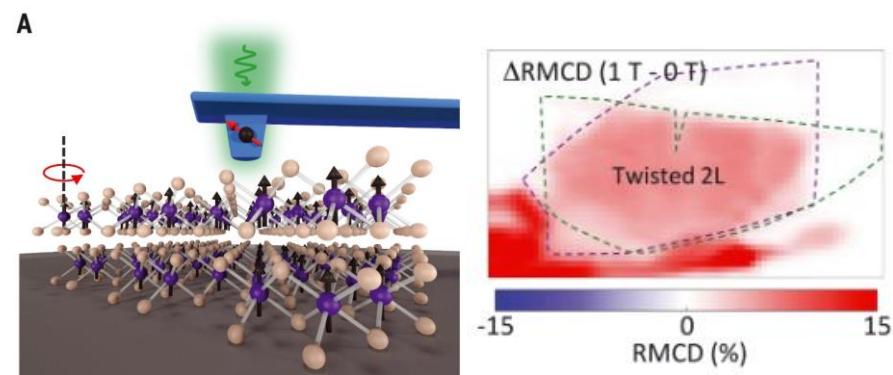


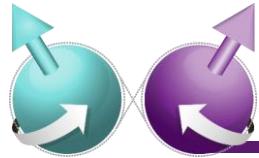
# More imaging examples

## Imaging viscous flow in graphene

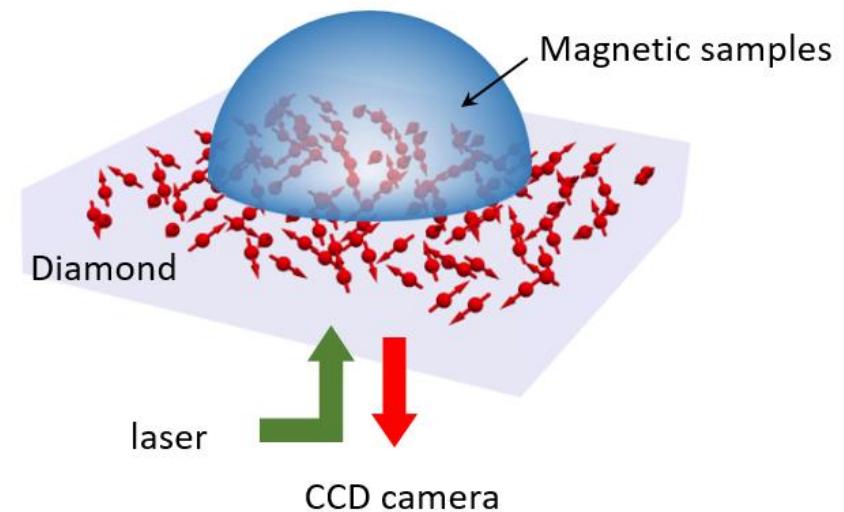
