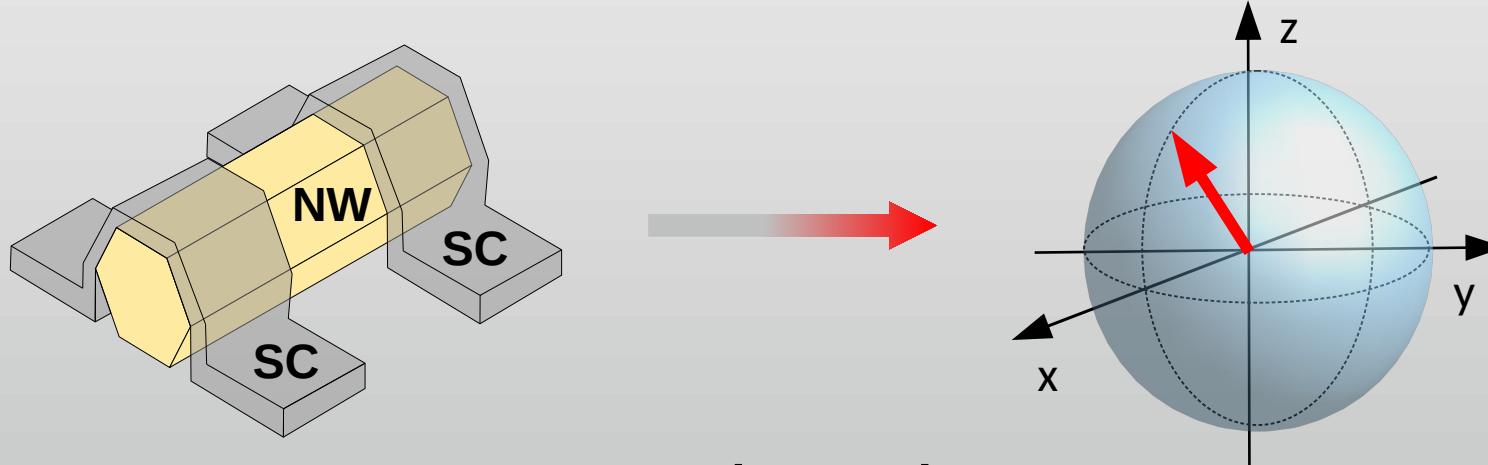


# Nanowire-Based Quantum Devices

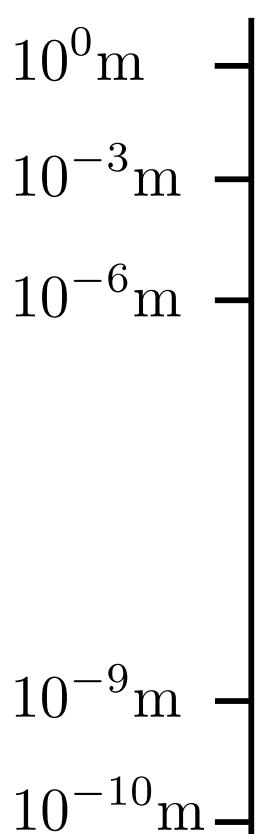


Sunghun Park

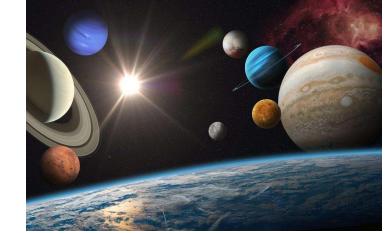
Center for Theoretical Physics of Complex Systems

Institute for Basic Science, Daejeon, Korea

# Macroscopic quantum mechanics

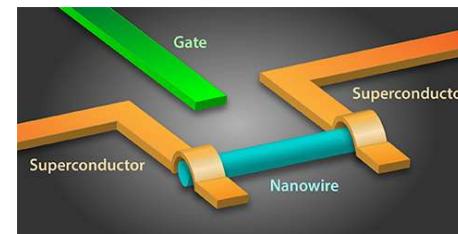
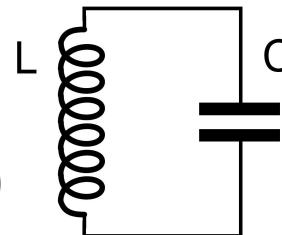


**Macroscopic  
(Classical)**

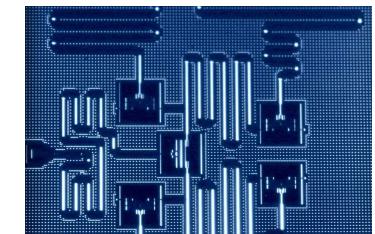


GETTY

**Mesoscopic  
(Artificial atoms,  
Quantum devices)**

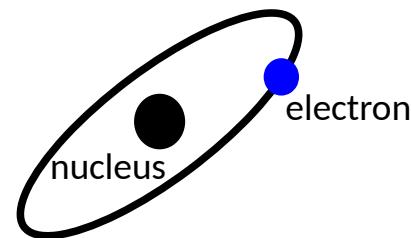
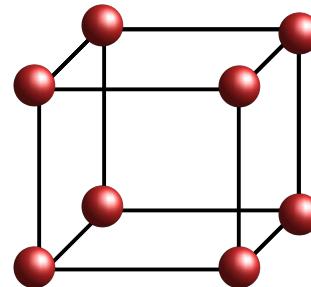


APS/Alan Stonebraker



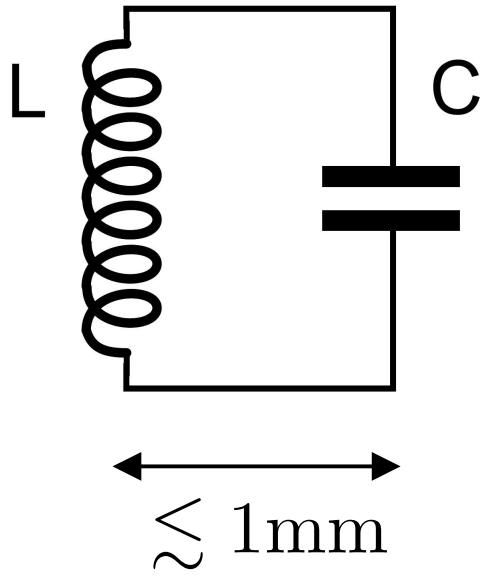
IBM

**Microscopic  
(Quantum)**



# Quantum LC resonator

---



Lumped element

$$L = 1 \text{ nH}, \quad C = 10 \text{ pF}$$

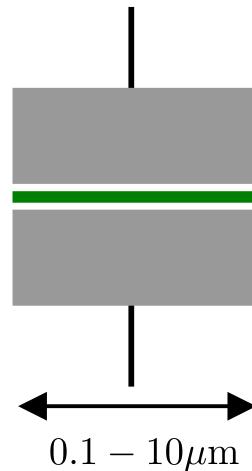
cf. electrical components:

$$L_e = 1\mu\text{H} - 1\text{mH}, \quad C_e = 1\mu\text{F} - 1\text{mF}$$

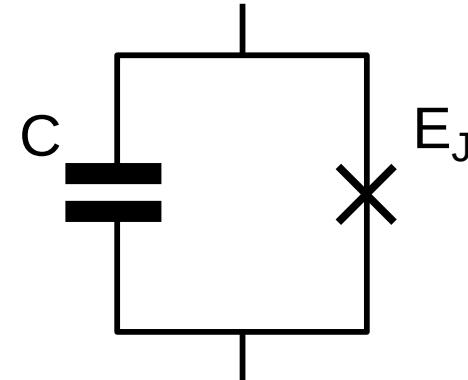
$$f_r = \frac{1}{2\pi\sqrt{LC}} \simeq 1.6 \text{ GHz}$$

$$\text{Wavelength } \lambda \simeq 20 \text{ cm}$$

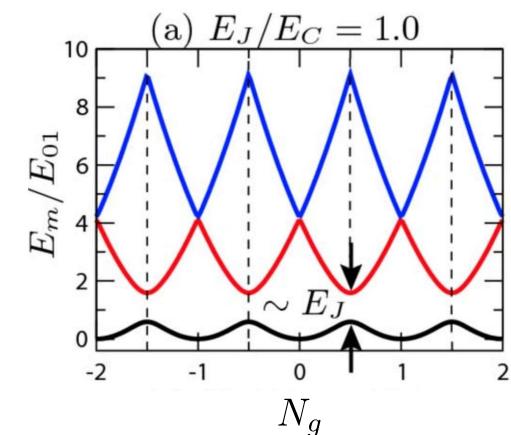
# Josephson tunnel junction



Superconductor 1  
Insulator  
Superconductor 2



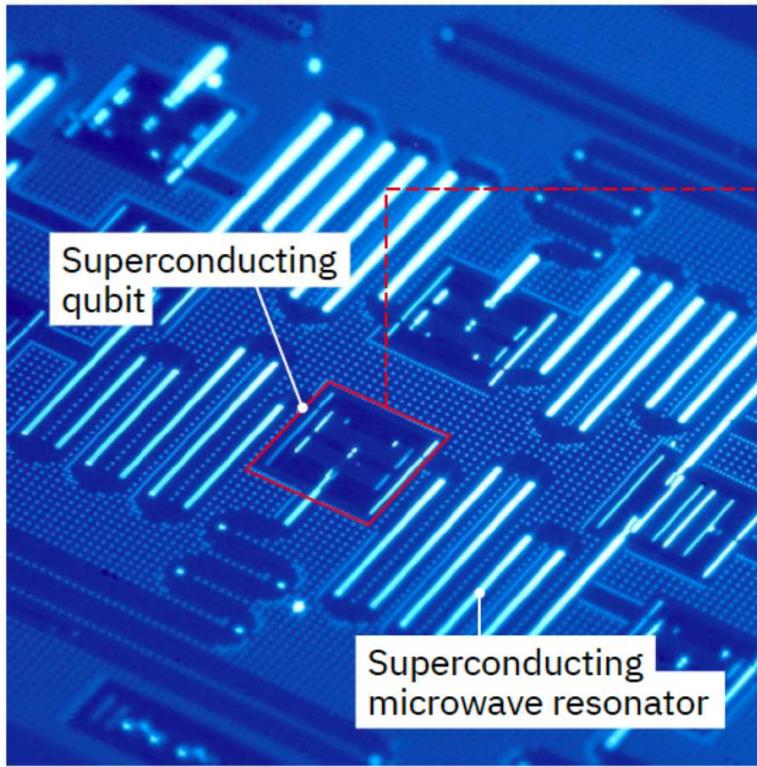
$$\begin{aligned} H &= \sum_N 4E_C(\hat{N} - N_g)^2 - E_J \cos \hat{\varphi} \\ &= \sum_N 4E_C(\hat{N} - N_g)^2 - \frac{E_J}{2} (|N\rangle\langle N+1| + |N+1\rangle\langle N|) \\ E_C &= \frac{e^2}{2C}, \quad E_J = \frac{\hbar}{8e^2} G_t \Delta \end{aligned}$$



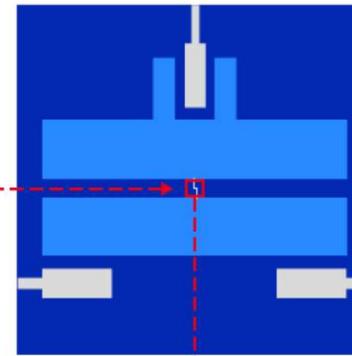
# A superconducting quantum processor at IBM

---

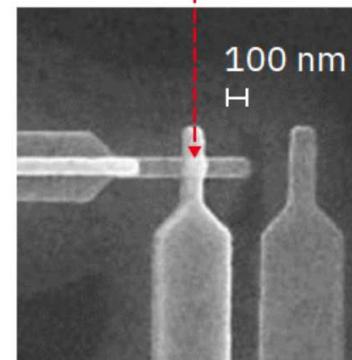
Quantum processor chip



600  $\mu\text{m}$



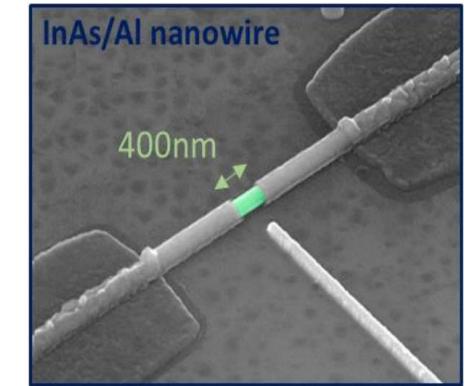
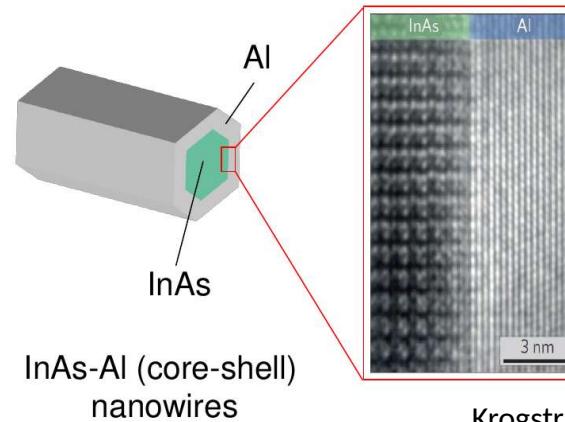
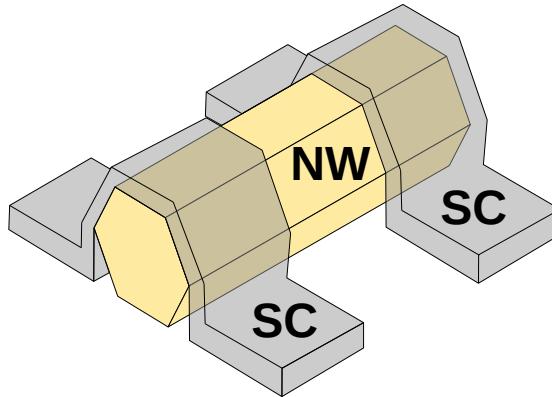
Super-conducting qubit



Josephson junction

# Nanowire Josephson junction

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Krogstrup et al., Nature Materials 14, 400 (2015)  
Goffman et al., New J. Phys. 19, 092002 (2017)

## Goal of the research

- Understanding the **physics of Andreev bound states** in nanowire Josephson junctions
- Maximizing the advantages and strengths of the nanowire-superconductor **hybrid** systems

# Outline

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Part I. Nanowire Josephson junction

Part II. Josephson junction coupled to a microwave

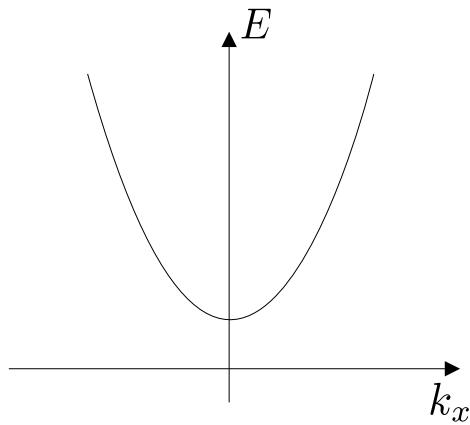
Part III. Overview of recent studies

## **Part I. Nanowire Josephson junction**

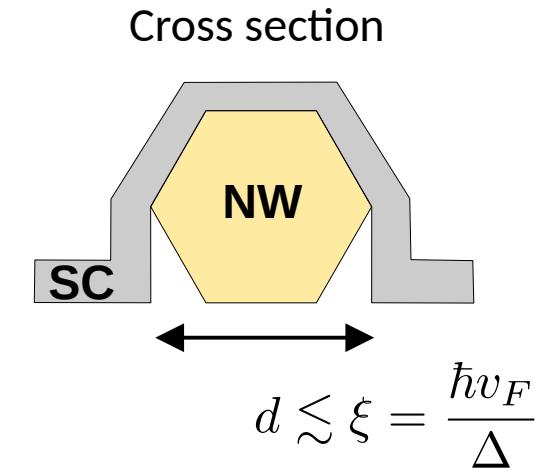
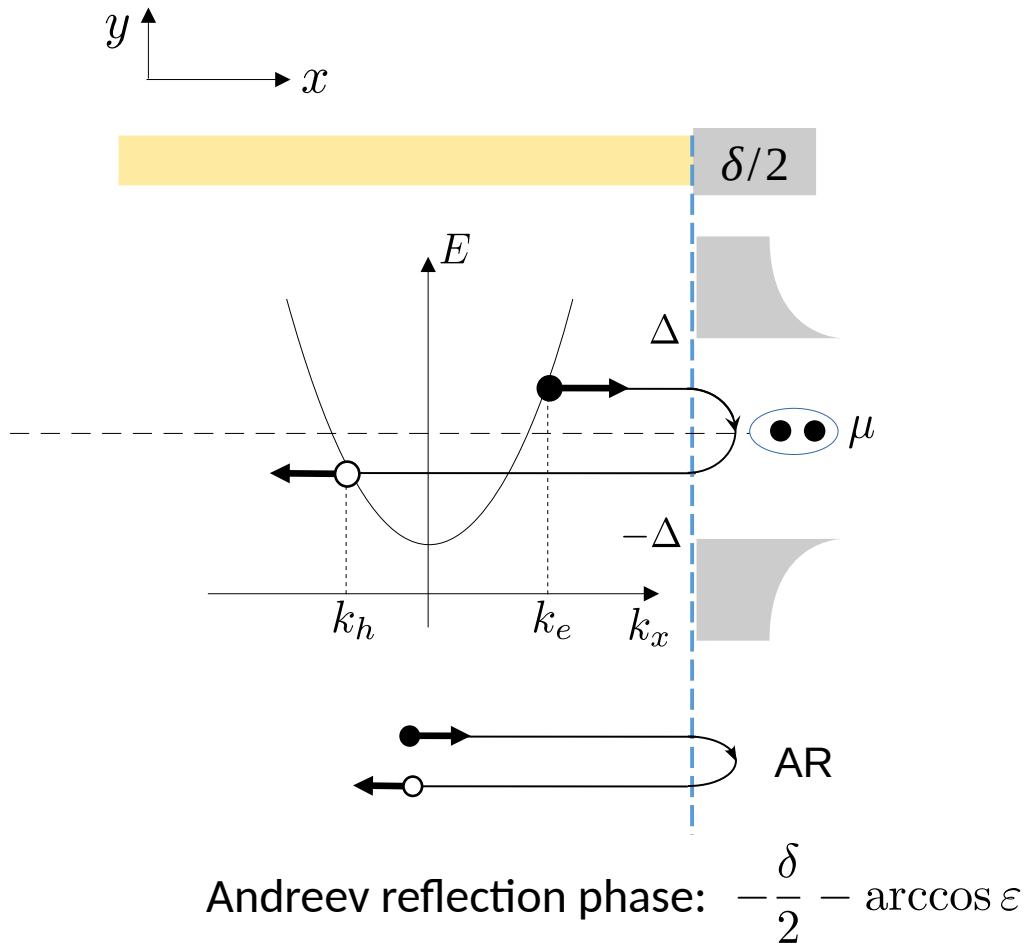
- Andreev reflections
- Andreev bound states
- Effect of scattering and spin-orbit coupling