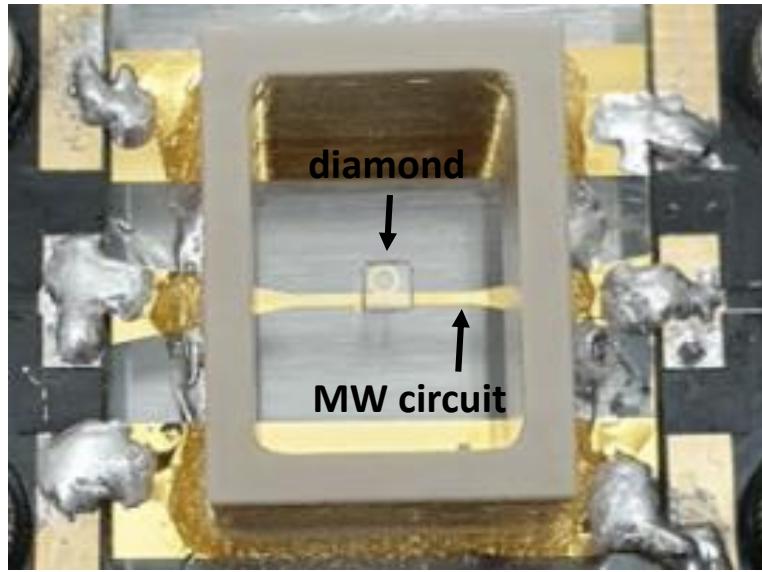
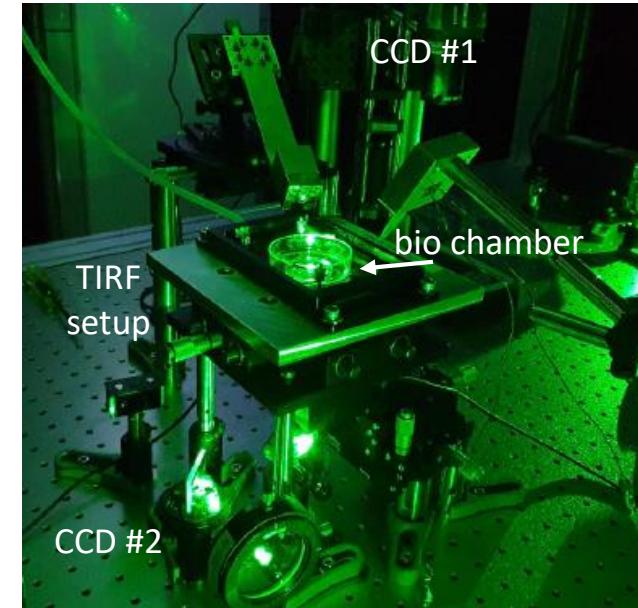
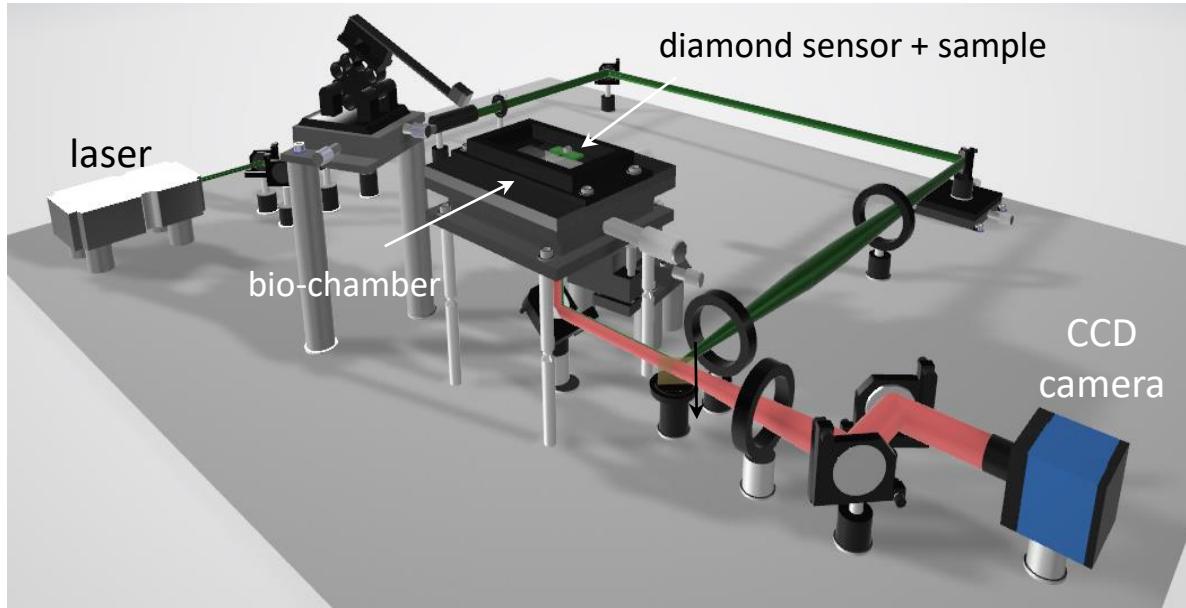


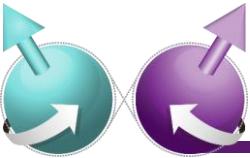
## Imaging magnetic domains in twisted CrI<sub>3</sub>