# A single band

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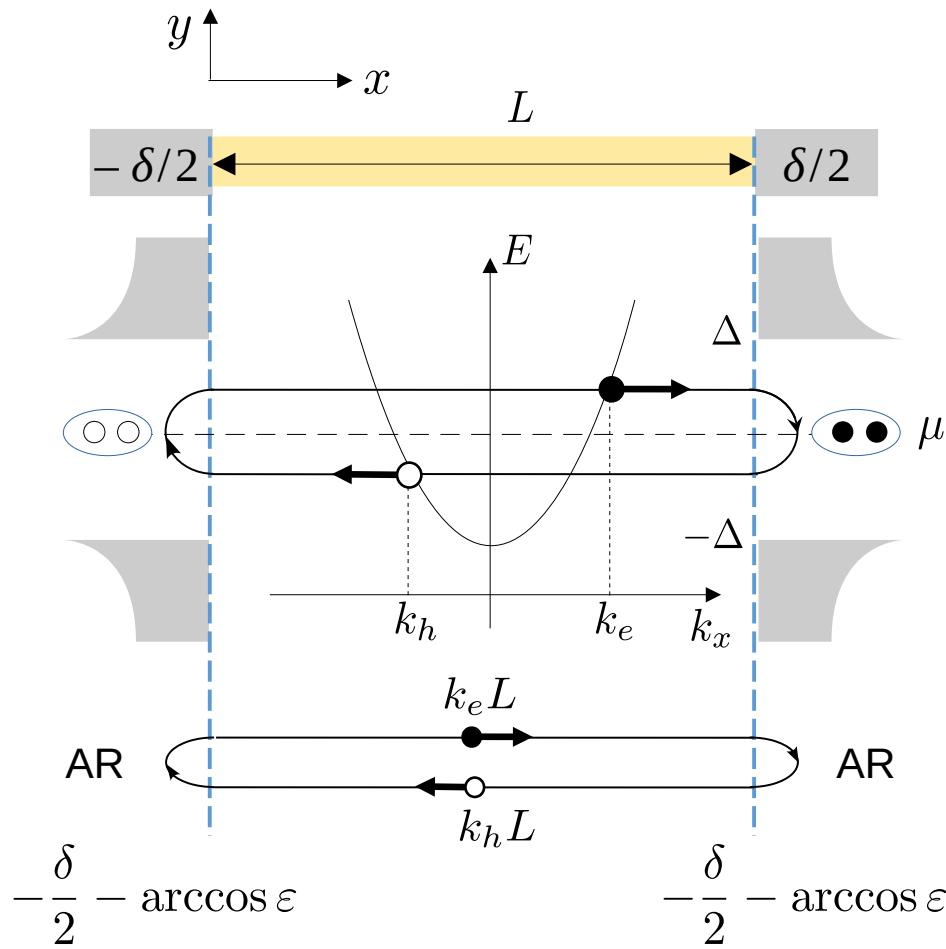
# Andreev reflection



Superconducting proximity effect

$$\varepsilon = \frac{E - \mu}{\Delta}$$

# Ballistic channel



$$k_e = k_F + \frac{E - \mu}{\hbar v_F}, \quad k_h = -k_F + \frac{E - \mu}{\hbar v_F}$$

Dynamical phase

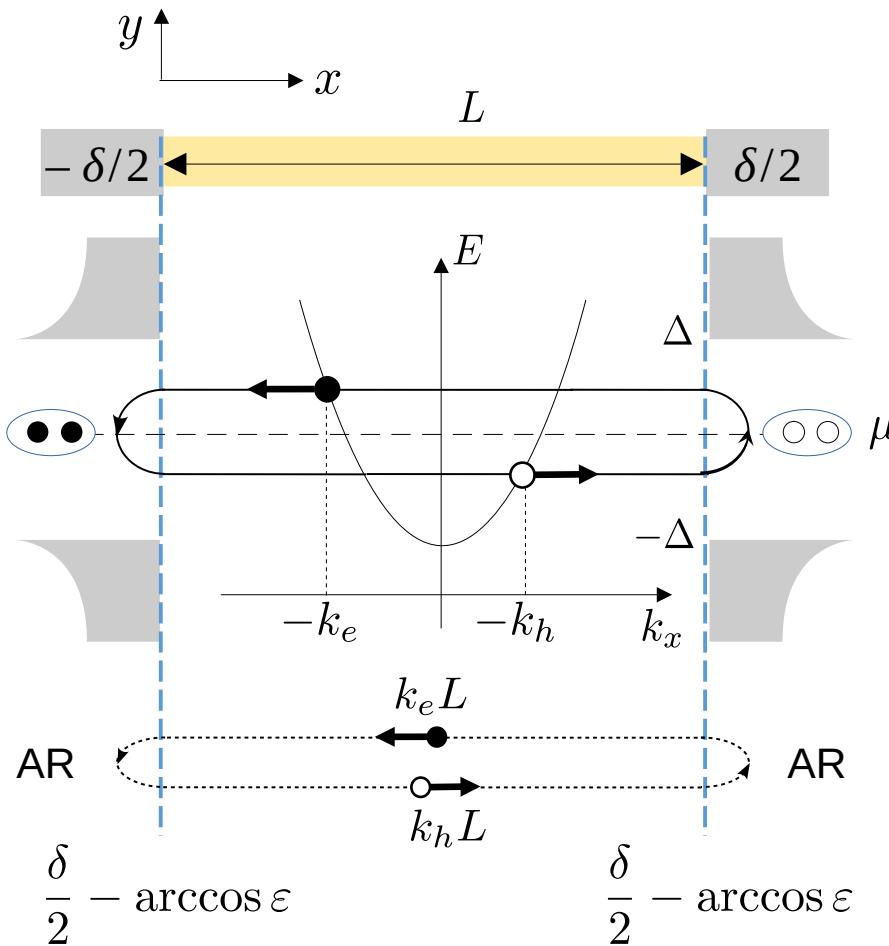
$$k_e L + k_h L = 2\lambda\varepsilon$$

$$\lambda = \frac{L\Delta}{\hbar v_F} = \frac{L}{\xi}$$

Energy quantization condition

$$-\delta - 2\arccos \varepsilon + 2\lambda\varepsilon = 2\pi n$$

# Ballistic channel



$$k_e = k_F + \frac{E - \mu}{\hbar v_F}, \quad k_h = -k_F + \frac{E - \mu}{\hbar v_F}$$

Dynamical phase

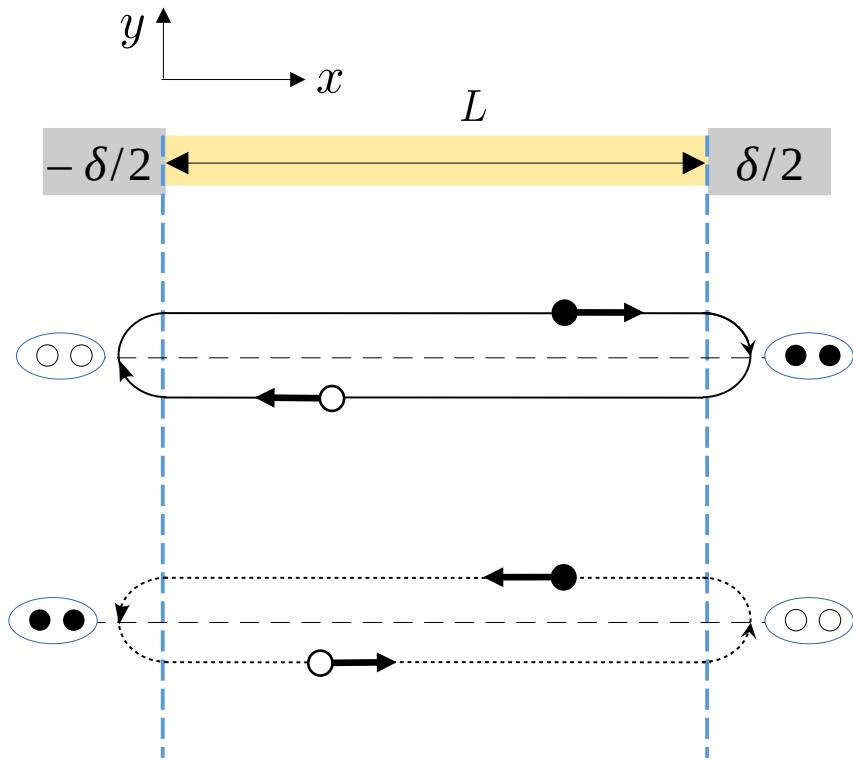
$$k_e L + k_h L = 2\lambda\varepsilon$$

$$\lambda = \frac{L\Delta}{\hbar v_F} = \frac{L}{\xi}$$

Energy quantization condition

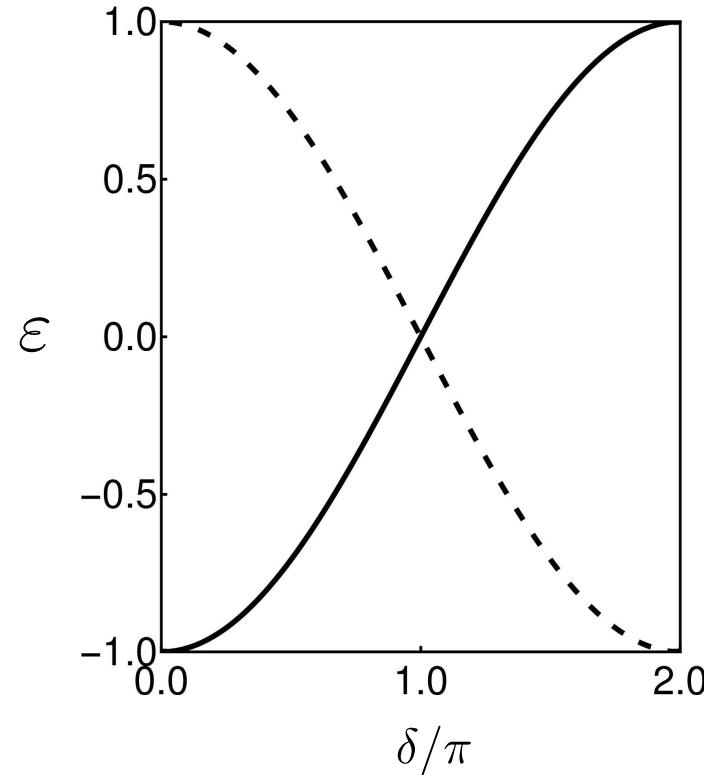
$$\delta - 2\arccos \varepsilon + 2\lambda\varepsilon = 2\pi n$$

# Andreev bound states – ballistic case



$$\mp\delta - 2\arccos\varepsilon + 2\lambda\varepsilon = 2\pi n$$

$$\lambda = L/\xi = 0$$

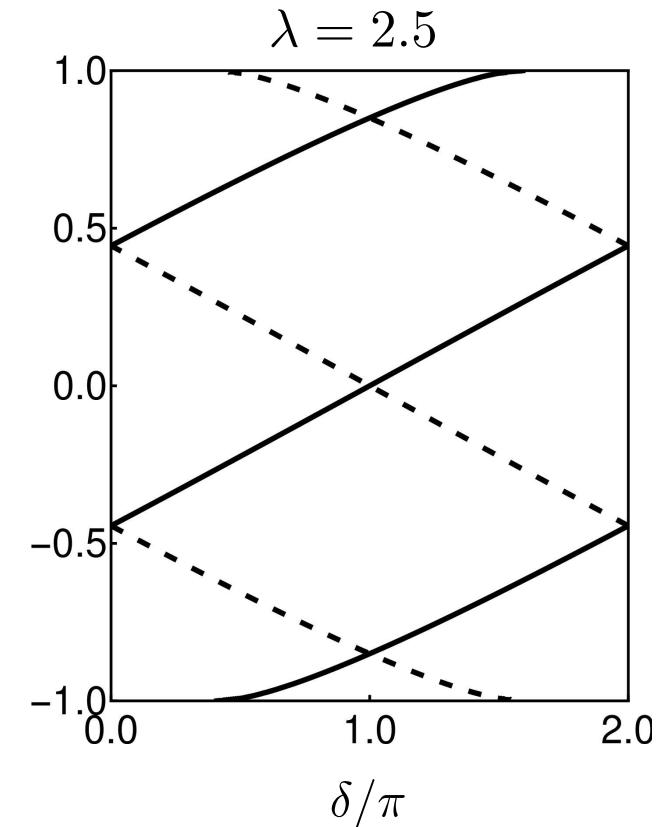
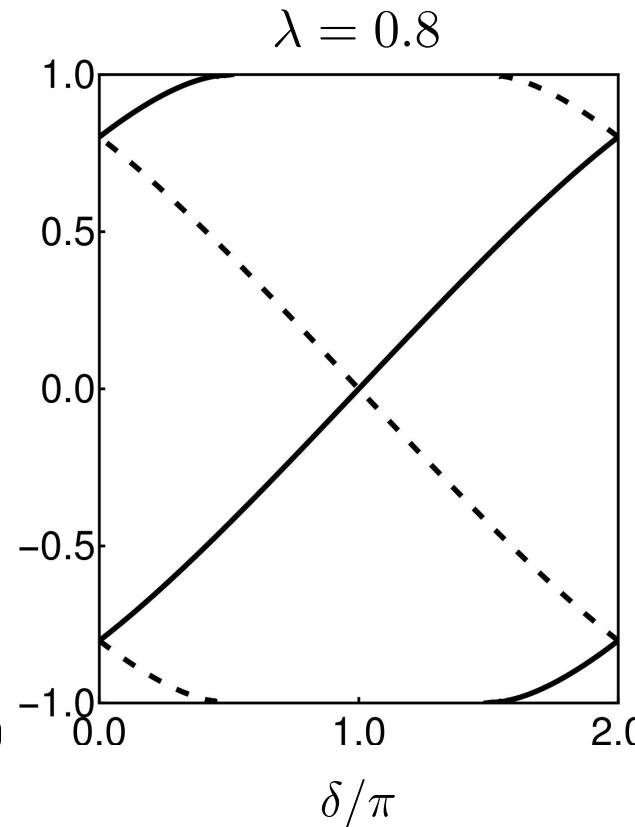
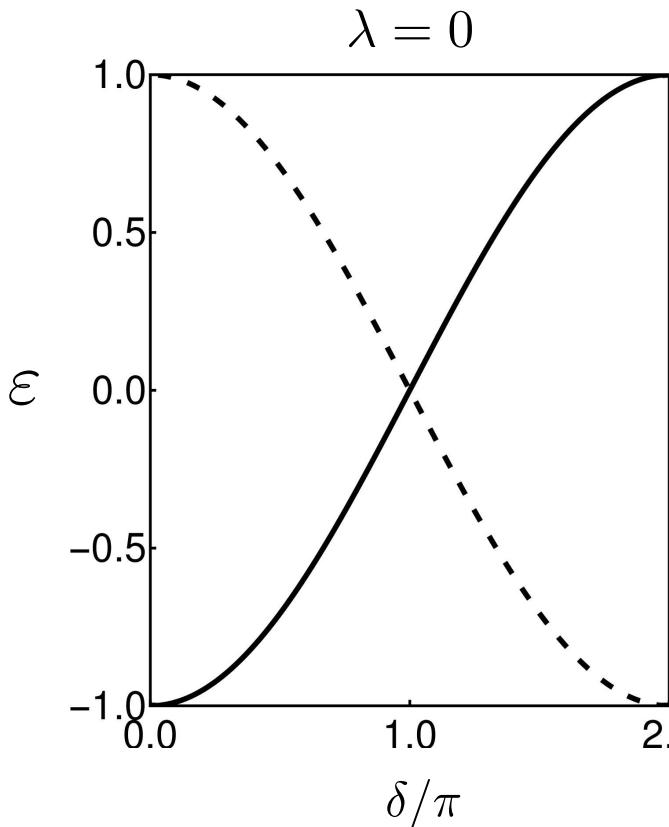


Bagwell, PRB 46, 12573 (1992)  
Beenakker and Houten, PRL 66, 3056 (1991)  
Kulik, JETP 30, 944 (1970)

# Andreev energies from short to long junction length

$$\lambda = \frac{L\Delta}{\hbar v_F}$$

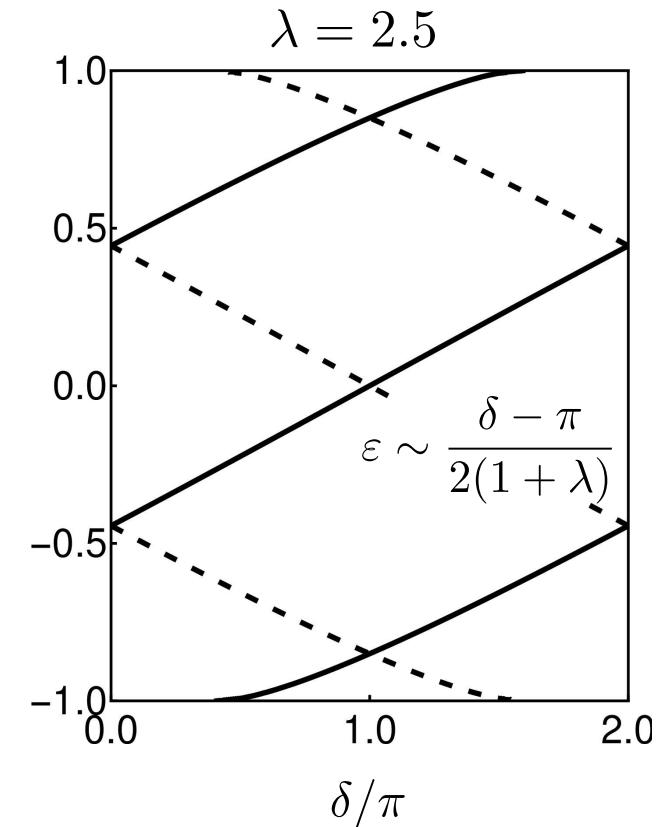
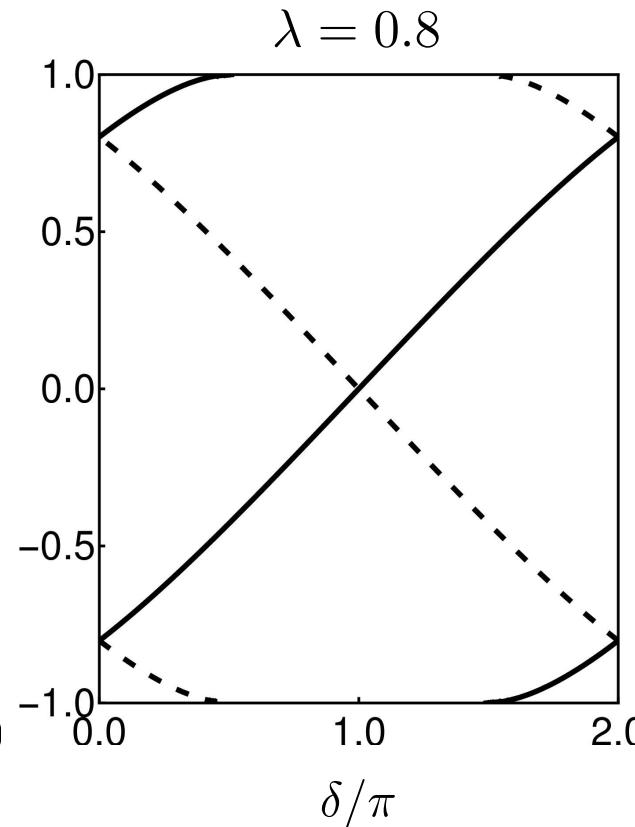
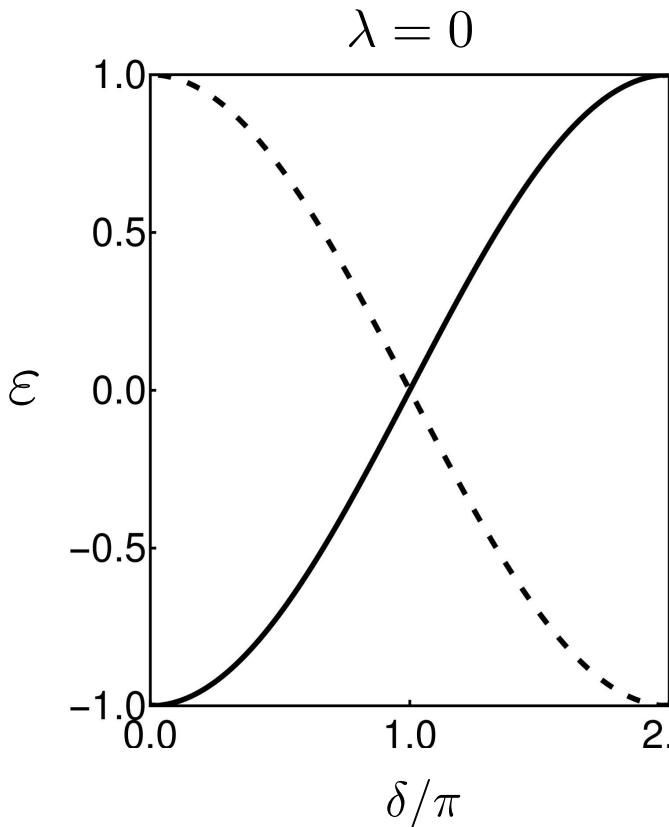
$$\mp\delta - 2\arccos\varepsilon + 2\lambda\varepsilon = 2\pi n$$



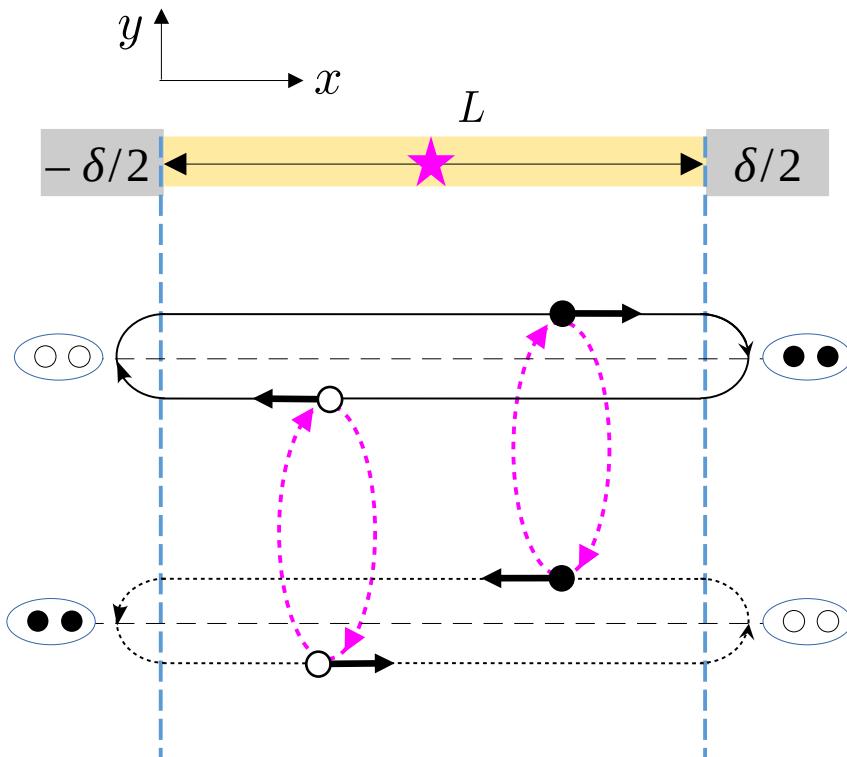
# Andreev energies from short to long junction length

$$\lambda = \frac{L\Delta}{\hbar v_F}$$

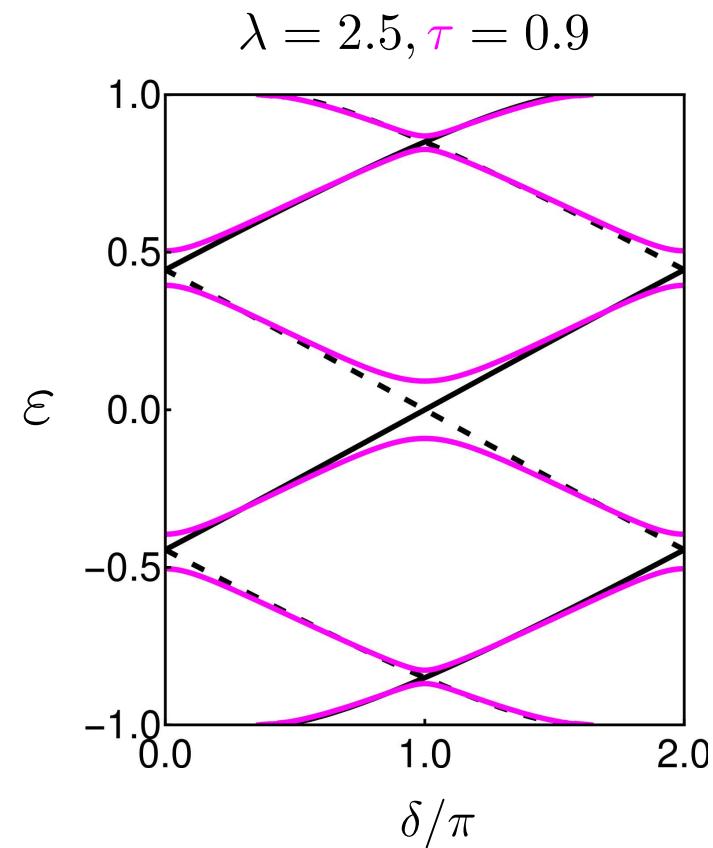
$$\mp\delta - 2\arccos\varepsilon + 2\lambda\varepsilon = 2\pi n$$



# Andreev bound states with scatterer



$$\cos(2\arccos \varepsilon - 2\lambda\varepsilon) = \tau \cos(\delta) + (1-\tau)\cos(2\lambda\varepsilon x_r)$$

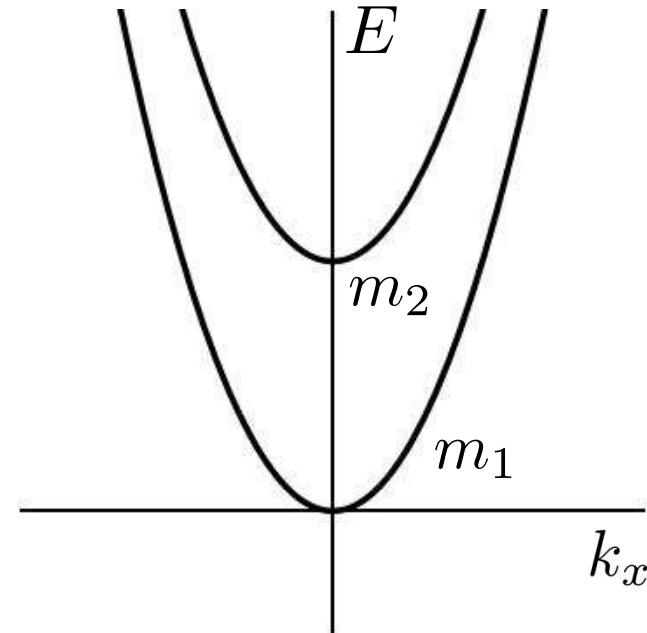
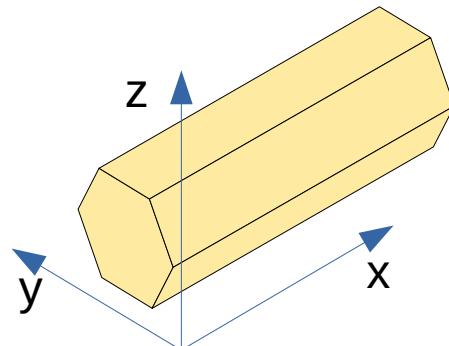


# Rashba spin-orbit effect

---

$$\underline{H_{NW} = \frac{p_x^2}{2m} + \frac{p_y^2 + p_z^2}{2m} + U_c(y, z) - \alpha p_x \sigma_y + \alpha p_y \sigma_x}$$

Nanowire (InAs or InSb)



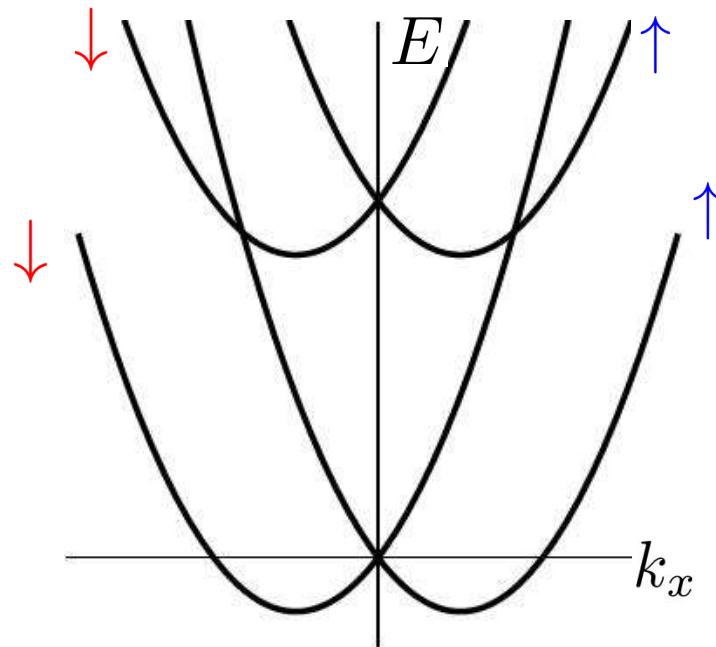
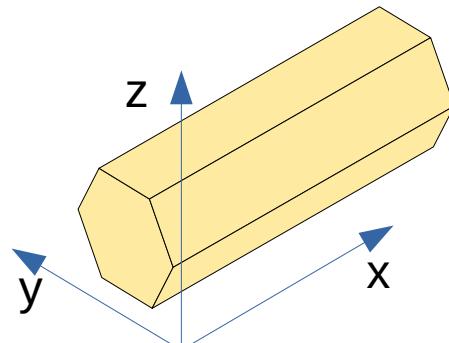
Measurement of the SOC: Fasth et al., PRL 98, 266801 (2007)

# Rashba spin-orbit effect

---

$$H_{NW} = \frac{p_x^2}{2m} + \frac{p_y^2 + p_z^2}{2m} + U_c(y, z) \boxed{-\alpha p_x \sigma_y + \alpha p_y \sigma_x}$$

Nanowire (InAs or InSb)

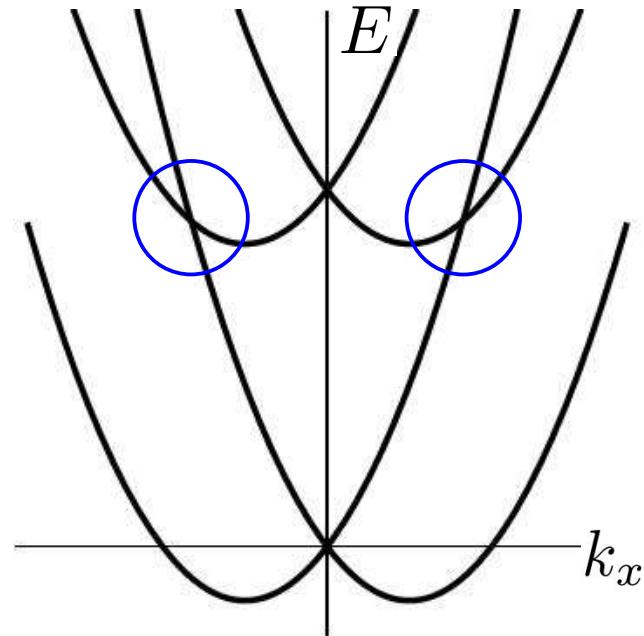
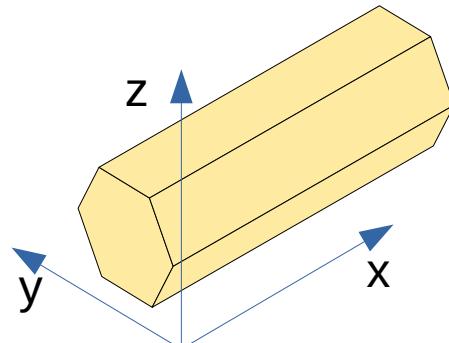