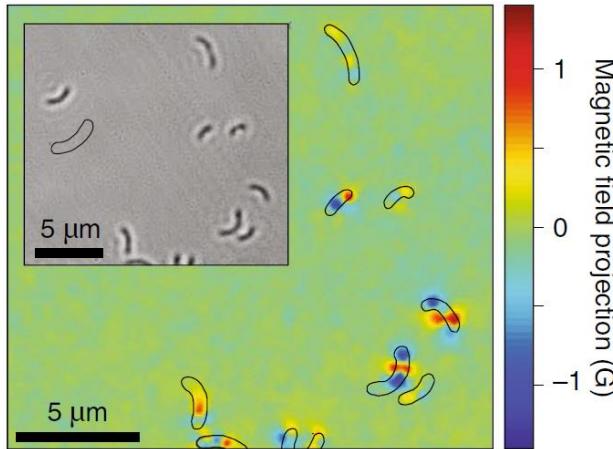


# Imaging with wide-field quantum microscope

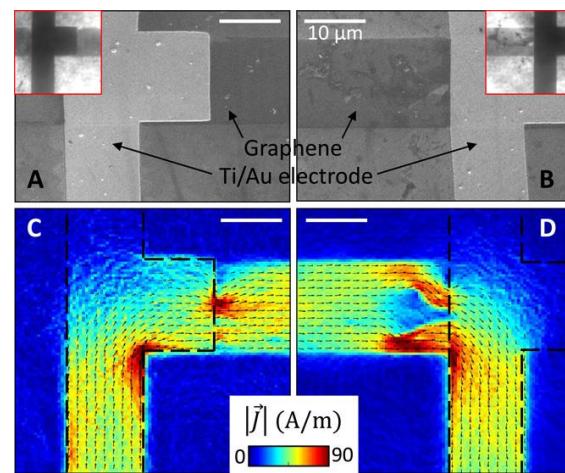




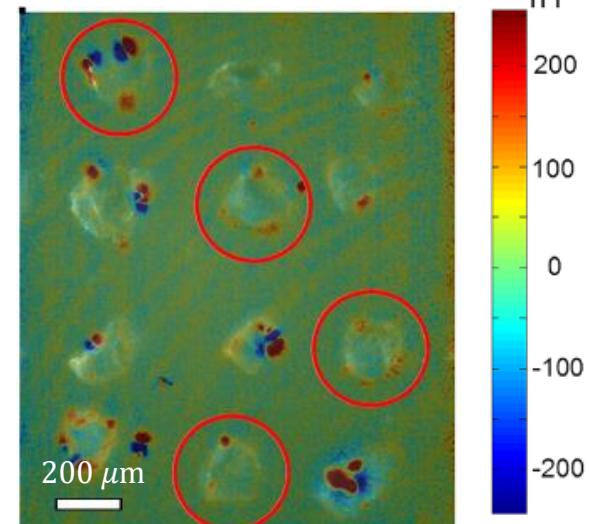
# More imaging examples



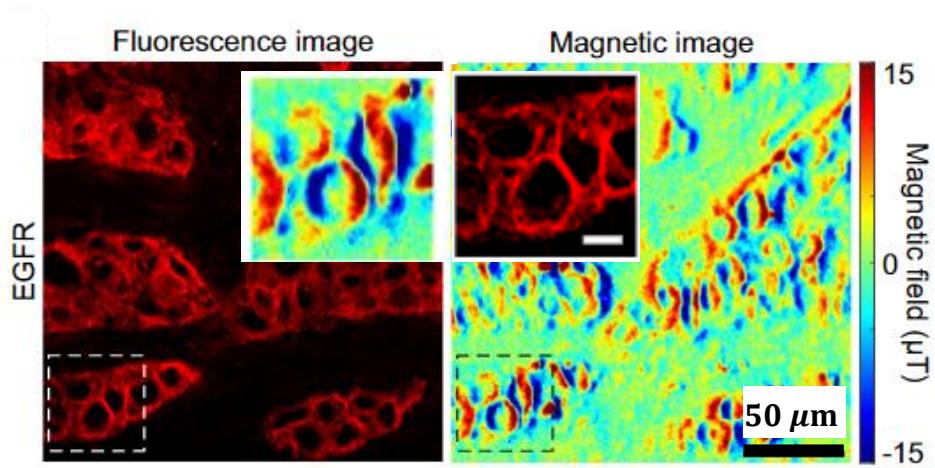
Le Sage et al. Nature (2013)