# Rashba spin-orbit effect

---

$$H_{NW} = \frac{p_x^2}{2m} + \frac{p_y^2 + p_z^2}{2m} + U_c(y, z) - \alpha p_x \sigma_y + \boxed{\alpha p_y \sigma_x}$$

Nanowire (InAs or InSb)

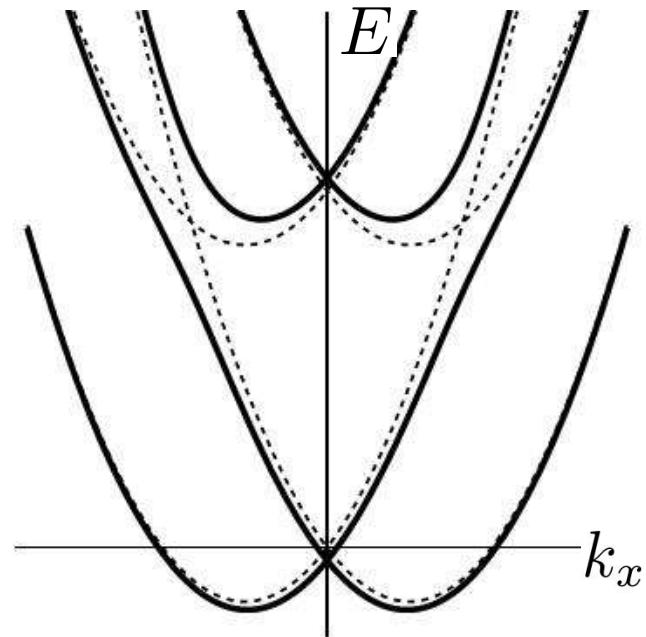
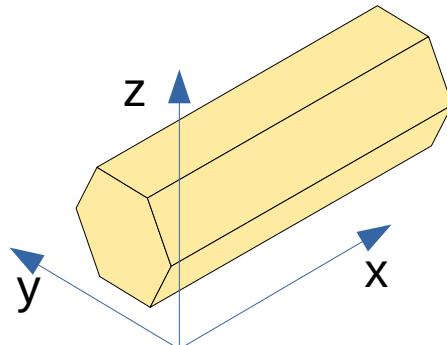


# Rashba spin-orbit effect

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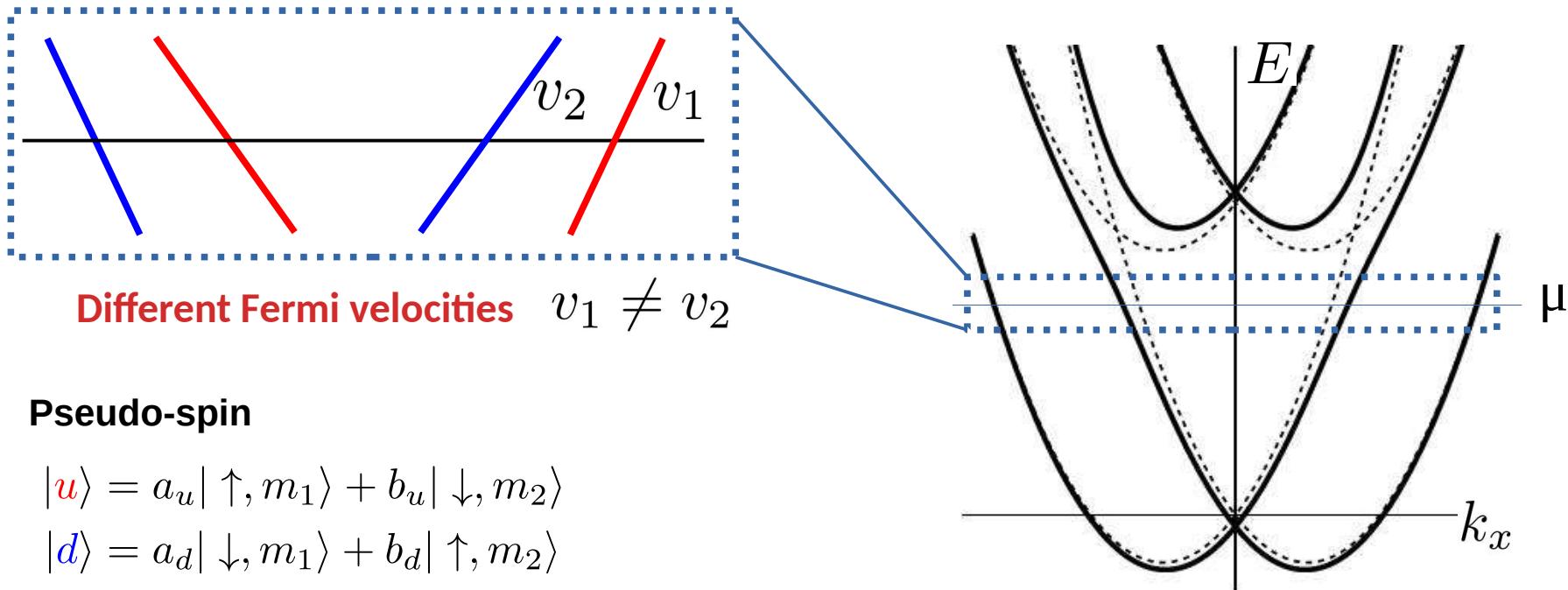
$$H_{NW} = \frac{p_x^2}{2m} + \frac{p_y^2 + p_z^2}{2m} + U_c(y, z) - \alpha p_x \sigma_y + \boxed{\alpha p_y \sigma_x}$$

Nanowire (InAs or InSb)



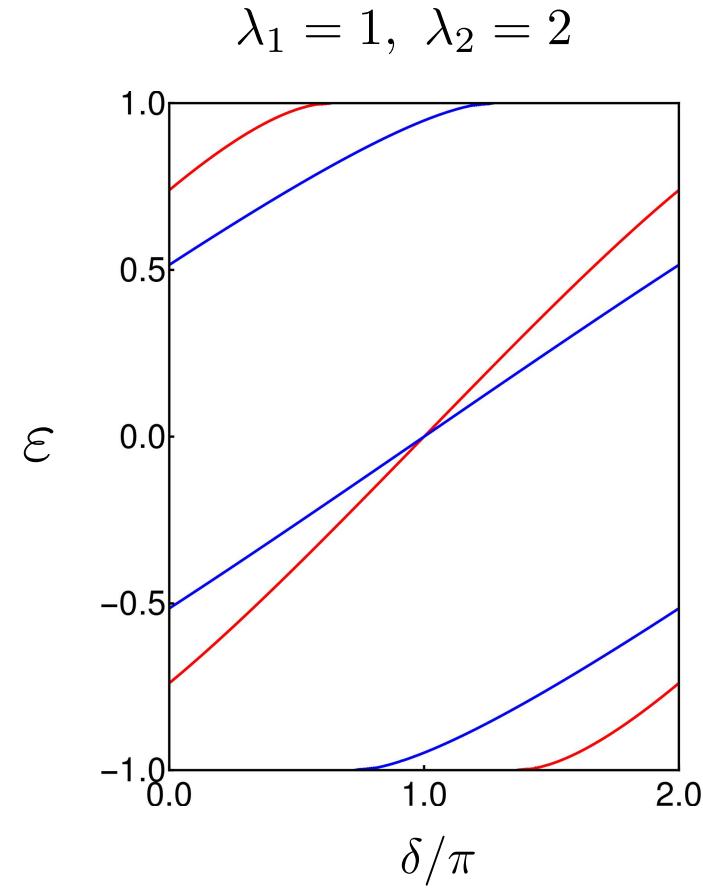
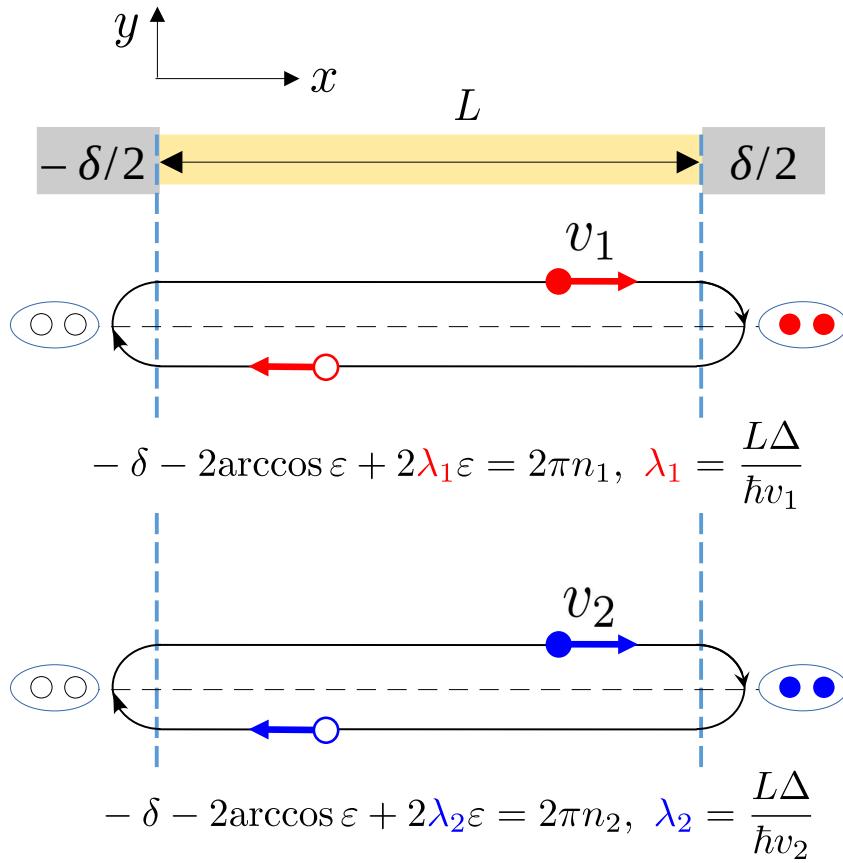
# Rashba spin-orbit effect

$$H_{NW} = \frac{p_x^2}{2m} + \frac{p_y^2 + p_z^2}{2m} + U_c(y, z) - \alpha p_x \sigma_y + \alpha p_y \sigma_x$$

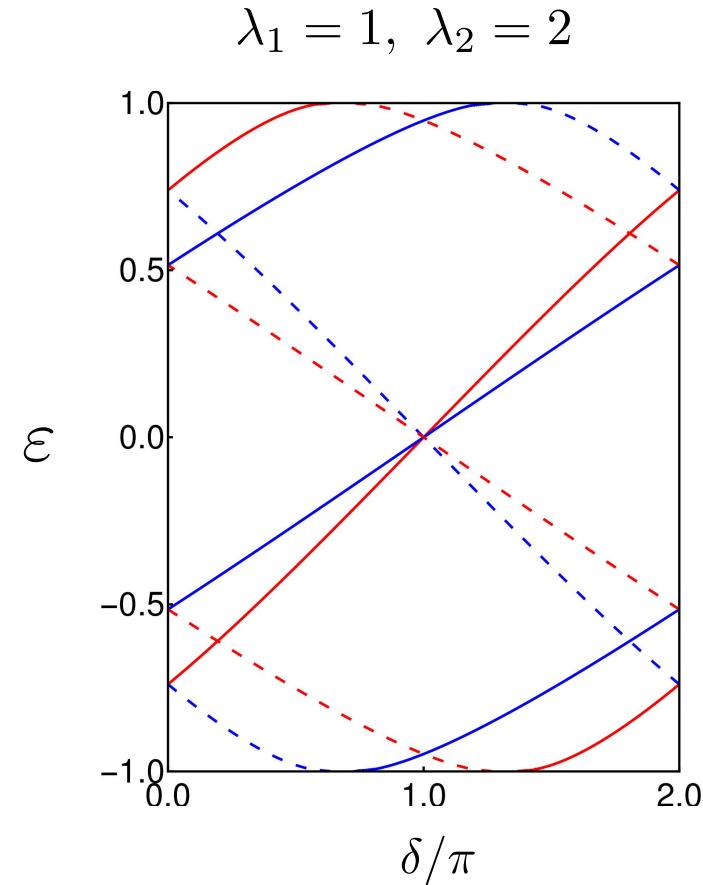
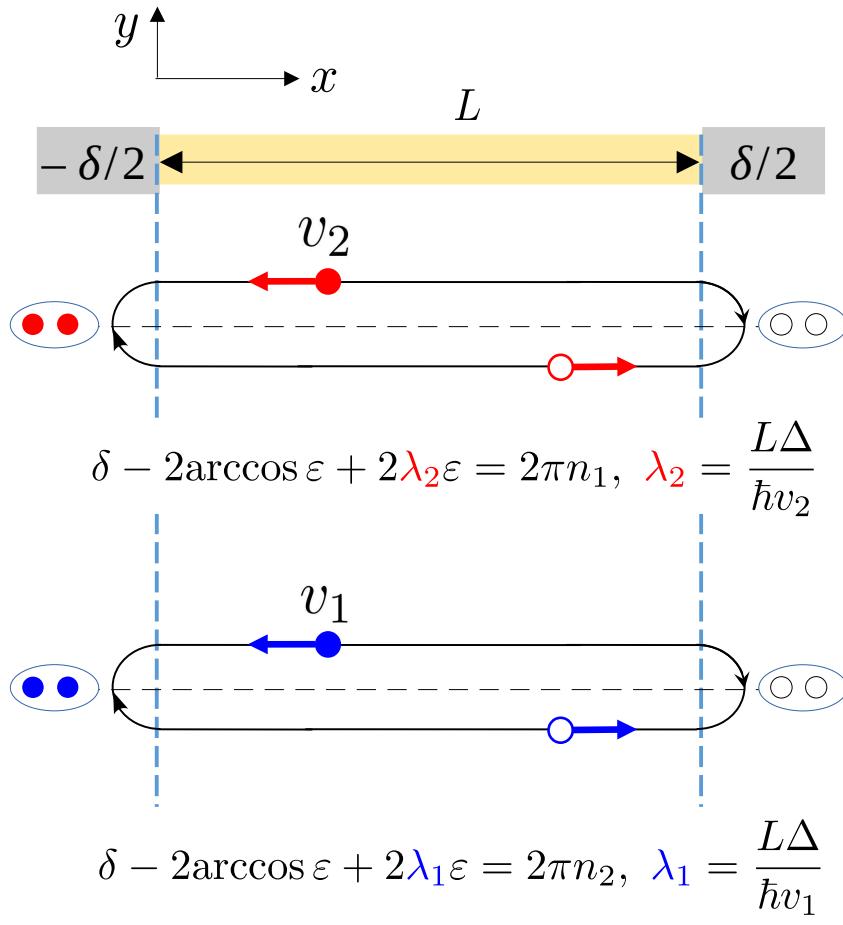


Moroz and Barnes, PRB 60, 14272 (1999)

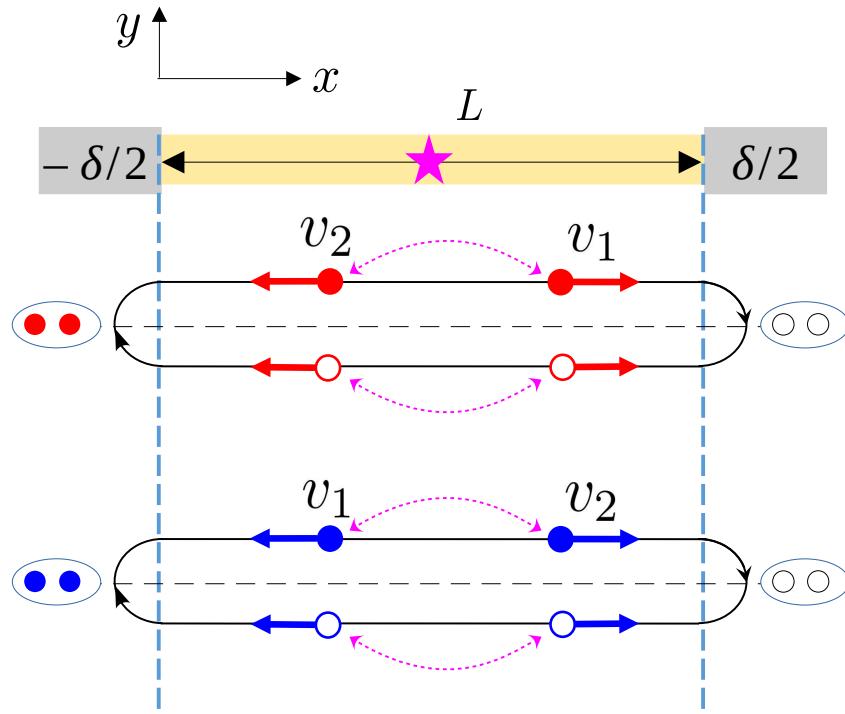
# Spin-split Andreev levels - ballistic channel



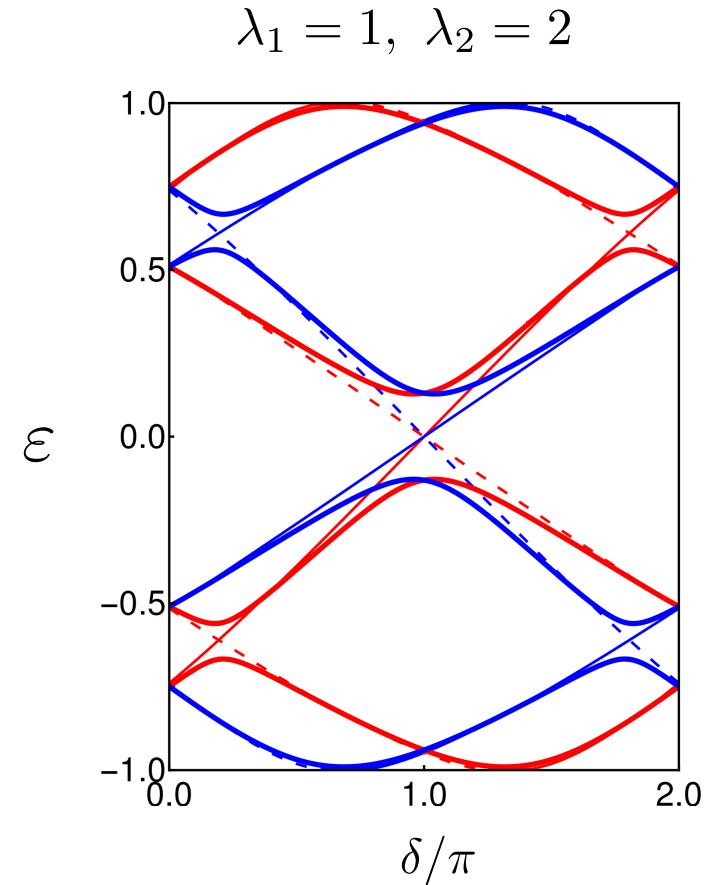
# Spin-split Andreev levels - ballistic channel



# Spin-split Andreev levels with scatterer



$$\begin{aligned} \tau \cos [(\lambda_1 - \lambda_2)\varepsilon \mp \delta] + (1 - \tau) \cos [(\lambda_1 + \lambda_2)\varepsilon x_r] \\ = \cos [2\arccos \varepsilon - (\lambda_1 + \lambda_2)\varepsilon] \end{aligned}$$

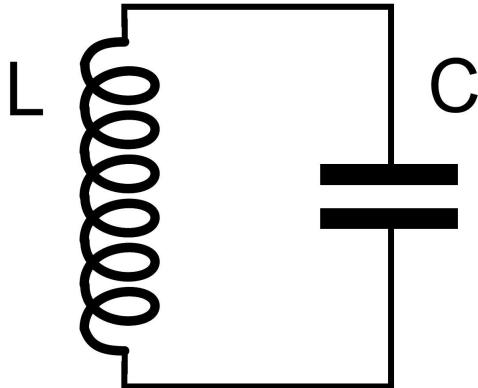


## **Part II. Josephson junction coupled to a microwave**

- Coherent coupling
- Readout: state-dependent frequency shift

# Superconducting LC resonator

---



$$H_r = \frac{\hat{Q}^2}{2C} + \frac{\hat{\Phi}^2}{2L}$$
$$= hf_r \left( a^\dagger a + \frac{1}{2} \right)$$

$$\hat{Q} = -i\sqrt{\frac{\hbar}{2}}\sqrt{\frac{C}{L}}(a - a^\dagger), \quad \hat{\Phi} = \sqrt{\frac{\hbar}{2}}\sqrt{\frac{L}{C}}(a + a^\dagger)$$

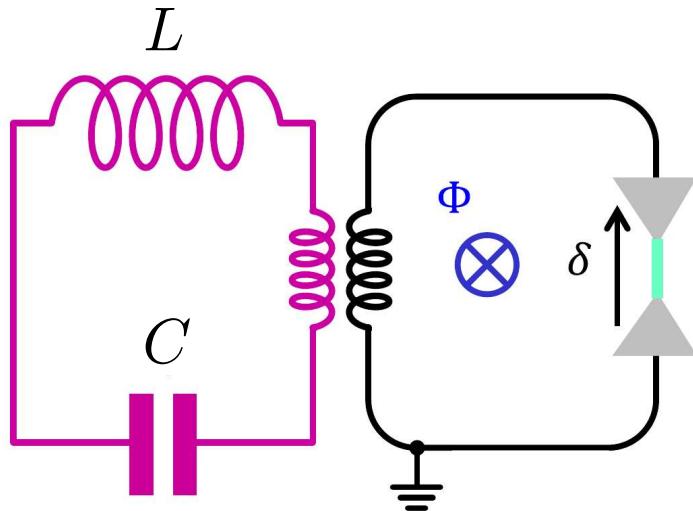
$$f_r = \frac{1}{2\pi\sqrt{LC}}$$

Quantum fluctuation

$$\langle (\Delta Q)^2 \rangle \langle (\Delta \Phi)^2 \rangle \geq \frac{\hbar^2}{4}$$

# Resonator-coupled Josephson junction

---



$$H_J(\delta) \rightarrow H_J(\delta + \hat{\delta}_r)$$
$$\hat{\delta}_r = \delta_{ZP}(a + a^\dagger)$$

$$H = H_r + H_J(\delta) + \delta_{ZP} \frac{dH_J(\delta)}{d\delta} (a + a^\dagger) + \frac{\delta_{ZP}^2}{2} \frac{d^2H_J(\delta)}{d\delta^2} (a + a^\dagger)^2$$

---

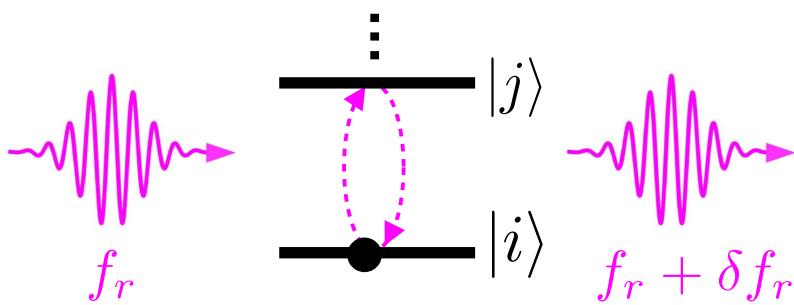
First order

Second order

# Frequency shift of the resonator

---

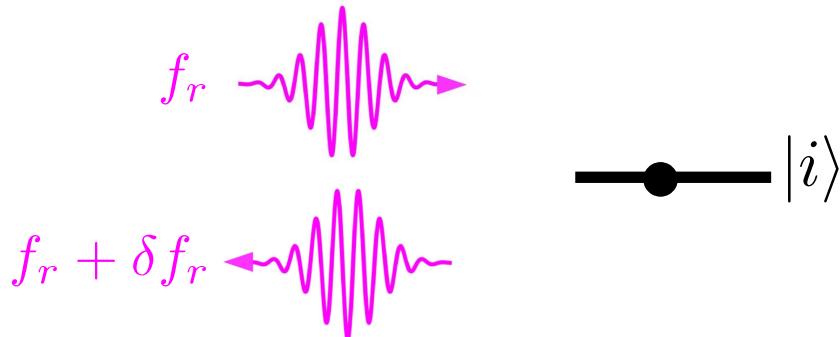
First order coupling contribution



Dominant if  $E_j - E_i \sim h f_r$

$$\delta f_r = \delta_{ZP}^2 \frac{|\langle i | dH_J(\delta)/d\delta | j \rangle|^2}{E_j - E_i - h f_r}$$

Second order coupling contribution

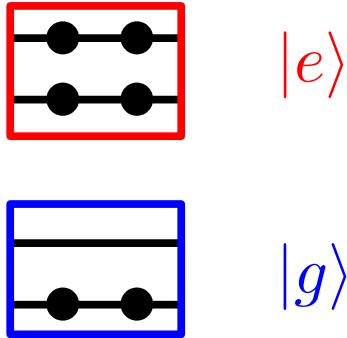
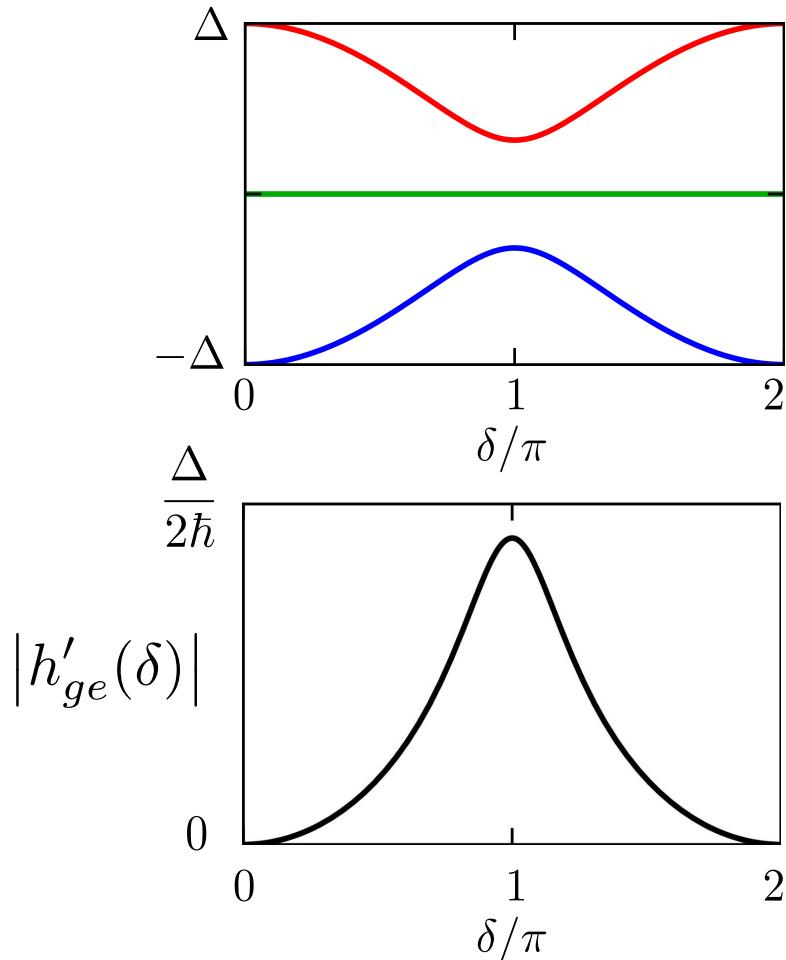


Dominant if  $|E_j - E_i| \gg h f_r$

$$\delta f_r = \delta_{ZP}^2 \frac{d^2 E_i(\delta)}{h d\delta^2} = \delta_{ZP}^2 \frac{1}{h} \frac{(h/2e)^2}{L_J}$$

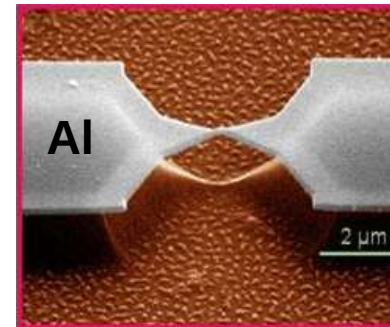
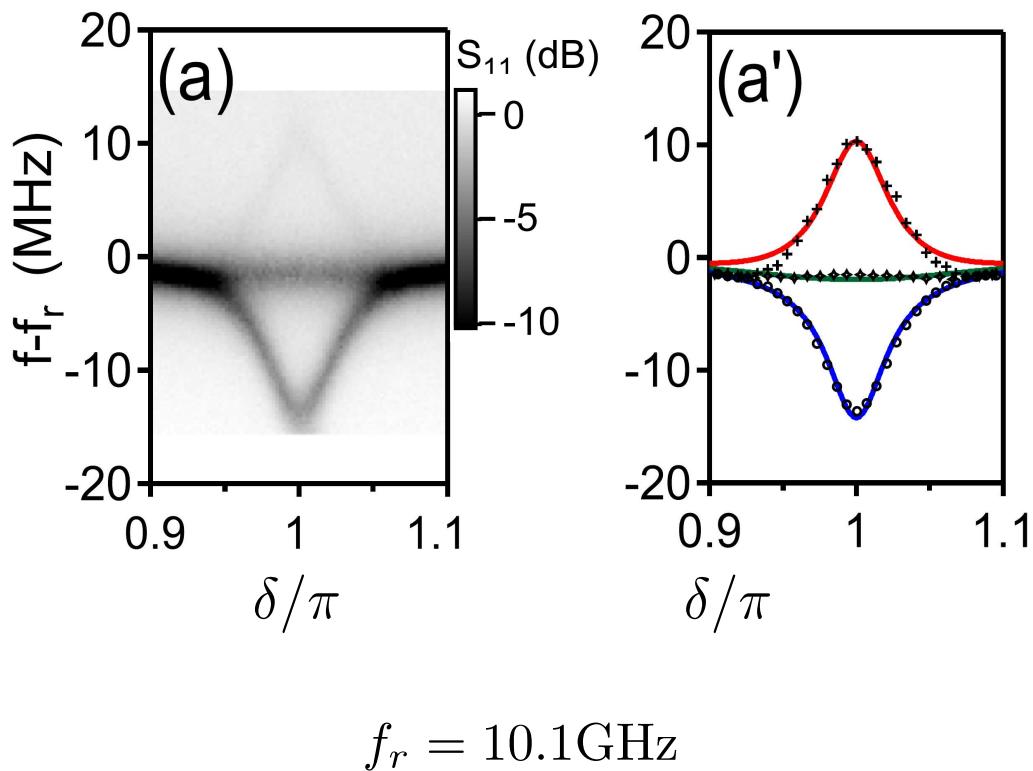
# State-dependent frequency shift - short Josephson junction

---



$$\begin{aligned} h'_{ge}(\delta) &= \langle g \left| \frac{dH(\delta)}{d\delta} \right| e \rangle \\ &= \frac{\Delta \tau \sqrt{1 - \tau} \sin^2(\delta/2)}{2 \sqrt{1 - \tau \sin^2(\delta/2)}} \end{aligned}$$

# State-dependent frequency shift - short Josephson junction



$$|e\rangle : f - f_r \approx \delta_{ZP}^2 \frac{|h'_{ge}|^2}{E_e - (E_g + h f_r)}$$

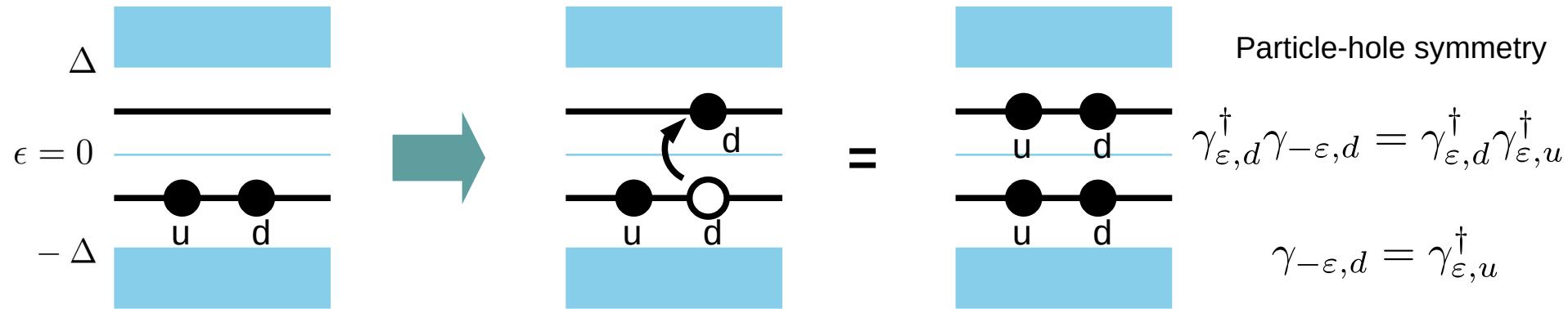
$$|g\rangle : f - f_r \approx \delta_{ZP}^2 \frac{|h'_{ge}|^2}{(E_g + h f_r) - E_e}$$

## **Part III. Overview of recent studies**

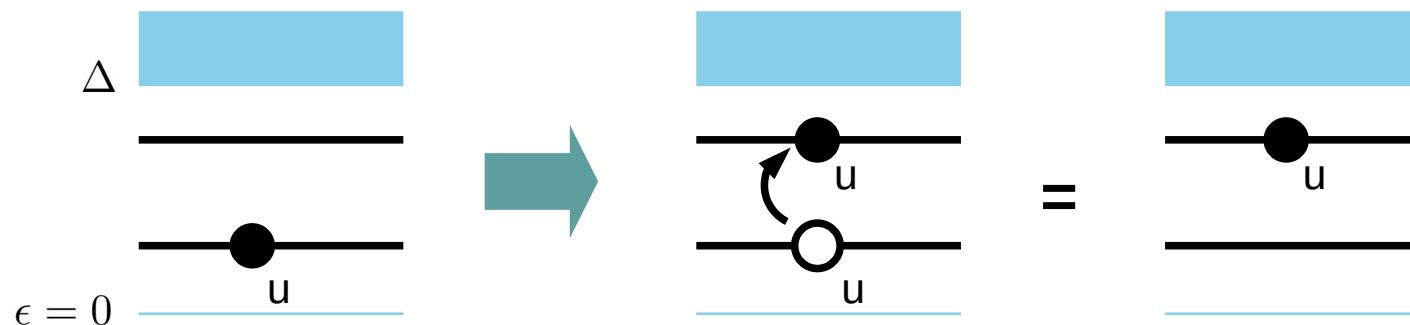
- Spectroscopic study of spin-split ABSs
- Dynamical parity selection using a microwave