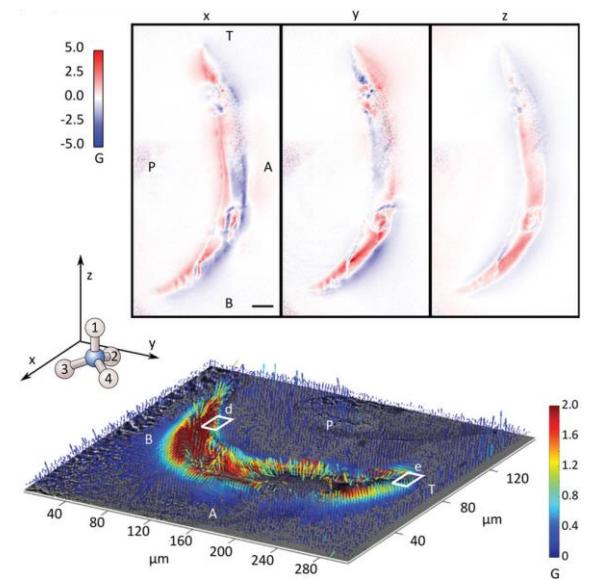
J-T Tetienne et al. Science Advances (2017)



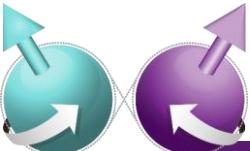
Glenn et. al. Geo. Geophys. Geosys. (2017)



Chen et. al. PNAS (2022)

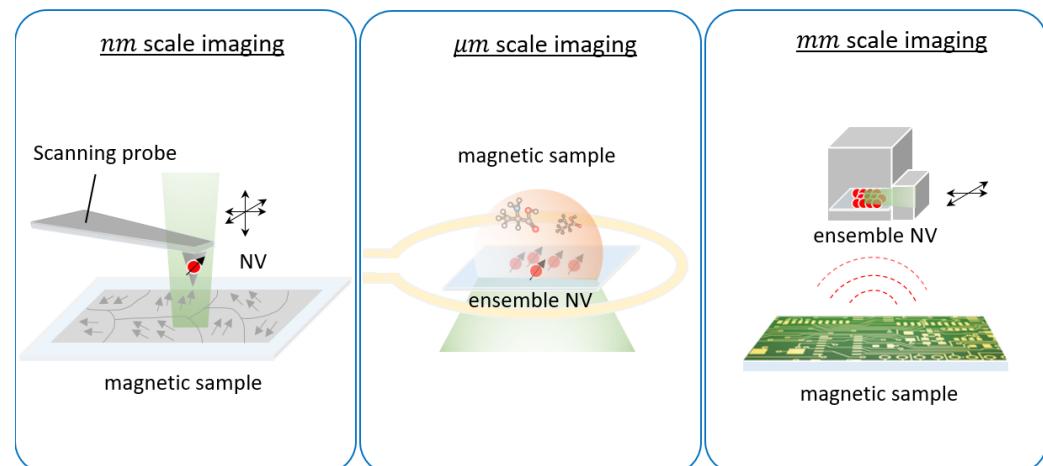
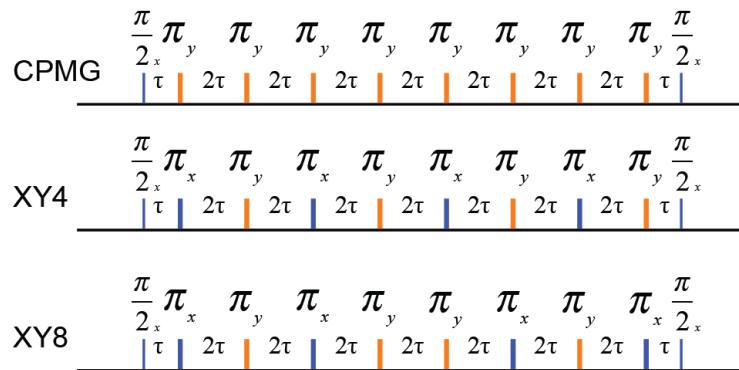


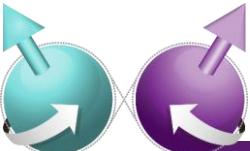
McCoey et. al. Small (2020)



# Summary

- 스피ن 큐비트 기반 양자센싱 원리 (e.g. Ramsey, echo, dynamical decoupling, etc.)
- 다이아몬드 NV 센터 소개
- NV 센터 기반 양자 센싱 소개
- NV 센터 기반 양자 이미징 소개





# Summary

- Quantum sensing, quantum metrology (양자센싱, 양자계측)
- 측정은 모든 물리 실험의 기본
- 양자센싱 및 이미징은 양자현상에 기반한 물리 실험의 새로운 방법론 제공
- 중시계 등 다양한 기초·응용 물리 실험에 활용 가능