# Transitions between Andreev levels by a microwave

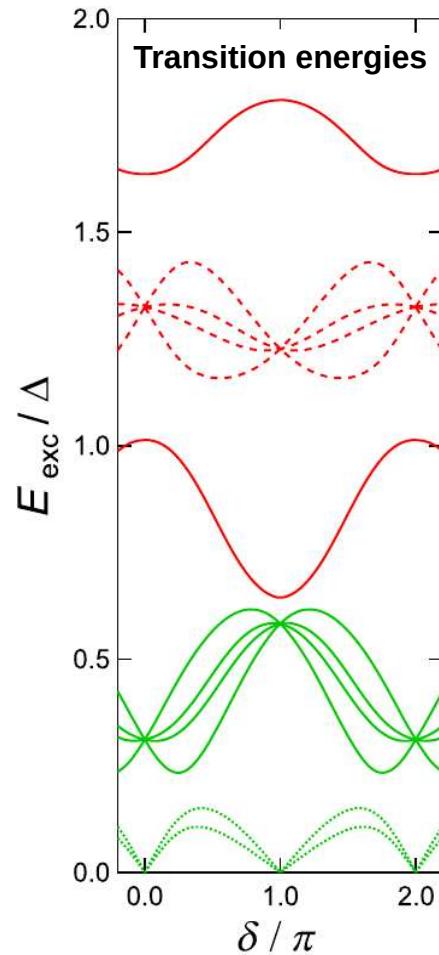
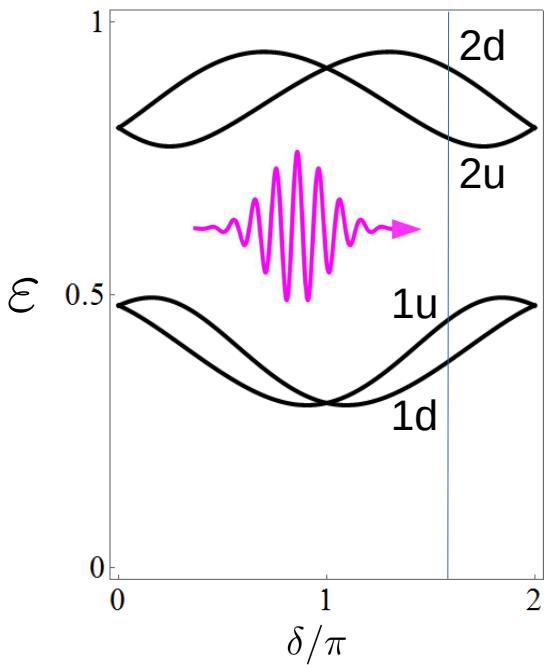
Pair transitions : ground state to excited state



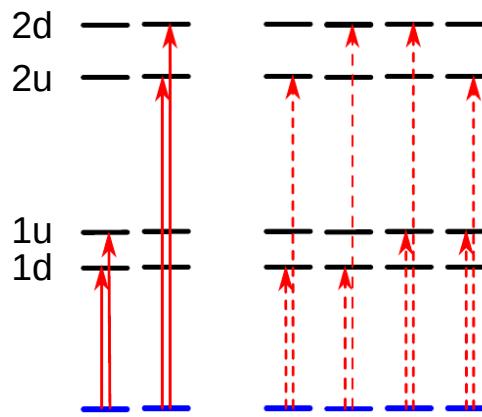
Single quasiparticle transitions



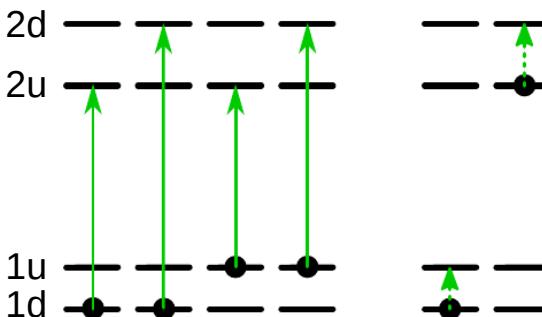
# Transitions between spin-split Andreev levels by a microwave



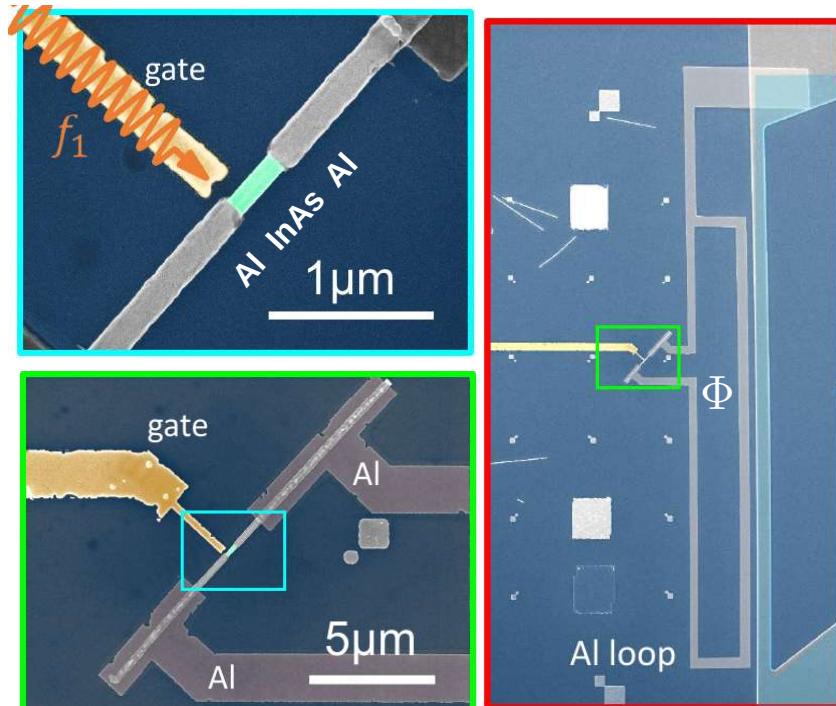
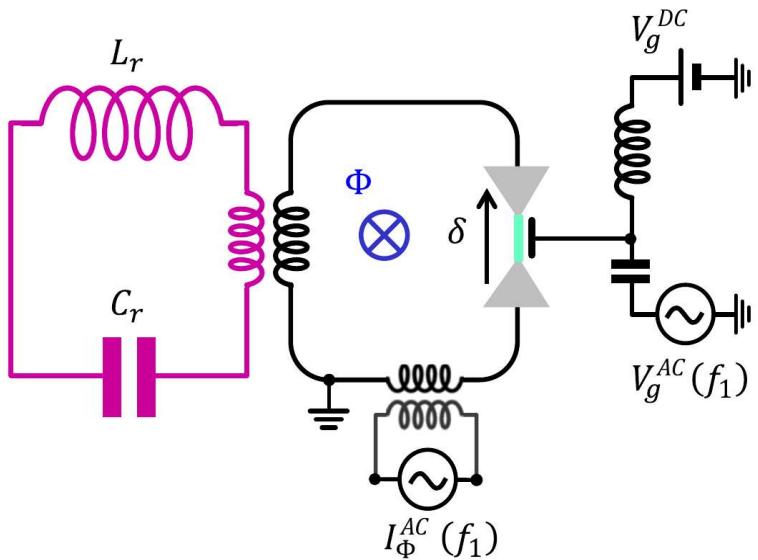
Pair transitions



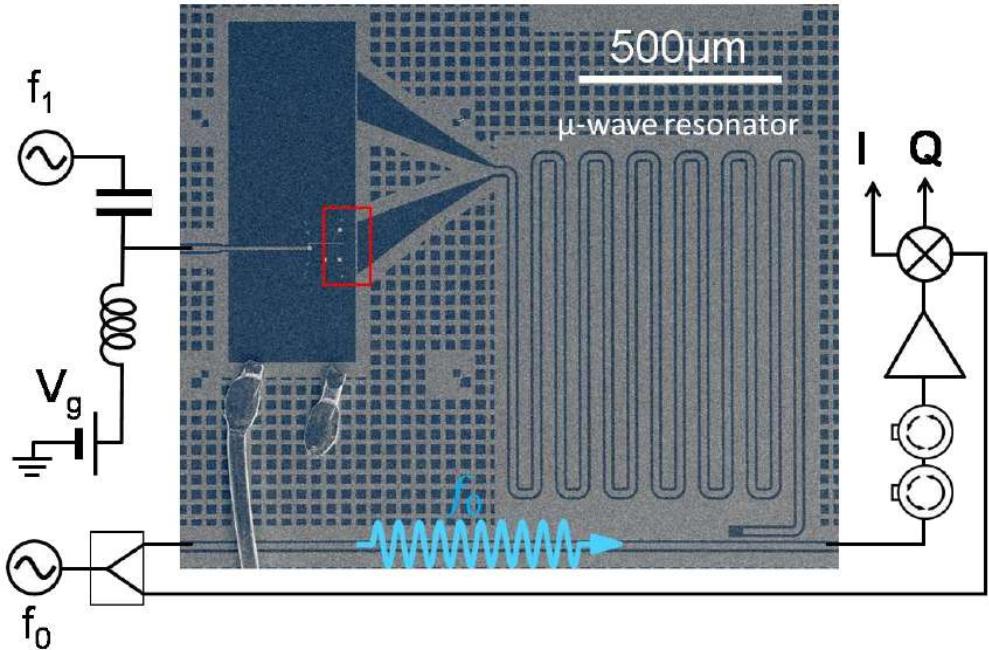
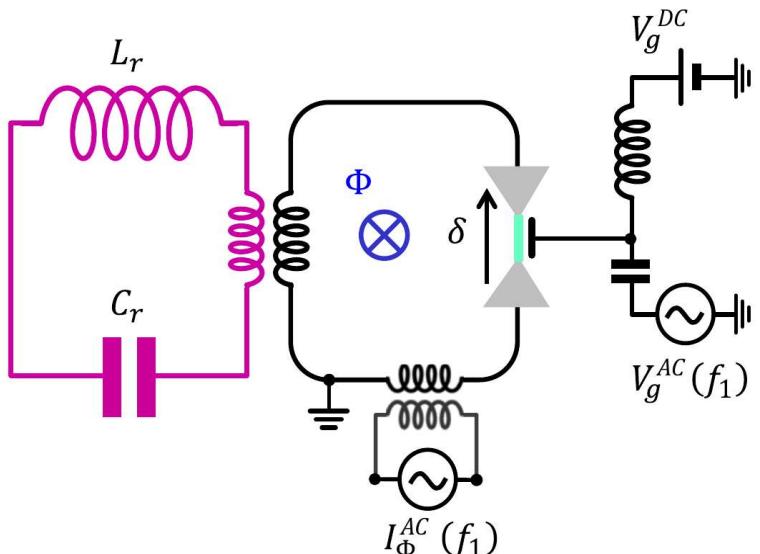
Single particle transitions



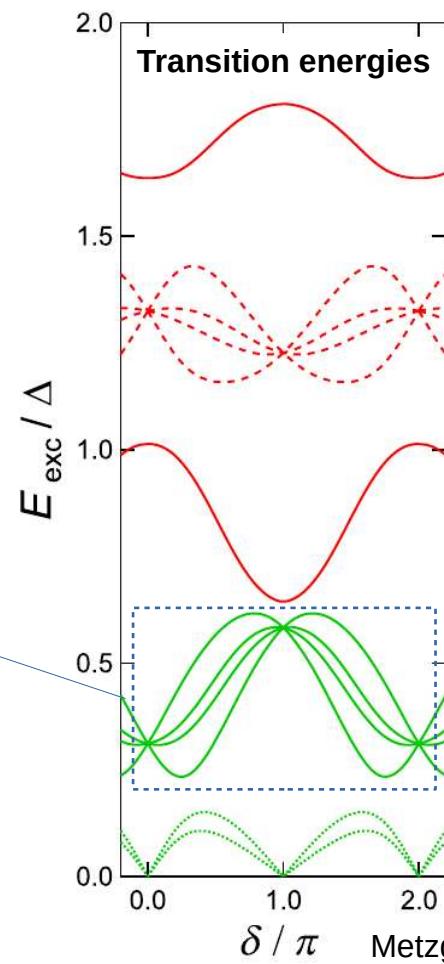
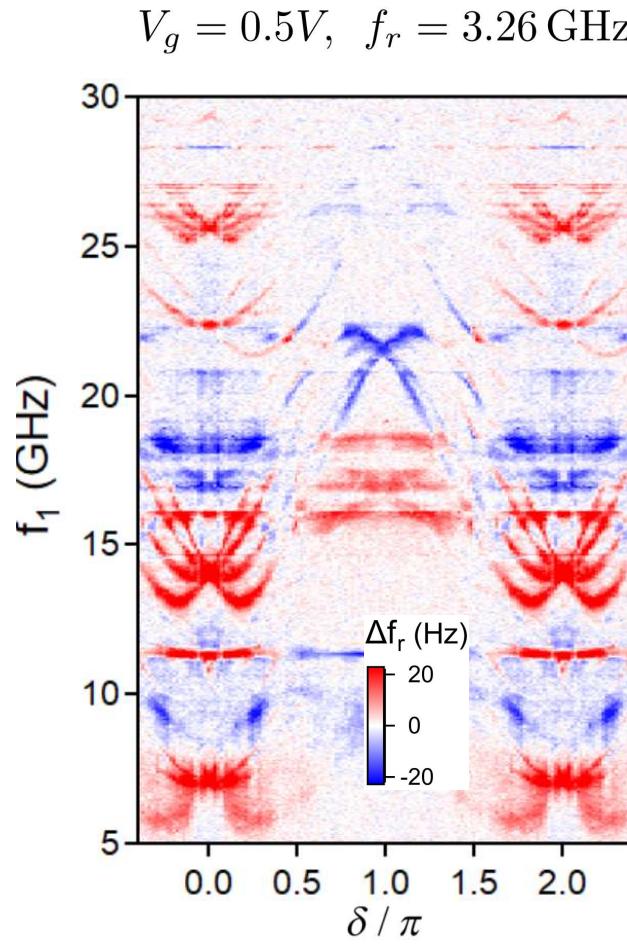
# Experimental setup – Quantronics group at CEA Saclay



# Experimental setup – Quantronics group at CEA Saclay



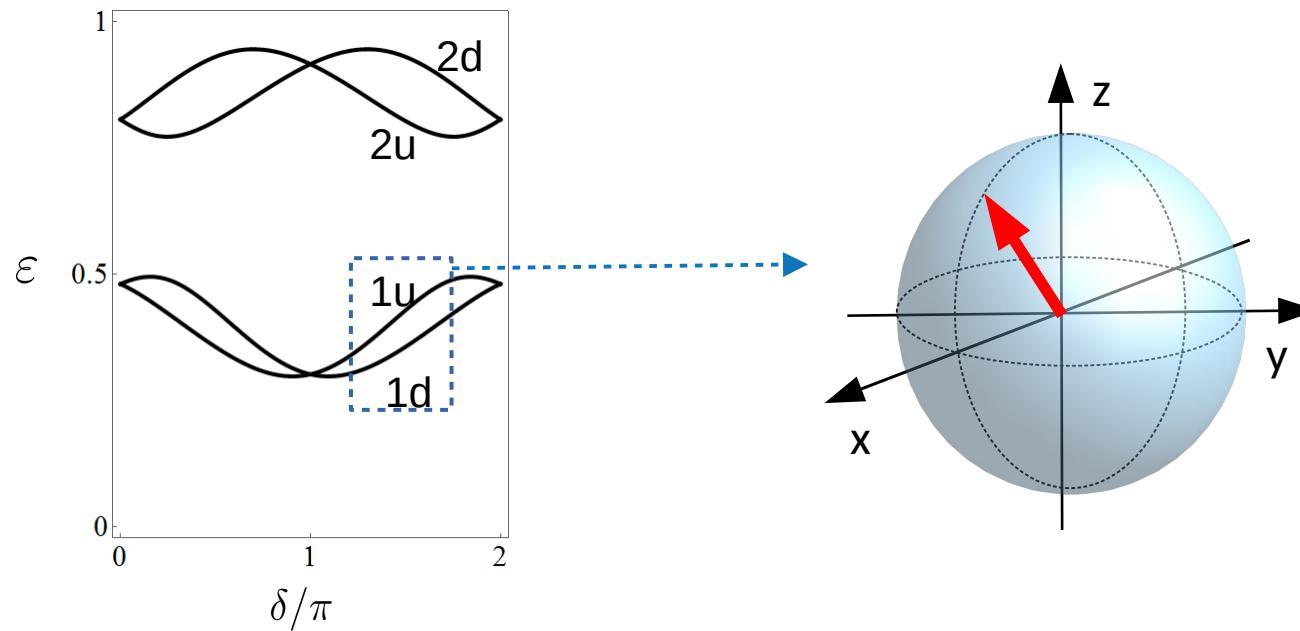
# Two-tone spectroscopy



# TO DO

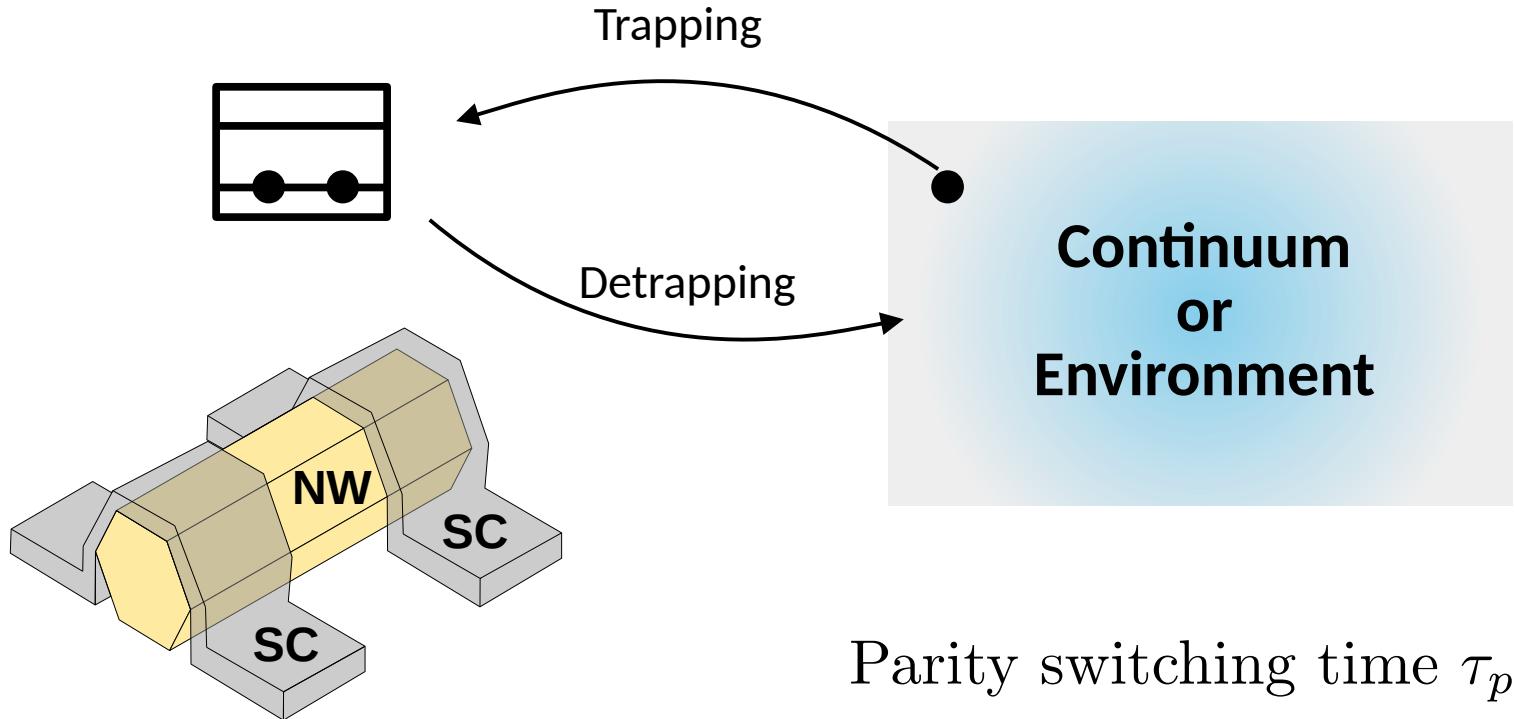
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- On-demand control of Andreev spin qubit
- Is a competitive qubit ? - coherence time



# Fermion parity fluctuation

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# Dynamical polarization of the fermion parity in a nanowire Josephson junction

J. J. Wesdorp<sup>1</sup>, L. Grünhaupt<sup>1</sup>, A. Vaartjes<sup>1</sup>, M. Pita-Vidal<sup>1</sup>, A. Bargerbos<sup>1</sup>,  
L. J. Splitthoff<sup>1</sup>, P. Krogstrup<sup>3</sup>, B. van Heck<sup>2</sup>, and G. de Lange<sup>2</sup>

<sup>1</sup>*QuTech and Kavli Institute of Nanoscience, Delft University of Technology, 2628 CJ, Delft, The Netherlands*

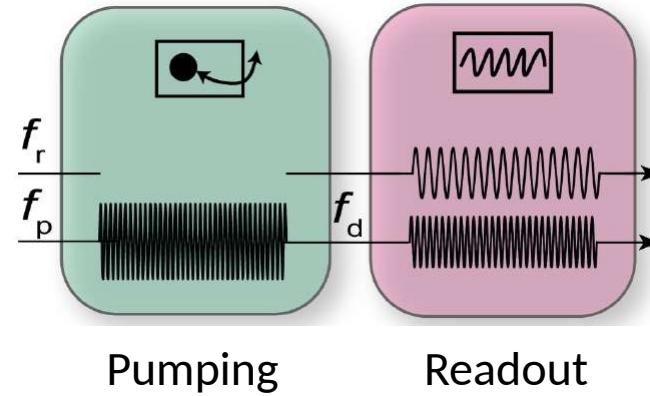
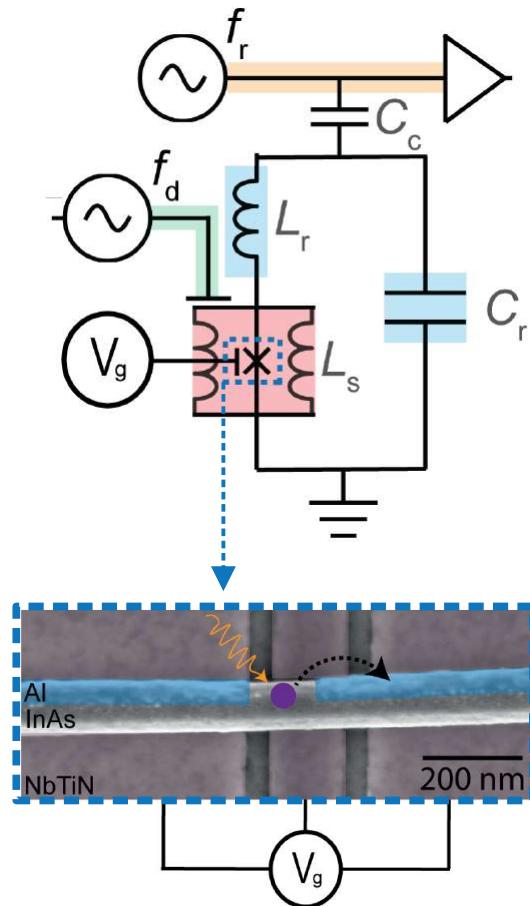
<sup>2</sup>*Microsoft Quantum Lab Delft, 2628 CJ, Delft, The Netherlands*

<sup>3</sup>*Center for Quantum Devices, Niels Bohr Institute,  
University of Copenhagen and Microsoft Quantum Materials Lab Copenhagen, Denmark*

(Dated: December 6, 2021)

“ ... the fermion parity of the junction can be even or odd. ... Here,  
we show that we can **polarize the fermion parity** dynamically using  
microwave pulses ... ”

# Experimental setup

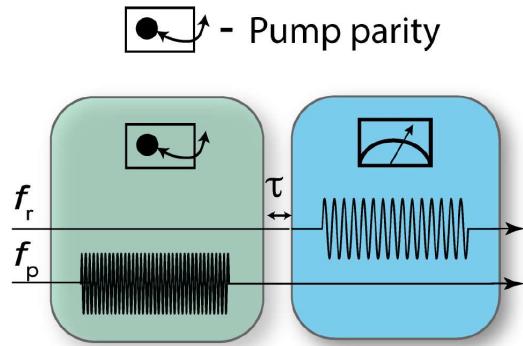


$f_r$  : probe frequency

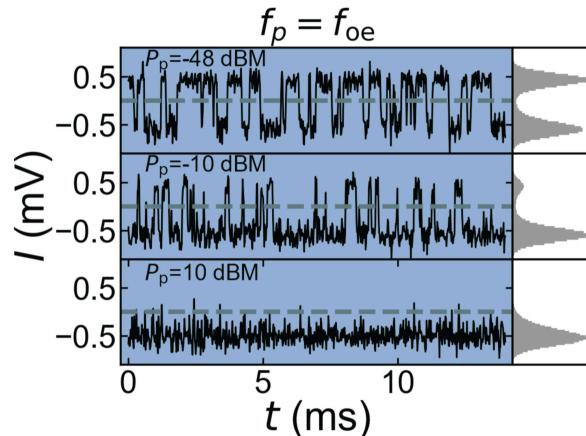
$f_p$  : pumping pulse frequency

$f_d$  : driving frequency

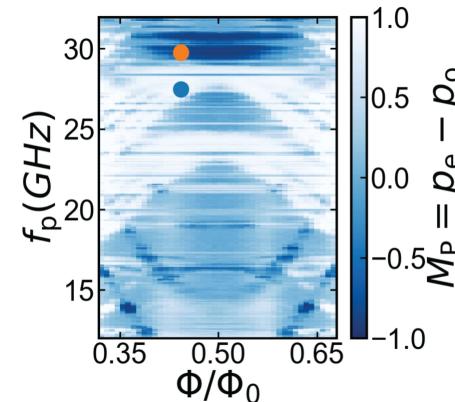
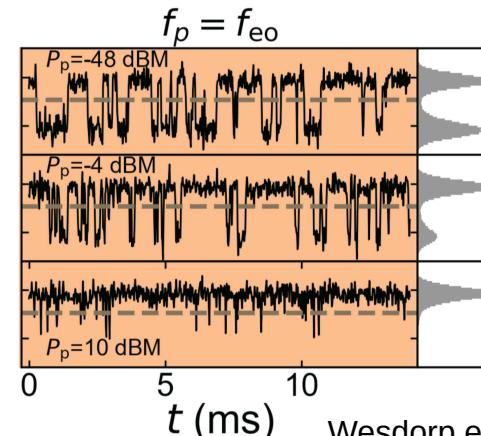
# Fermion parity polarization



Odd pumping  $\rightarrow$  even parity polarization

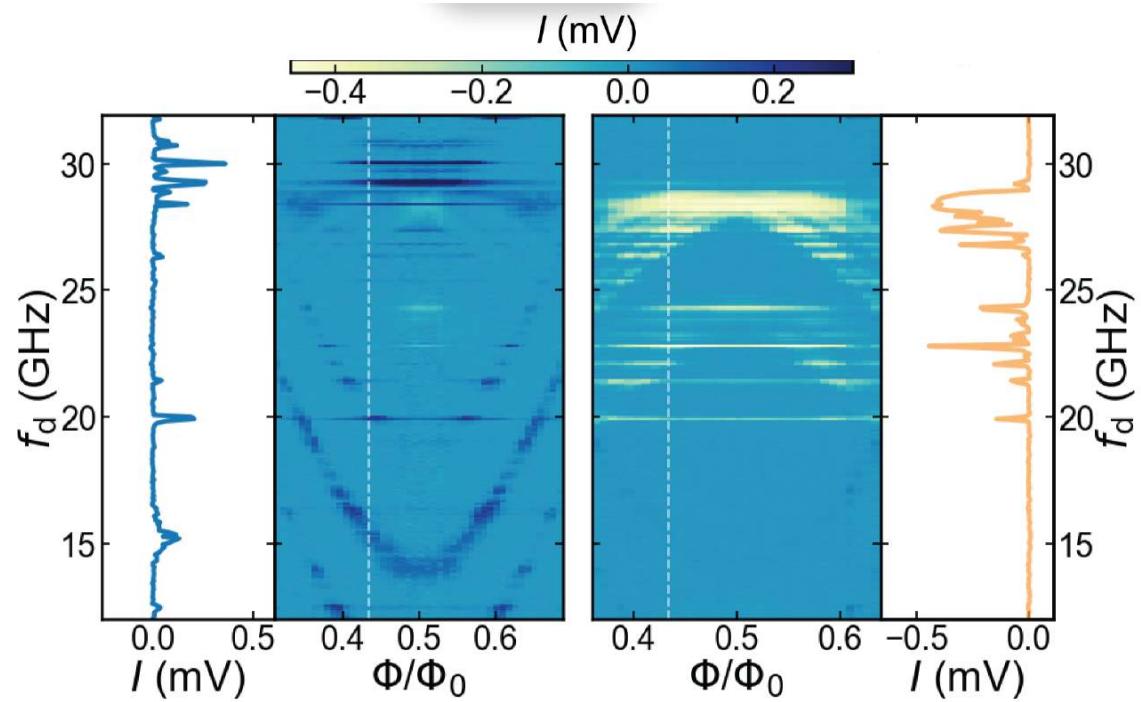
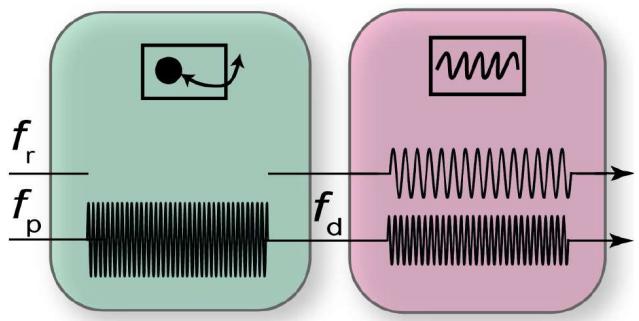


Even pumping  $\rightarrow$  odd parity polarization



# Experimental observation

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## Dynamical parity selection in superconducting weak links

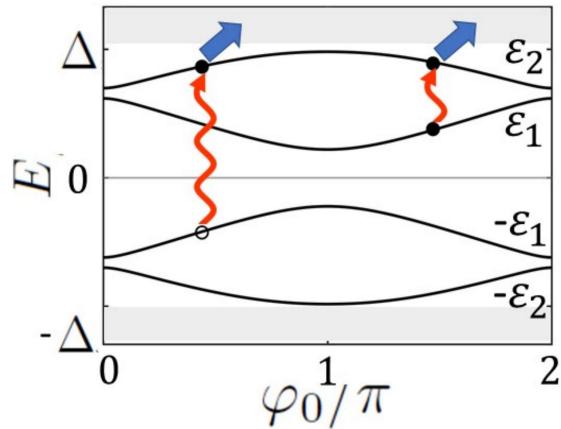
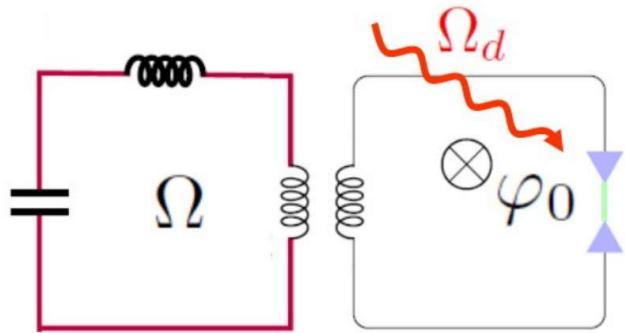
Nico Ackermann,<sup>1</sup> Alex Zazunov,<sup>2</sup> Sunghun Park,<sup>1</sup> Reinhold Egger,<sup>2</sup> and Alfredo Levy Yeyati<sup>1</sup>

<sup>1</sup>*Departamento de Física Teórica de la Materia Condensada,  
Condensed Matter Physics Center (IFIMAC) and Instituto Nicolás Cabrera,  
Universidad Autónoma de Madrid, 28049 Madrid, Spain*

<sup>2</sup>*Institut für Theoretische Physik, Heinrich-Heine-Universität, D-40225 Düsseldorf, Germany*

“ ... dynamical polarization in a given parity sector is achievable by applying a microwave pulse matching a transition in the opposite parity sector. ... ”

# What we solve



Finite length nanowire Josephson junction

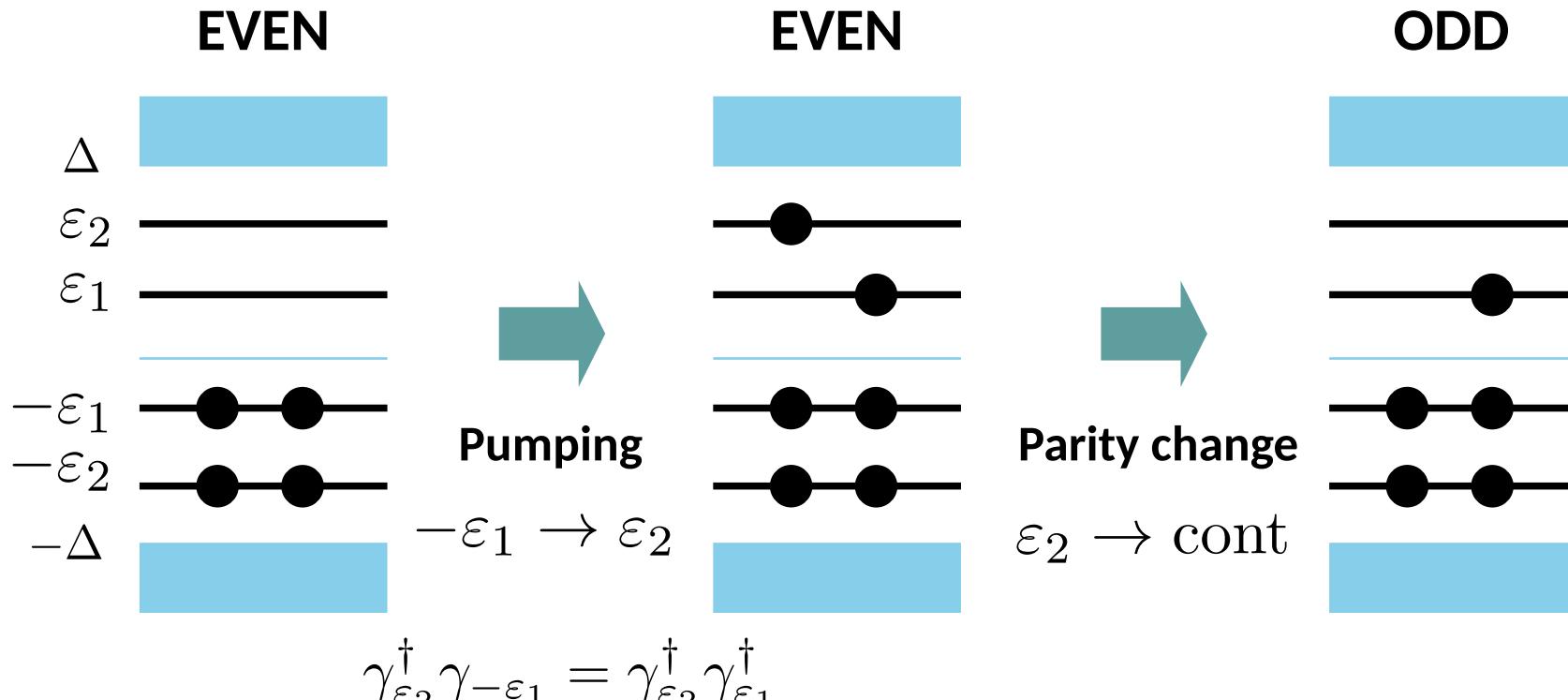
Lindblad equation

$$\dot{\rho} = -i [H_J, \rho] + \sum_{\nu \neq \nu'} \Gamma_{\nu\nu'} \mathcal{L}(Q_{\nu'\nu}) \rho$$

$$\Gamma_{\nu\nu'} = 2\pi |I_{\nu'\nu}|^2 J(\omega_{\nu\nu'}) [n_B(\omega_{\nu\nu'}) + 1]$$

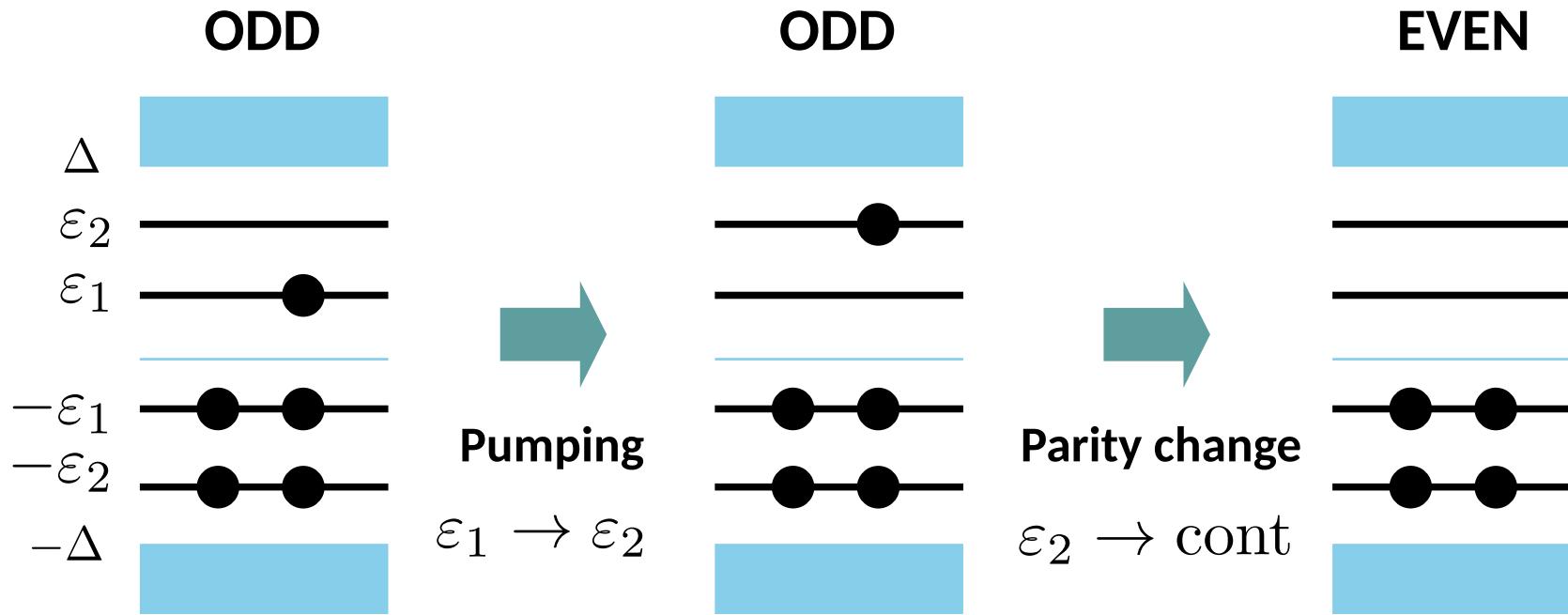
$$\mathcal{L}(Q_{\nu'\nu}) \rho = Q_{\nu'\nu} \rho Q_{\nu'\nu}^\dagger - \frac{1}{2} \left\{ Q_{\nu'\nu}^\dagger Q_{\nu'\nu}, \rho \right\}$$

# Main mechanism – Odd polarization



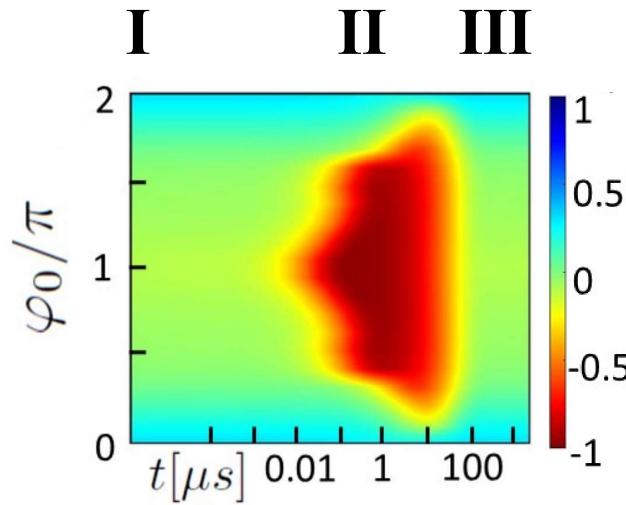
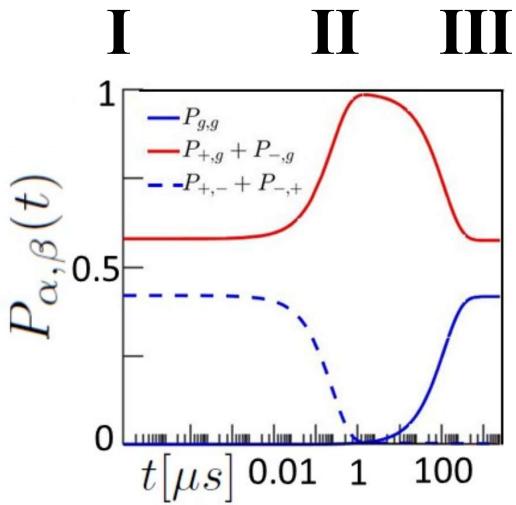
Mixed pair transition → Odd parity polarization

# Main mechanism – Even polarization

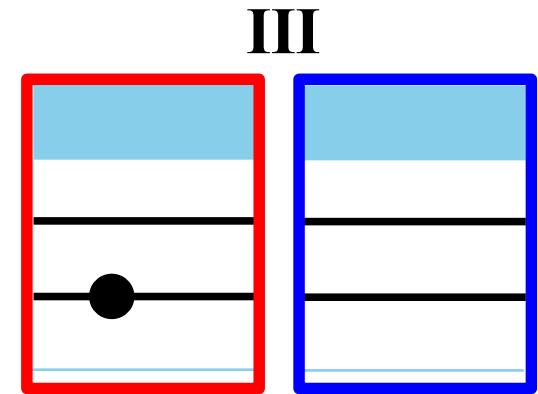
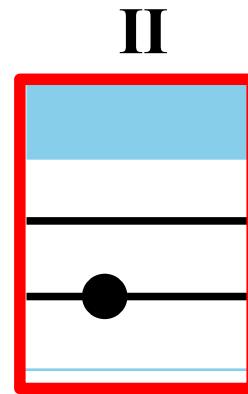
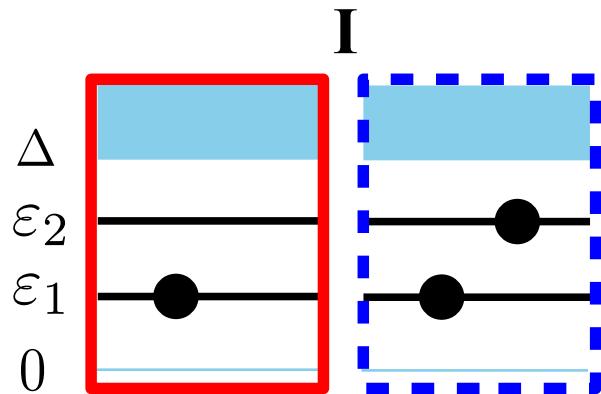


Single quasiparticle transition → Even parity polarization

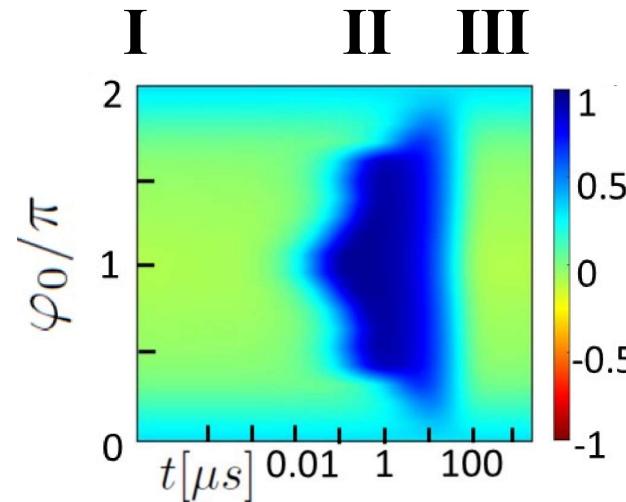
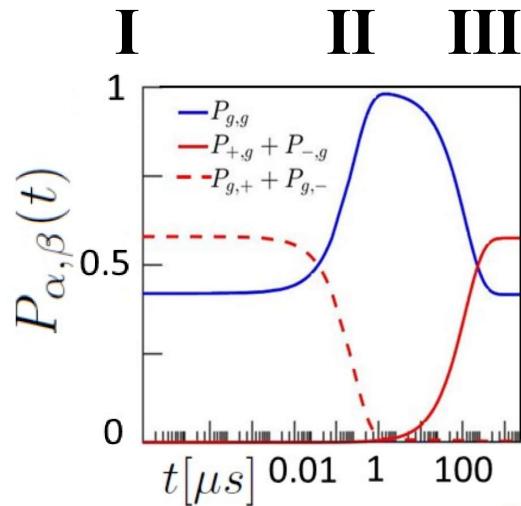
# Theory results – Odd polarization



**I:**  $P(t=0)$   
**II:** Transient period  
**III:** Stationary period

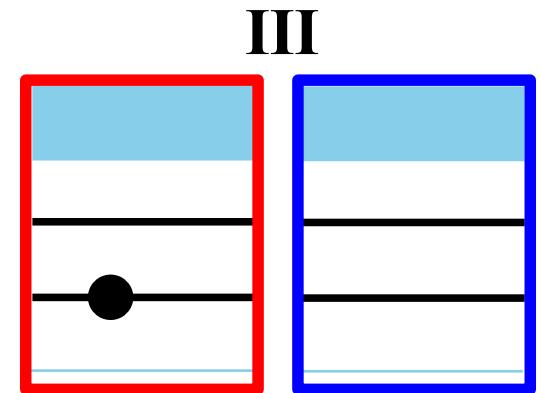
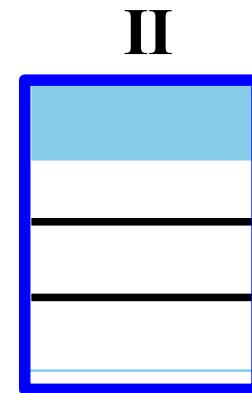
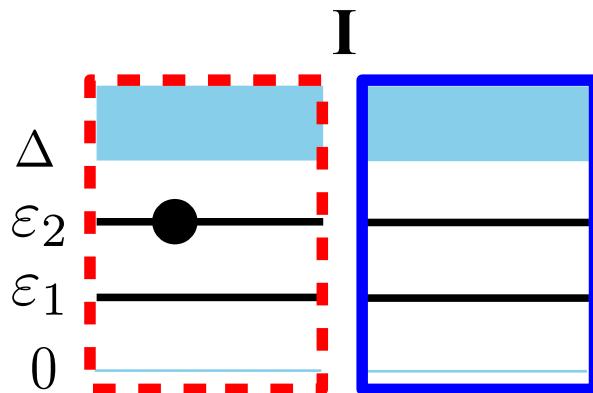
$$\Delta P(t) = P_{\text{even}}(t) - P_{\text{odd}}(t)$$


# Theory results – even polarization



**I:**  $P(t=0)$   
**II:** Transient period  
**III:** Stationary period

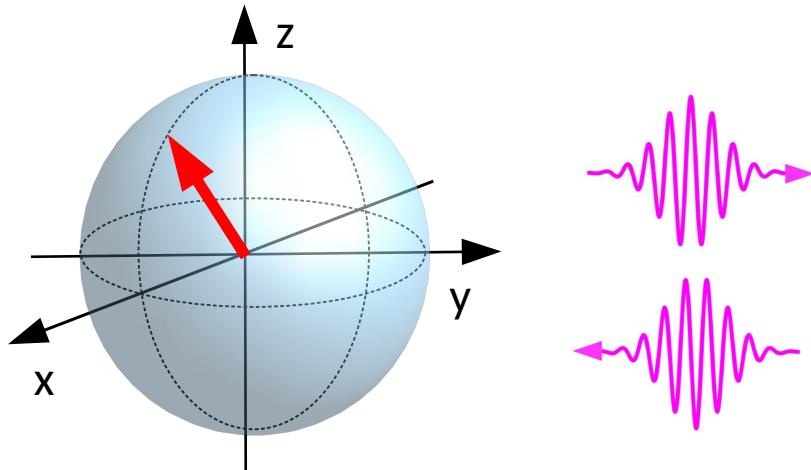
$$\Delta P(t) = P_{\text{even}}(t) - P_{\text{odd}}(t)$$



# TO DO

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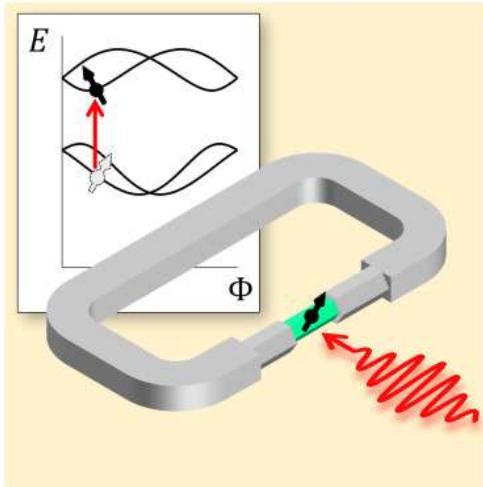
- Theoretical study of the spin-orbit effect
- How to use a bath (environment & continuum) for qubit control



**Continuum  
or  
Environment**

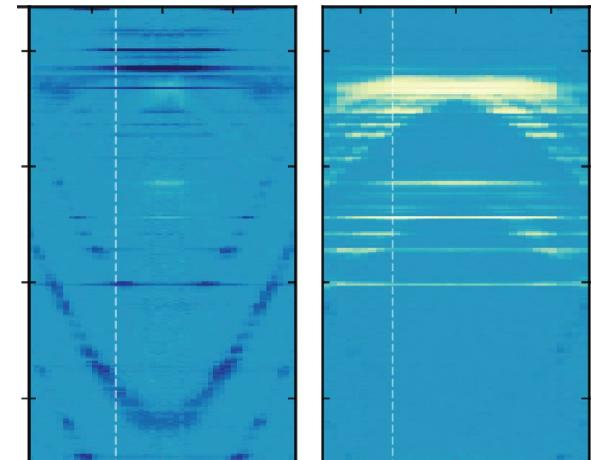
# Summary

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- Nanowire Josephson junction
  - Spin-orbit coupling and multichannel structure
  - Spin-split Andreev levels at zero magnetic field

- Research towards real device applications
  - Coherent manipulation by a microwave
  - Dynamical control of fermion parity



## Acknowledgments:

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Cyril Metzger (Boulder, USA)

Alex Zazunov, Reinhold Egger (Dusseldorf, Germany )